

# Deploying Differential Privacy in Industry: Progress and Learnings



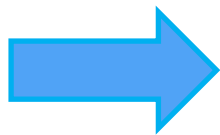
Ryan Rogers

Staff Software Engineer, LinkedIn  
November 29, 2021, UCSB



**Collaborators:** Subbu Subramaniam, Sean Peng, Seunghyun Lee, Sajjad Moradi, Akash Kaura, Nikhil Gahlawat, Adrian Rivera Cardoso, Mark Cesar, Jinshuo Dong, David Durfee, Koray Mancuhan, Paul Ko, Santosh Kumar Kancha, Neha Jain, Shraddha Sahay, Parvez Ahammad, Ya Xu

# Agenda

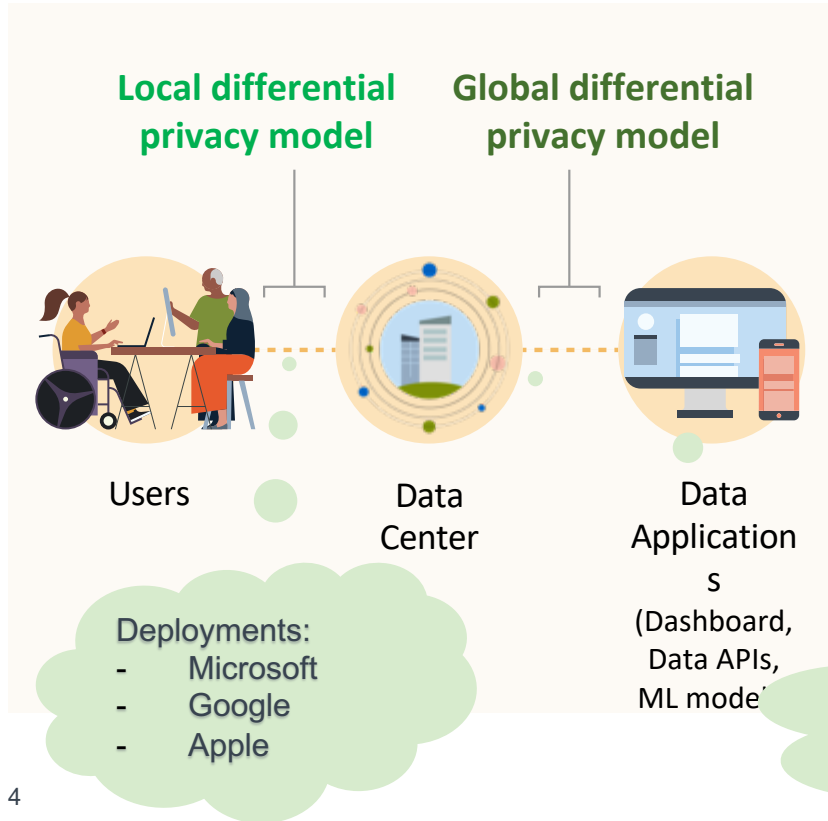


- 1 Overview of Differential Privacy
- 2 Overview of DP approach at LinkedIn
- 3 DP Top- $k$  Algorithms
- 4 Privacy Budget Management
- 5 Deployments and Conclusion

## Mission

Utilizing data while  
protecting the privacy of  
members.

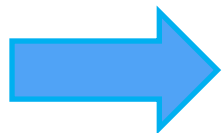
# Models and Deployments of Differential Privacy



- Traditional data protection techniques are not sufficient to defend data privacy
- Differential Privacy ensures data learnings are similar with/without a single member's data



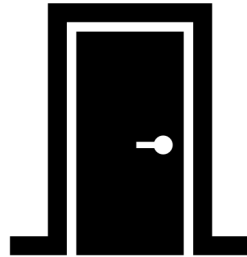
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# Initial Discussions

- What teams are interested in releasing aggregates?
- What are the general problems and what solutions would be the most applicable?
- What additional constraints are there?

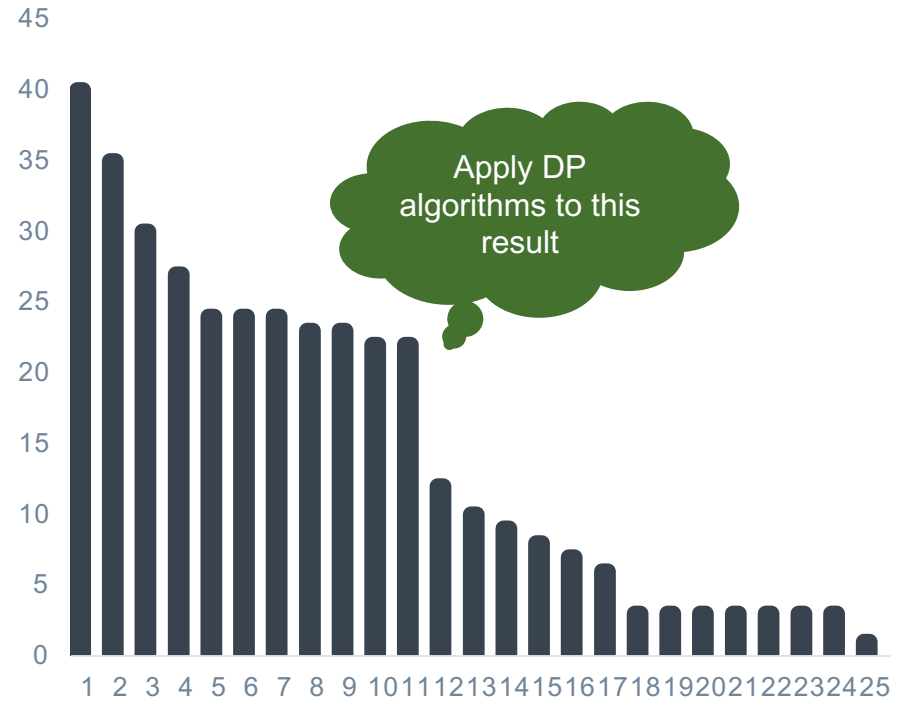
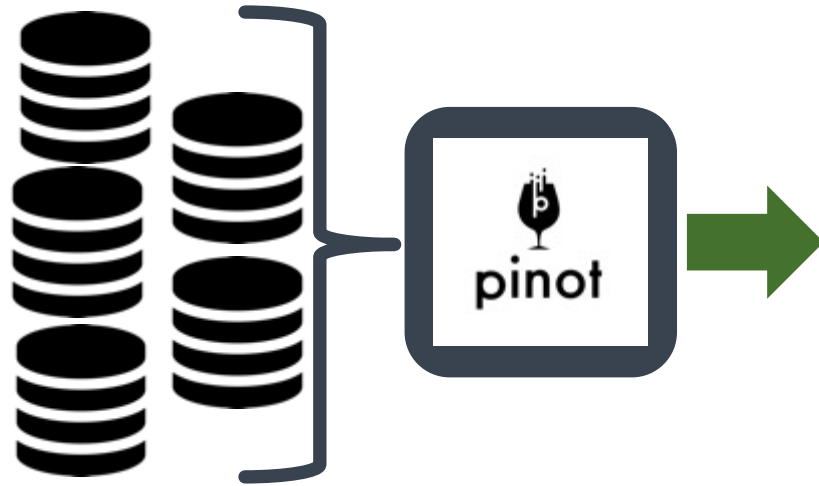


## Key Takeaways

- Existing infrastructure for computing aggregates quickly.
- Want tunable privacy as well as tunable run time.
- Lots of data analytics can be reduced to histograms.
- Labels of the histograms are not always known.
- Typically, only want top- $k$  results
- Want consistent results, see PriPeARL [Kenthapadi,Tran'18].

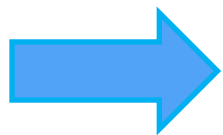


# Existing Systems for Data Analytics





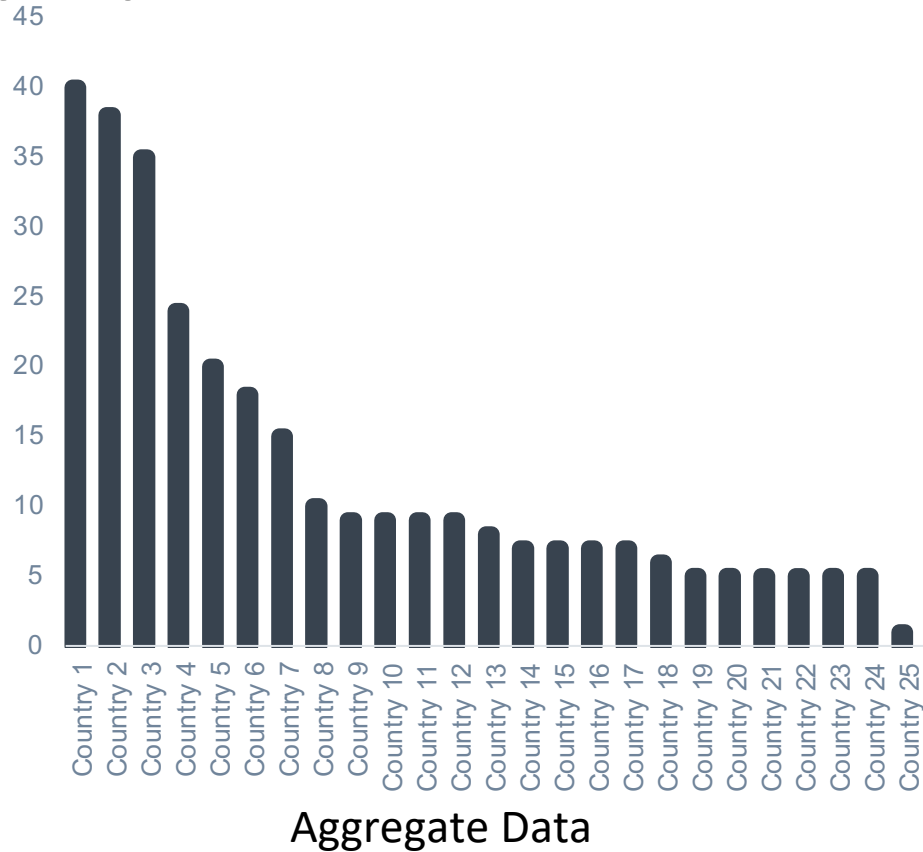
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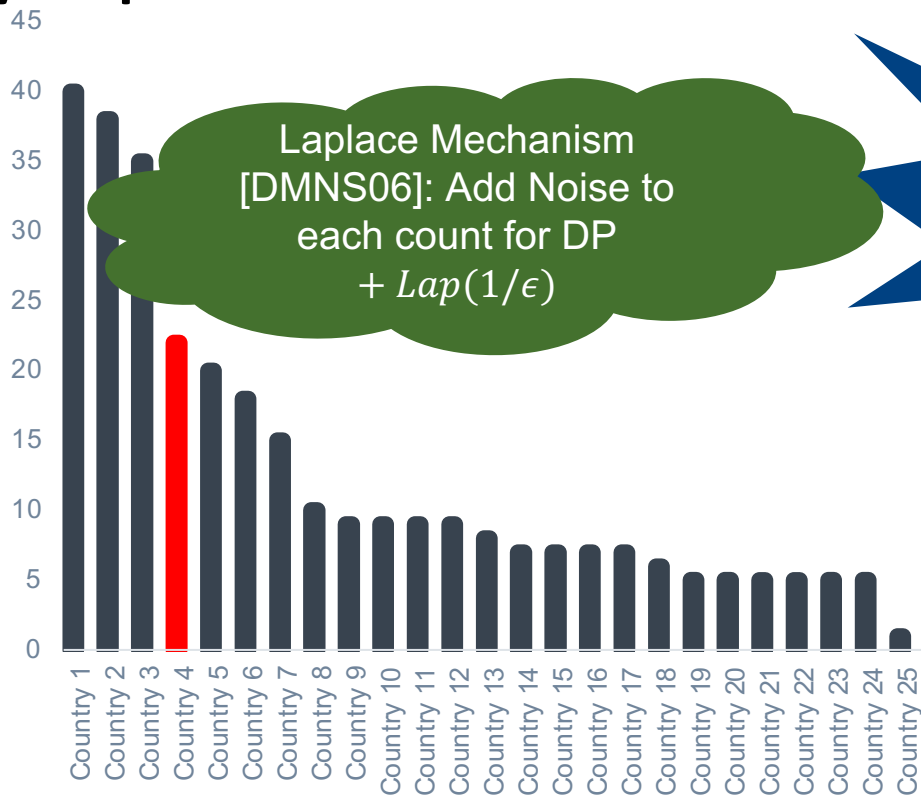
# Sensitivity of the Query

**Query: Top-10 countries with certain skill set?**



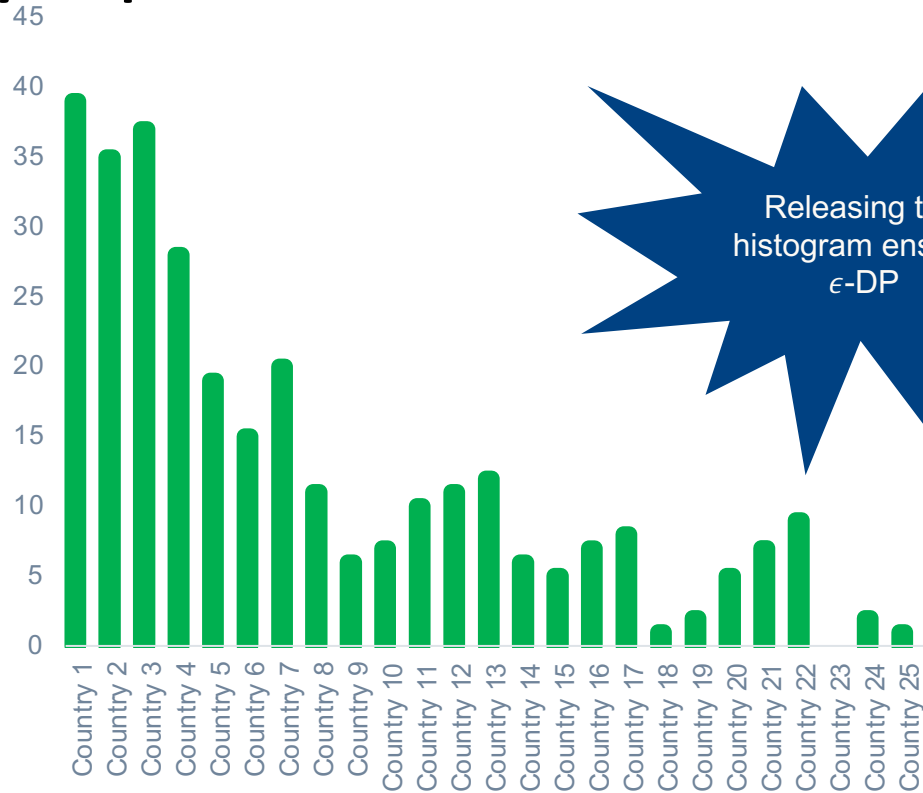
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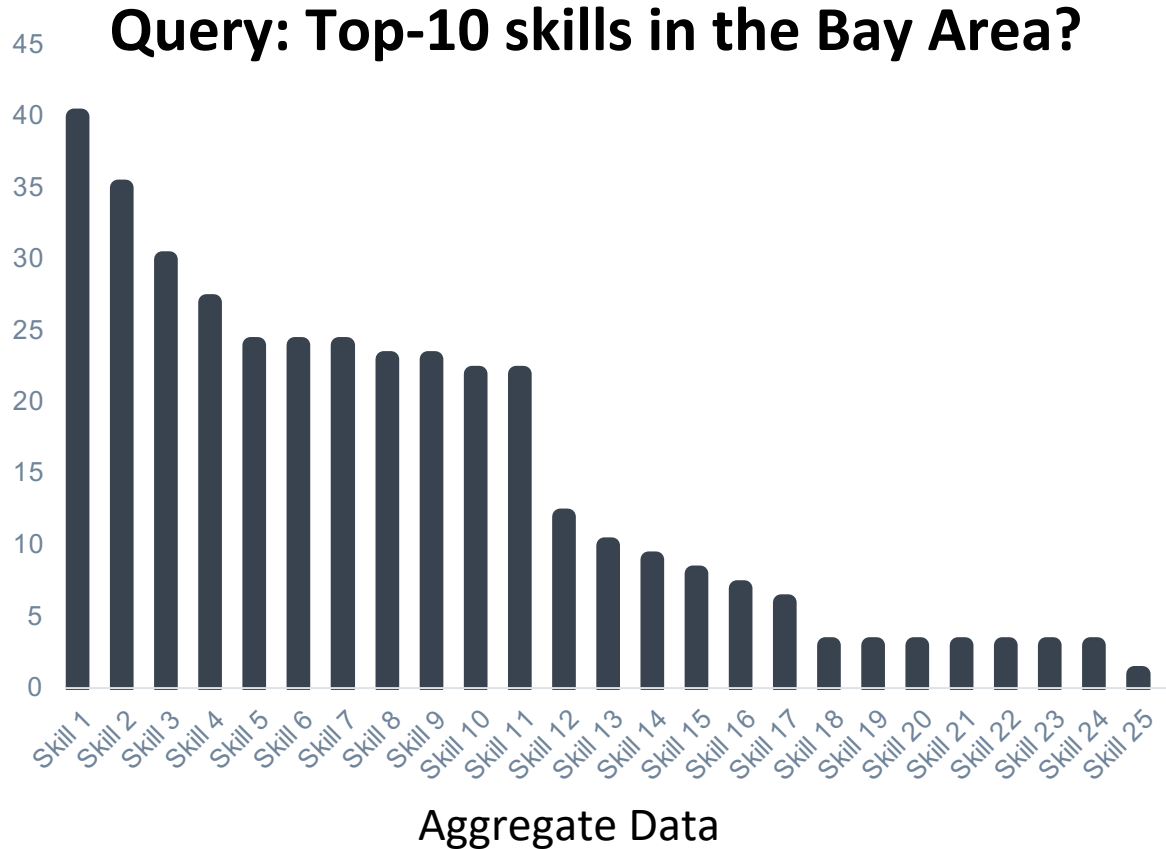
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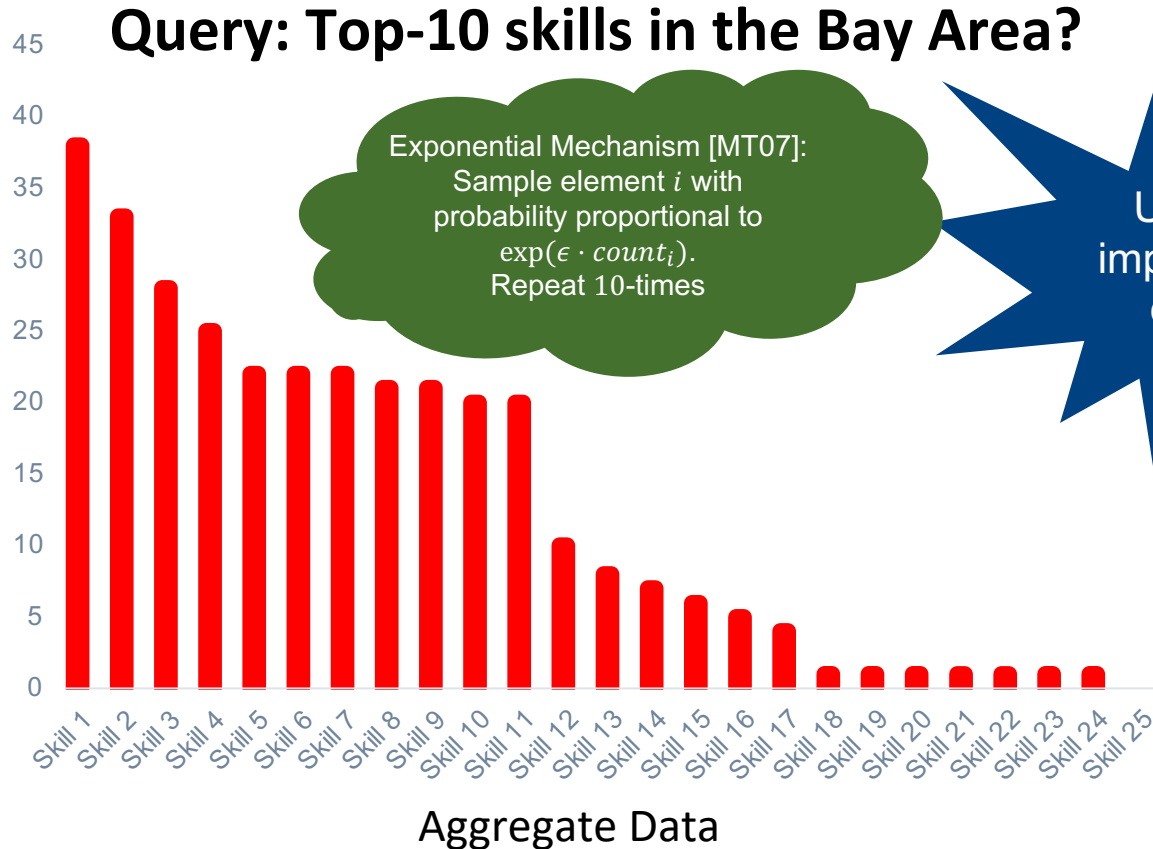


Aggregate Data

# Sensitivity of the Query



# Sensitivity of the Query



# Sensitivity of the Query

## Query: Top-10 skills in the Bay Area?

Exponential Mechanism [MT07]:  
Sample element  $i$  with  
probability proportional to  
 $\exp(\epsilon \cdot \text{count}_i)$ .  
Repeat 10-times

Releasing only elements in top- $k$   
(not their counts) ensures  
 $k\epsilon$ -DP

# Known Algorithms for Private Data Analytics

$\ell_0$ -Restricted Sensitivity	$\ell_0$ -Unrestricted Sensitivity
<b>Algorithm: Laplace Mechanism</b> [DMNS'06]	<b>Algorithm: Exponential Mechanism</b> [MT'07]



# Implementing Exp Mech

- Folklore result: Exp Mech = Adding *Gumbel*  $\left(\frac{1}{\epsilon}\right)$  to each count and reporting the arg noisy max.
- [DR'19] Can simulate repeated Exponential Mechanisms in one-shot this way to get  $\left(\approx \epsilon \sqrt{k \log \frac{1}{\delta}}, \delta\right)$ -DP.
- Improves on work from [Dwork, Su, Zhang '15] and [Garg, Su, Zhang '21] that adds *Laplace*  $\left(\frac{1}{\epsilon}\right)$  to each count and reports the  $k$  largest noisy count elements in order.



See blog post:  
<https://differentialprivacy.org/one-shot-top-k/>

# Known Algorithms for Private Data Analytics

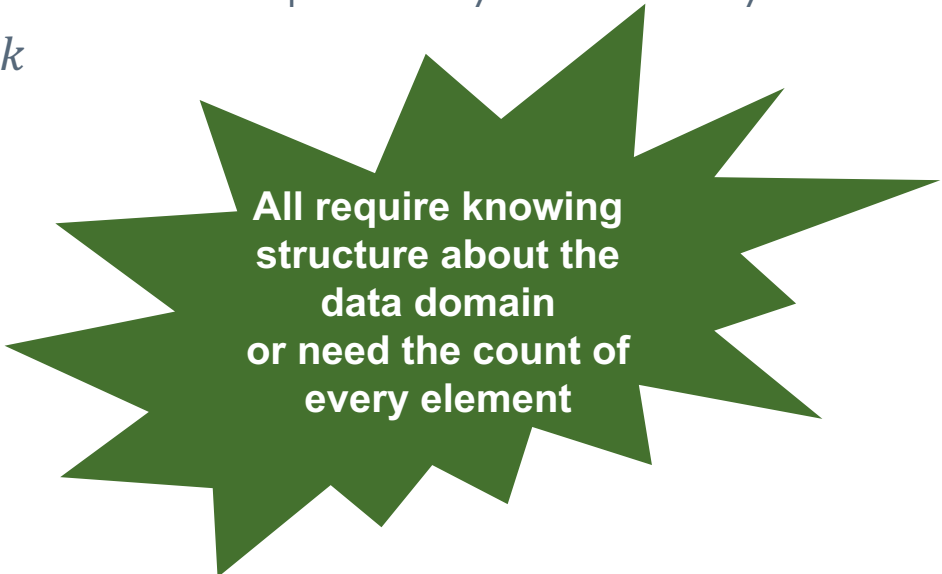
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# Known Algorithms for Private Data Analytics

$\ell_0$ -Restricted Sensitivity	$\ell_0$ -Unrestricted Sensitivity
<b>Algorithm: Known Laplace</b> [DMNS'06]	<b>Algorithm: Known Gumbel</b> [MT'07]

# Solving Top- $k$ subject to DP

- One of the most fundamental problems in exploratory data analytics
- Lots of work in DP on solving top- $k$ 
  - Local Model of DP (Heavy Hitters)
    - Bassily and Smith STOC'15
    - Fanti, Pihur, Erlingsson PoPETS'16
    - Bassily, Nissim, Stemmer, Thakurta NIPS'17.
  - Global Model of DP
    - Bhaskar, Laxman, Smith, Thakurta KDD'10
    - Li, Qardaji, Su, Cao VLDB'12
    - Zeng, Naughton, Cai VLDB'12
    - Lee and Clifton, KDD'14
    - Chaudhuri, Hsu, Song NIPS'14
    - Zhu, Kairouz, Sun, McMahan, Li '19

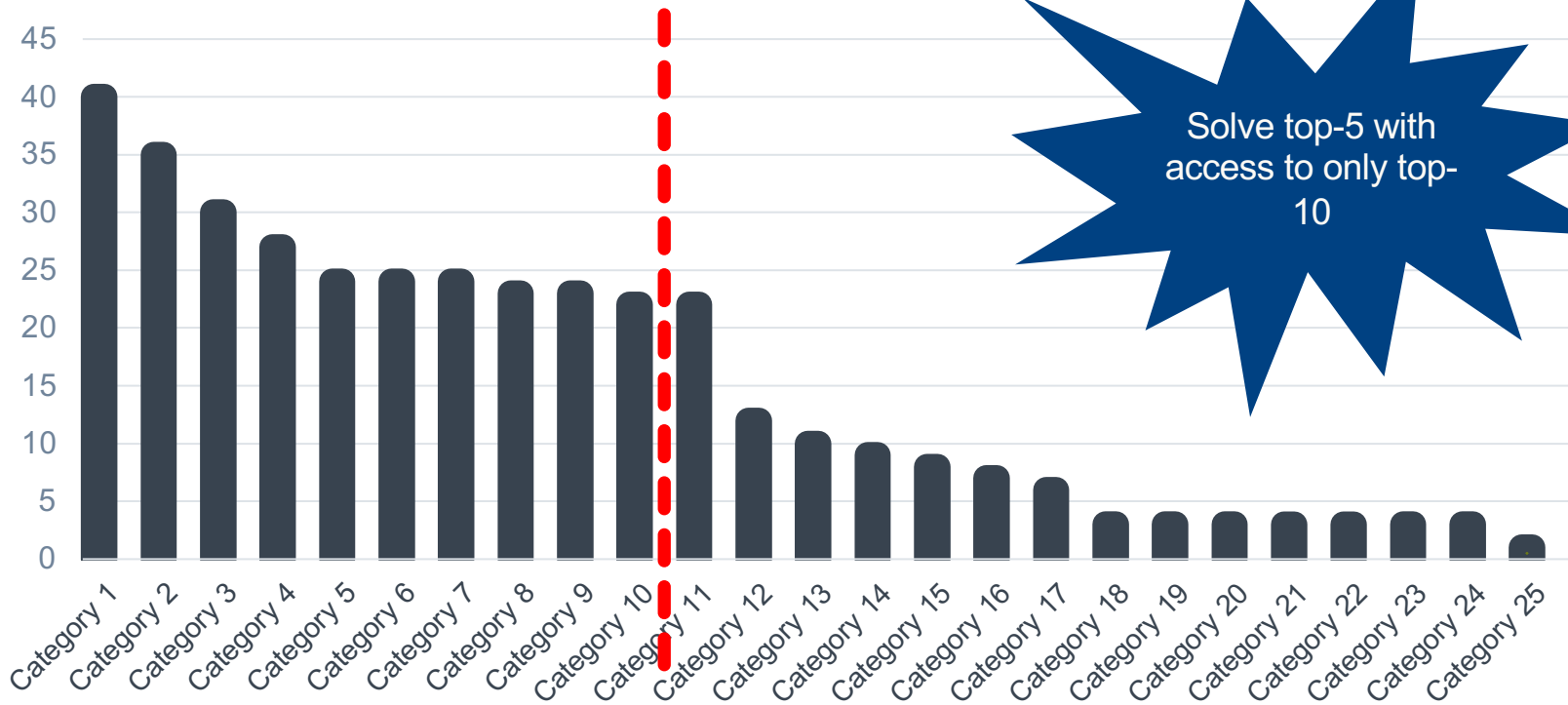


**All require knowing  
structure about the  
data domain  
or need the count of  
every element**

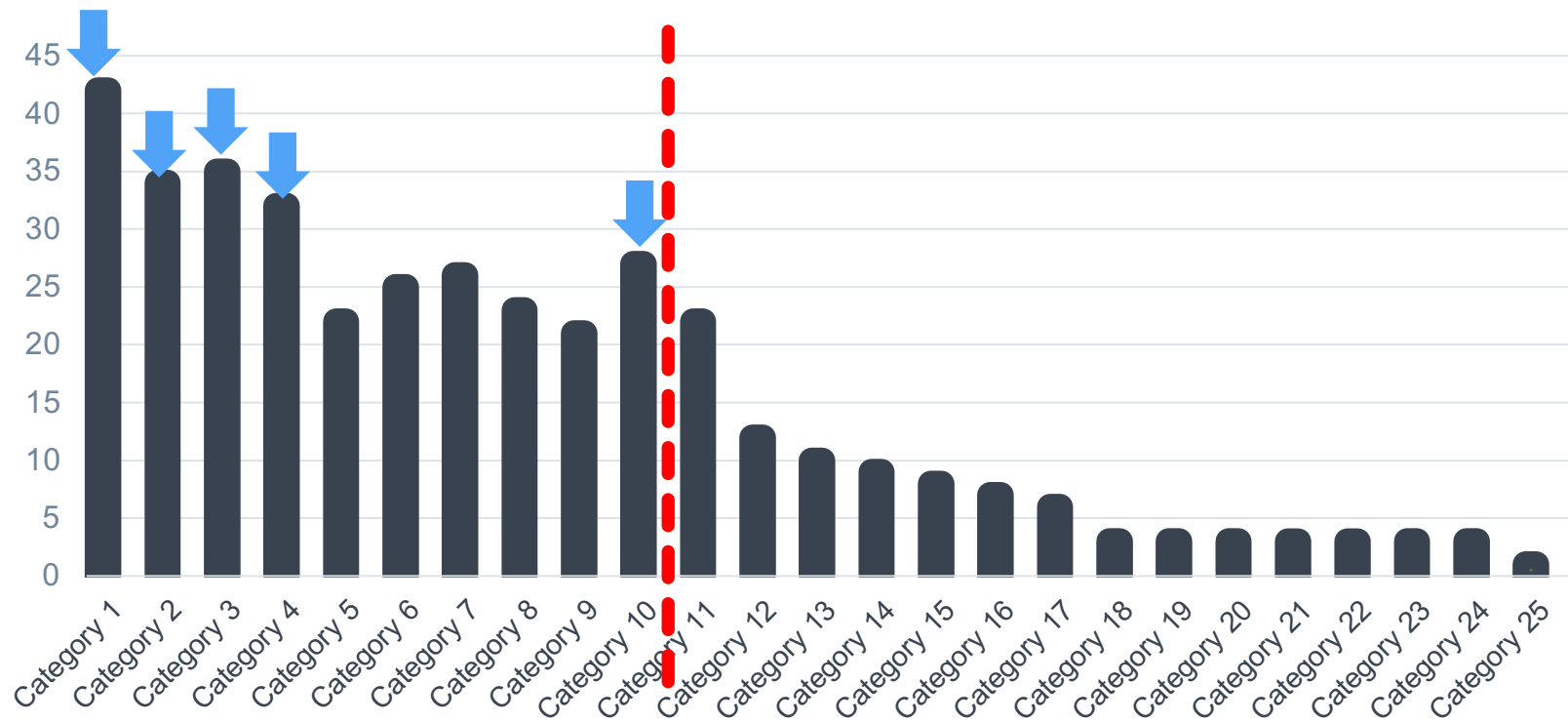
# Unknown Domain Setting

- Typically, the domain is unknown or very large and we restrict how many elements to consider
- Lots of prior work for Frequent Itemsets, but requires knowing structure of the data domain universe.
  - Can prune the number of things we need to query.
- Related work requiring full histogram:
  - [Korolova, Kenthapadi, Mishra, Ntoulas '09]
  - [Wilson, Zhang, Lam, Desfontaines, Simmons-Marengo, Gipson'20]
  - DP Set Union [Gopi, Gulhane, Kulkarni, Shen, Shokouhi, Yekhanin '20]

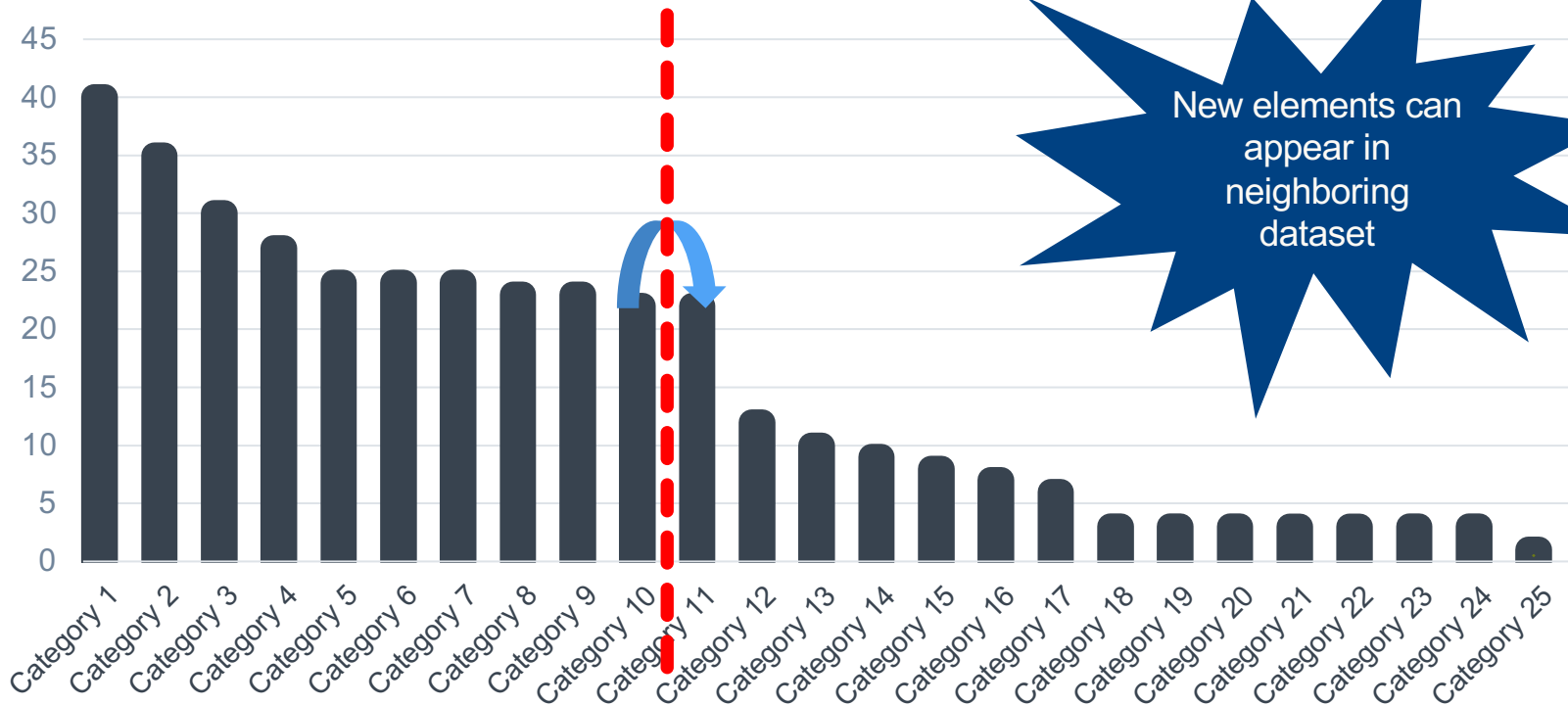
# First Attempt



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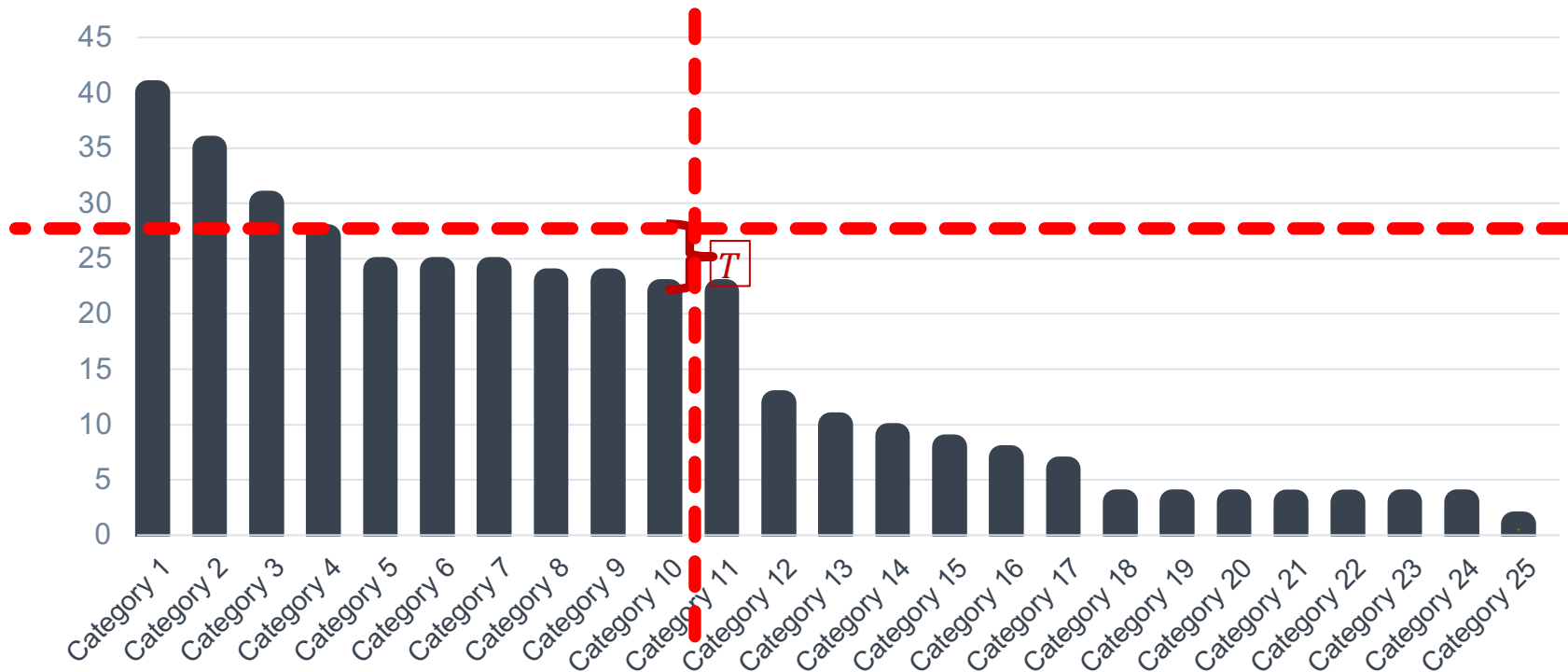


~~First Attempt~~

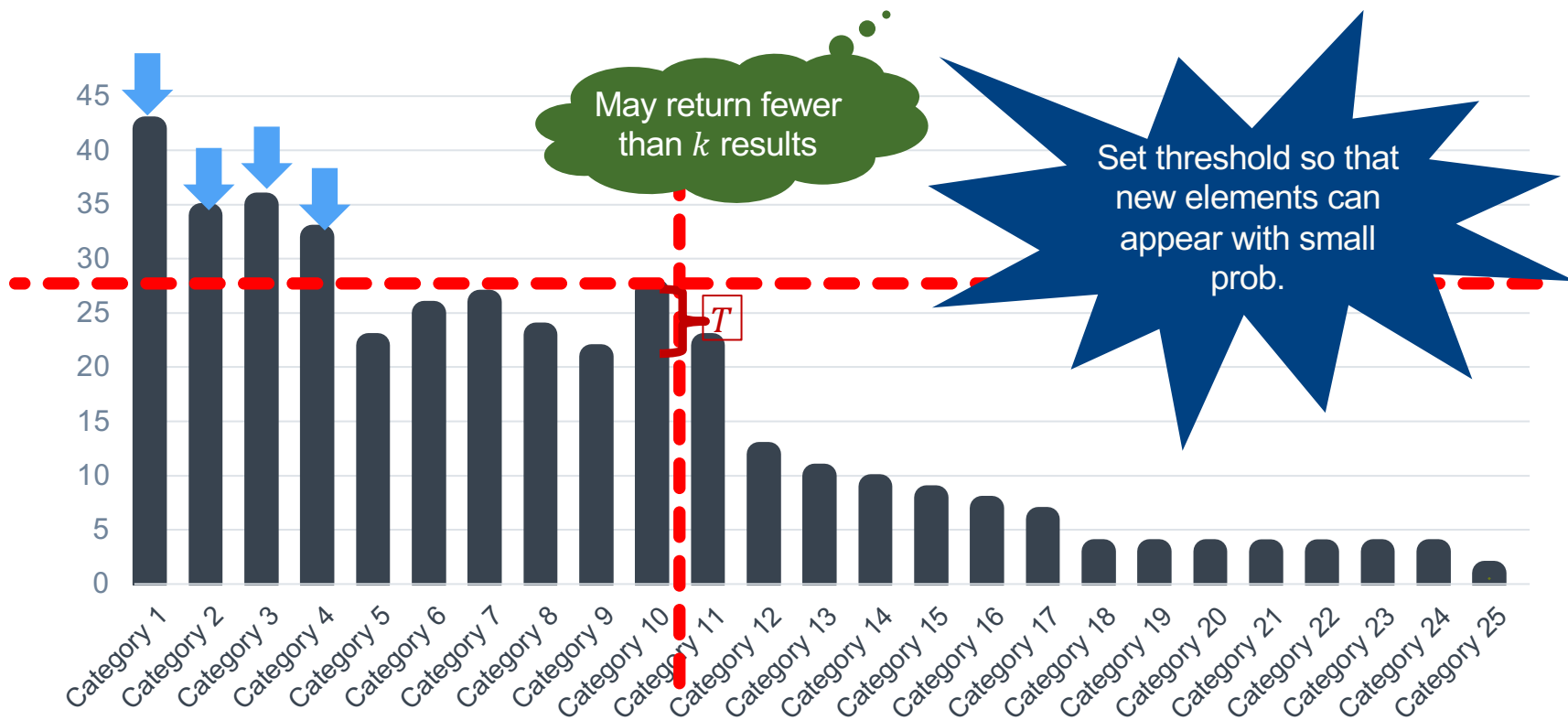




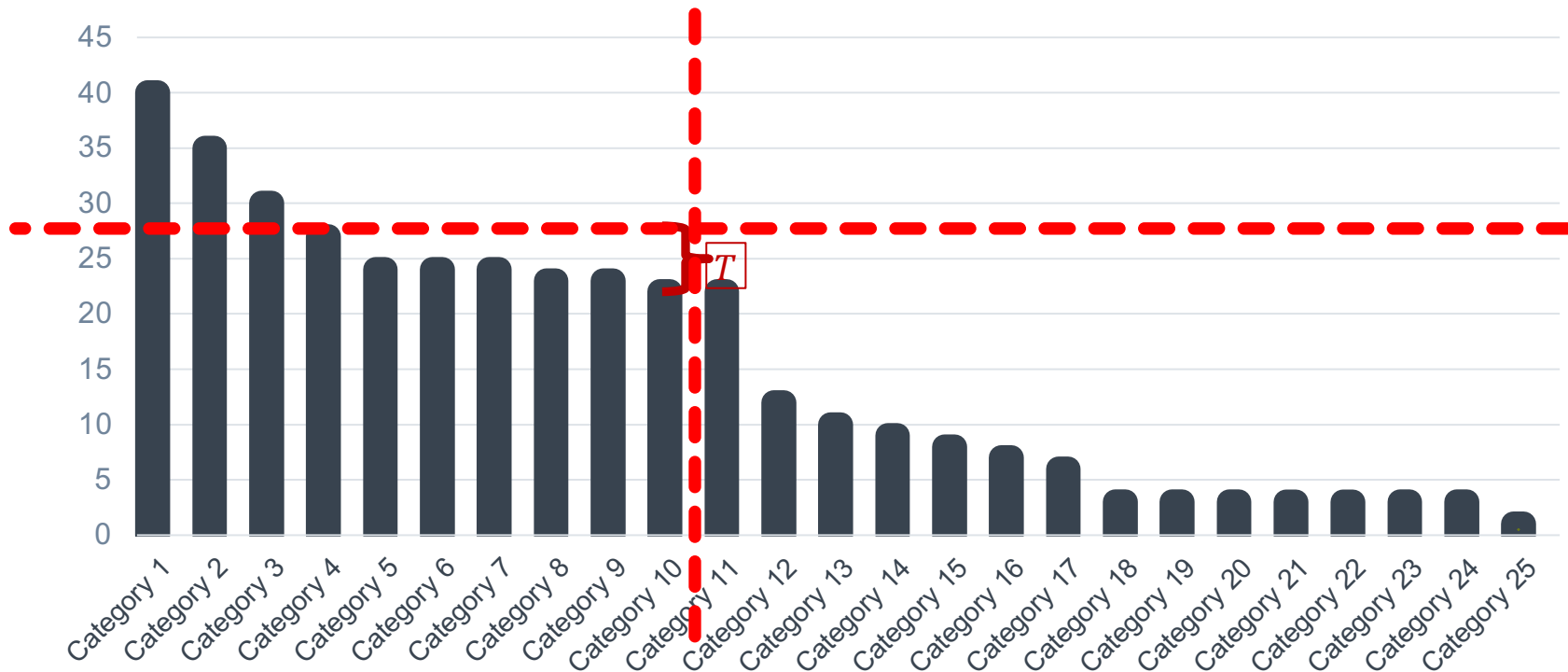
## Second Attempt – Include a Threshold



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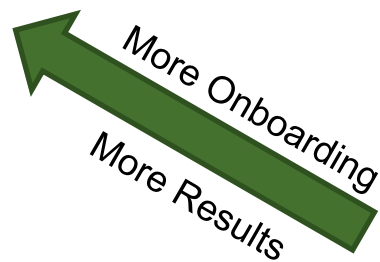


# Algorithms for Private Data Analytics

<i>DP Algorithms</i>	$\ell_0$ -Restricted Sensitivity	$\ell_0$ -Unrestricted Sensitivity
Known Domain	Known Laplace [DMNS'06]	Known Gumbel [MT'07]

# Algorithms for Private Data Analytics

<i>DP Algorithms</i>	$\ell_0$ -Restricted Sensitivity	$\ell_0$ -Unrestricted Sensitivity
Known Domain	Known Laplace [DMNS'06]	Known Gumbel [MT'07]
Unknown Domain	Unknown Laplace [Durfee, R'19]	Unknown Gumbel [Durfee, R'19]



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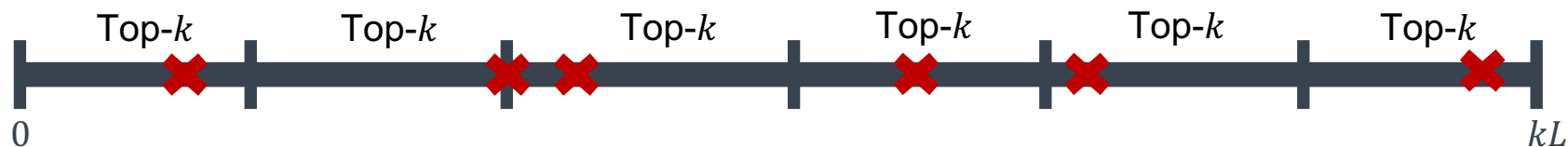
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## What is the Overall Privacy Loss?

- Assume that the  $k$  in each top- $k$  query is the same, at most  $L$  queries are allowed, and only using Unknown Gumbel.
  - Advanced Composition [Dwork, Rothblum, Vadhan '10]:  
$$\left( \approx \epsilon \sqrt{Lk \log \frac{1}{\delta}}, (L + 1)\delta \right)\text{-DP}$$
- Algorithm can give fewer results than what is asked.
  - Is it possible to only pay for what you get?

# Pay-what-you-get Composition [DR'19]

- Assume there is a global budget  $(\epsilon_g, \delta_g)$  with  $\epsilon$ -parameter in each Unknown Gumbel



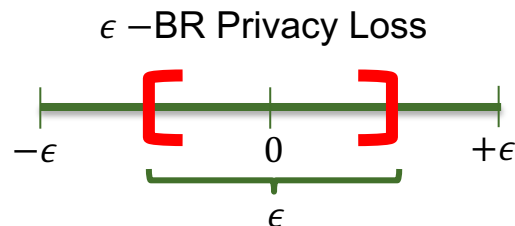
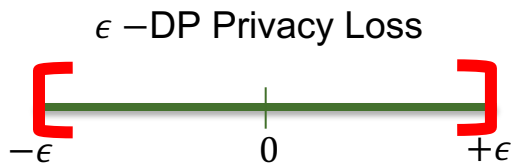
Unknown Gumbel can be analyzed with repeated Exponential Mechanisms



## Bounded Range Mechanisms [DR'19]

- Can we improve general DP composition when we restrict to using Exp Mech only?
  - Don't rely on black box DP composition.
- **Defn:** A mechanism  $M: X \rightarrow Y$  is  $\epsilon$ -**Bounded Range** (BR) if for any neighbors  $x, x' \in X$  and outcomes  $y, y' \in Y$ , we have:

$$\frac{\Pr[M(x)=y]}{\Pr[M(x')=y]} \leq e^\epsilon \frac{\Pr[M(x)=y']}{\Pr[M(x')=y']}$$



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- Note that  $\epsilon$ -BR  $\Rightarrow$   $\epsilon$ -DP and  $\epsilon$ -DP  $\Rightarrow$   $2\epsilon$ -BR.
- **Lemma** [DR'19]: Exp Mech satisfies  $\epsilon$ -BR and composing  $k^*$  of them gives:

$$\left( \approx \epsilon \sqrt{\frac{k^*}{2} \log \frac{1}{\delta}}, \delta \right)\text{-DP}$$

[Cesar, R '21]  
 $\epsilon$ -BR  $\Rightarrow$   $\epsilon^2/8$ -zCDP

# Optimal Comp of Exp Mech [Dong,Durfee,R ICML'20]

## Optimal Differential Privacy Composition for Exponential Mechanisms and the Cost of Adaptivity

Jinshuo Dong<sup>\*1</sup>, David Durfee<sup>2</sup>, and Ryan Rogers<sup>2</sup>

<sup>1</sup>Applied Mathematics and Computational Sciences, University of Pennsylvania

<sup>2</sup>Applied Research, LinkedIn

June 26, 2020

### Abstract

Composition is one of the most important properties of differential privacy (DP), as it allows algorithm designers to build complex private algorithms from DP primitives. We consider precise composition bounds of the overall privacy loss for exponential mechanisms, one of the most fundamental class of mechanisms in DP. We give explicit formulations of the optimal privacy loss for both the adaptive and nonadaptive settings. For the nonadaptive setting in which each mechanism has the same privacy parameter, we give an efficiently computable formulation of the optimal privacy loss. Furthermore, we show that there is a difference in the privacy loss when the exponential mechanism is chosen adaptively versus nonadaptively. To our knowledge, it was previously unknown whether such a gap existed for any DP mechanisms with fixed privacy parameters, and we demonstrate the gap for a widely used class of mechanism in a natural setting. We then improve upon the best previously known upper bounds for adaptive composition of exponential mechanism with efficiently computable formulations and show the improvement.



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# Audience Engagement API

- API Product to provide insights on LinkedIn engagement content and audience data
- Provides information about member data to external marketing partners
- Built on top of **Pinot** for fast, real-time data analytics



# Understanding the Task

- Advertiser can interact adaptively with the API
- Differencing attacks are a concern
- Want to provide both real-time analytics and privacy
- Queries are general top- $k$  queries

# Audience Engagement API

- For more information, see <https://arxiv.org/abs/2002.05839>

## LinkedIn's Audience Engagements API: A Privacy Preserving Data Analytics System at Scale

Ryan Rogers<sup>1</sup>, Subbu Subramaniam<sup>1</sup>, Sean Peng<sup>1</sup>, David Durfee<sup>1</sup>, Seunghyun Lee<sup>1</sup>,  
Santosh Kumar Kancha<sup>1</sup>, Shraddha Sahay<sup>1</sup>, and Parvez Ahammad<sup>1</sup>

<sup>1</sup>LinkedIn Corporation

November 17, 2020

### **Abstract**

We present a privacy system that leverages differential privacy to protect LinkedIn members' data while also providing audience engagement insights to enable marketing analytics related applications. We detail the differentially private algorithms and other privacy safeguards used to provide results that can be used with existing real-time data analytics platforms, specifically with the open sourced Pinot system. Our privacy system provides user-level privacy guarantees. As part of our privacy system, we include a budget management service that enforces a strict differential privacy budget on the returned results to the analyst. This budget management service brings together the latest research in differential privacy into a product to maintain utility given a fixed differential privacy budget.

# Labor Market Insights

- Tracking labor market trends is incredibly important especially during this pandemic.
- Leverage LinkedIn's Economic Graph to show these trends across different regions:
  - What employers are hiring the most?
  - What jobs are most in demand?
  - What are the top skills from these most in demand jobs?
- Global Skilling Event: <https://news.microsoft.com/skills/>

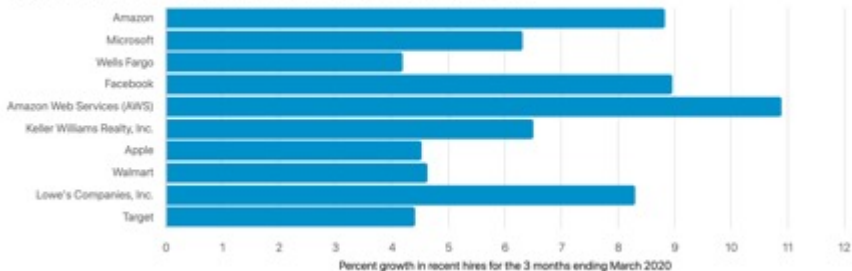


# Labor Market Insights

## Top Trending Employers

March 2020

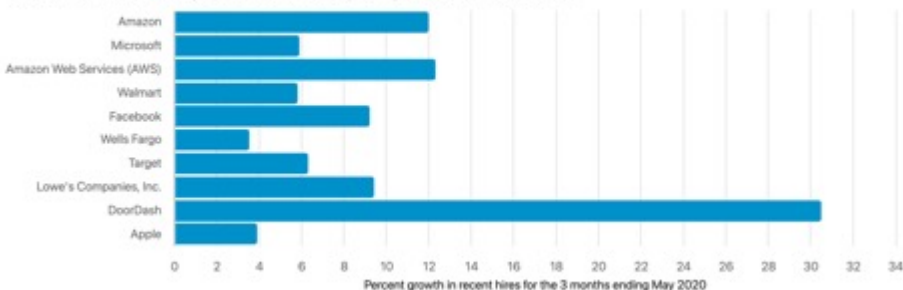
Companies in all industries in all regions, United States ranked by the largest number of hires on LinkedIn.



## Top Trending Employers

May 2020

Companies in all industries in all regions, United States ranked by the largest number of hires on LinkedIn.



## Privacy considerations

In publishing these labor market insights from LinkedIn's Economic Graph, we wanted to provide accurate statistics while ensuring our members' privacy. We applied privacy techniques, such as [differential privacy](#), to aggregate insights from our datasets without learning about specific individuals. Our differentially private [algorithms](#) have been deployed in other LinkedIn products used by our marketing partners, including the [Audience Engagement API](#) in LinkedIn Marketing Solutions.

[graph.linkedin.com/insights/labor-market](https://graph.linkedin.com/insights/labor-market)

# Labor Market Insights

- For more information, see <https://arxiv.org/abs/2010.13981>

## A Members First Approach to Enabling LinkedIn's Labor Market Insights at Scale

Ryan Rogers\*, Adrian Rivera Cardoso\*, Koray Mancuhan, Akash Kaura, Nikhil Gahlawat, Neha Jain, Paul Ko, Parvez Ahammad

LinkedIn Corporation

October 28, 2020

### **Abstract**

We describe the privatization method used in reporting labor market insights from LinkedIn's Economic Graph, including the differentially private algorithms used to protect member's privacy. The reports in <https://graph.linkedin.com/insights/labor-market> show who are the top employers, as well as what are the top jobs and skills in a given country/region and industry. We hope this data will help governments and citizens track labor market trends during the COVID-19 pandemic while also protecting the privacy of our members.

# Career Explorer

- <https://linkedin.github.io/career-explorer/#explore>
- Helps members discover new occupations based on the skills they have
- Helps members understand how the acquisition of new skills can lead to new opportunities.

The screenshot displays the LinkedIn Career Explorer interface. At the top, the LinkedIn logo is followed by 'Economic Graph' and navigation links: 'The future of work', 'Workforce data', 'Resources', 'Blog', 'About', and 'Follow'. Below the navigation bar, there is a 'SELECT YOUR CITY' dropdown menu with 'Atlanta, GA' selected. On the left side, there is an 'ENTER A JOB' input field containing 'Food Server'. To the right of this field is a 'SORT' dropdown menu set to 'Similarity Score (low to high)'. Below the input field, a list of skills for 'Food Server' is shown, including: Food & Beverage, Teamwork, Waiting Tables, Time Management, Communication, Hospitality, Customer Service, Social Media, Organization Skills, Multitasking, Restaurant Management, Public Speaking, Cashiering, Customer Satisfaction, Event Planning, Microsoft Access, and Research. The main content area shows '87 job matches in United States for Food Server. Showing 20 results.' The first match is 'Banquet Captain' with a '50% match' badge. Below the job title, there are three panels: 'Skill Overlap' showing a comparison between 'Food Server' and 'Banquet Captain' with a bar chart and the text '+11 unique skills to each'; 'Skills To Build' listing 'Banquet Operations', 'Hospitality Management', 'Hotel Management', 'Event Management', and 'MICROS'; and 'Popularity' showing a gauge chart with a score of '0.2' and the text 'Transitioning to Banquet Captain from Food Server may be an untapped opportunity'. At the bottom of the job card, there are two buttons: 'Find Jobs on LinkedIn' and 'Find Connections on LinkedIn'.

# Continual Observation

<i>DP Algorithms</i>	$\ell_0$ -Restricted Sensitivity	$\ell_0$ -Unrestricted Sensitivity
Known Domain	Binary Mechanism [Chan, Shi, Song '11 and Dwork, Naor, Pitassi, Rothblum, Yekhanin '10]	Sparse Gumbel [Cardoso, R '21]
Unknown Domain	Unknown Base [Cardoso, R '21]	Meta Algo

# Concluding Remarks

- View privacy as a spectrum, not binary
- Can easily incorporate more privacy into systems that already are DP.
- How to rationalize large privacy loss (e.g. Census)?
  - There needs to be more open source attacks.
- Open Research Questions
  - How large is the gap between optimal adaptive vs non-adaptive composition for exponential mechanisms?
  - What about hardness results for some of these bounds?
  - How much can ordering impact the overall privacy loss?
    - See [Cesar, R'21]

# Thank you!

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