Deep Real-time Volumetric Rendering Using Multi-feature Fusion

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Figure 1: Multi-feature RPNN (MRPNN) renders multi-scattered cloud illumination in real time at 1024 × 1024 resolution, producing results close to the ground truth (a). Thanks to its novel network design, MRPNN supports configurable shading parameters (b), while the prior work only accepts fixed ones. G configures Henyey-Greenstein phase function. In addition, our network correctly handles the shadow boundary (c), which was previously a failure case.

ABSTRACT
We present Multi-feature Radiance-Predicting Neural Networks (MRPNN), a practical framework with a lightweight feature fusion neural network for rendering high-order scattered radiance of participating media in real time. By reformulating the Radiative Transfer Equation (RTE) through theoretical examination, we propose transmittance fields, generated at a low cost, as auxiliary information to help the network better approximate the RTE, drastically reducing the size of the neural network. The light weight network efficiently estimates the difficult-to-solve in-scattering term and allows for configurable shading parameters while improving prediction accuracy. In addition, we propose a frequency-sensitive stencil design in order to handle non-cloud shapes, resulting in accurate shadow boundaries. Results show that our MRPNN is able to synthesize indistinguishable output compared to the ground truth. Most importantly, MRPNN achieves a speedup of two orders of magnitude compared to the state-of-the-art, and is able to render high-quality participating material in real time.

CCS CONCEPTS
• Computing methodologies → Ray tracing; Neural networks.

KEYWORDS
Participating media, volumetric rendering, radiative transfer equation, real time, variable phase function

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1 INTRODUCTION
Participating media exists as a ubiquitous form of material observed widely in the real world, for example, in cloud, milk, jade, skin, and so on. Correctly handling the interaction between these materials and light greatly enhances the realism of rendering results. This subject has been the focus of numerous investigations, in the context of general light transport (e.g., bidirectional path tracing [Lafortune and Willems 1996], Metropolis methods [Pauly et al. 2000]), or specifically tailored to rendering participating media (e.g., photon beams [Jarosz et al. 2008], photon surfaces [Deng et al. 2019] and volumetric path guiding [Herholz et al. 2019]). However, since light could hardly be absorbed before undergoing thousands of bounces in the volume of participating media, especially those of low absorption rates such as clouds, the rendering process takes considerable time to converge to noise-free results. Researchers have been pursuing more effective approaches in recent years. While some of these approaches refer to diffusion theory and/or pre-computation, the line of research starting from Kallweit et al. [2017] introduced the Radiance-Predicting Neural Networks (RPNN). They achieved notable performance improvements and showed how neural networks (NN) can be used to estimate in-scattering irradiance.

Despite their accomplishments, the brute-force architecture of RPNN and its variants limits their performance and robustness. First, because RPNN receives only a few density samples as input and uses a fully connected structure, it is difficult for the network to infer the underlying physical principle of light transport. One clue is that RPNN does not correctly handle shadows (see Fig. 1). In order to map this extremely complicated function, excess neural connections were used, which resulted in bloated network structures and lower performance. Second, the shading parameters in RPNN are hardcoded. Changes in phase values or albedos triggers retraining of the network. The straightforward structure of RPNN merely encodes all scenarios in which different shading parameters push the dimension to an impractical level.

Our motivation is to create a network architecture that better approximates the solution to the RTE. We started by reformulating the RTE through theoretical examination. The investigation reveals that the media could be decomposed into multiple features, rather than being directly fed into the networks. The decomposed features include a set of density fields, pre-integrated phase values, and albedos (see Fig. 10). The decomposition leads to a smarter and fewer-shot network architecture with faster inference and helps achieve configurable parameters. Additionally, we suggest a new sample stencil with two parts, each concentrating on either low frequency (shadow-aware) or high frequency (diffusion-aware) information. The network thus achieves better results in shadow boundaries.

Based on the observations above, we offer Multi-feature Radiance-Predicting Neural Networks (MRPNN), a framework for fusing features extracted from the RTE and predicting the radiance in real time using a lightweight network.

Through experiments, we verify that our method achieves an order of magnitude performance boost over RPNN, configurable shading and better generalization capability in non-cloud shapes, which can never be achieved by previous work. With MRPNN, we are able to generate realistic volumetric rendering in real time.

In particular, our paper makes the following contributions:
- Reformulation of the radiance-predicting problem from an intricate mapping to a simpler one through multi-feature input, allowing us to significantly simplify the neural network structure while enabling dynamically adjustable albedos and phase parameters.
- A lightweight radiance-predicting framework that requires much less computation to achieve a real-time volumetric rendering solution, with better results on non-cloud shapes and the shadow boundary, and better quality compared to RPNN.

2 RELATED WORK
Monte Carlo Integration. Various approaches based on Monte Carlo (MC) integration have been developed to render participating media. Solving the RTE, i.e., finding all potential light paths connecting the light sources, the camera, and the medium vertices, is central to these approaches. For example, bidirectional path tracing [Lafortune and Willems 1996] generates rays from both the light sources and the camera to explore the path space. In order to efficiently find those paths with higher contribution, Pauly et al. [2000] introduced Metropolis Light Transport to media rendering. To reduce the estimation variance and increase light path utilization, the photon-based method was introduced to benefit efficiency [Jarosz et al. 2008], and further improved by Jarosz et al. [2011]. These schemes were unified into one framework to achieve a more robust integrator [Krivánek et al. 2014]. Although these methods are unbiased and they all speed up the rendering process considerably, they are still time consuming and can only be used for offline rendering [Kallweit et al. 2017].

Diffusion Theory. Diffusion estimators, in addition to MC integrators, are another type of RTE solvers for efficiently capturing multi-scattered volumetric illumination [Stam 1995]. The intention of diffusion-based methods is to address the multi-scatter issue of MC integrators. A foretaste, the Flux-Limited Diffusion (FLD) proposed by Koerner et al. [2014] is built based on Classical Diffusion Approximations (CDA) for more accuracy. Diffusion-based approaches [Jensen et al. 2001] address the high-order problem, but they are hampered by other concerns that prevent them from being used in real time. Their computational costs, for example, are polynomially dependent on grid resolution, which is also non-constant. However, with insufficient resolution, the bias would be distinguishable. Furthermore, because they naturally do not support progressive rendering, it is difficult to distribute the computational load across frames.

Learning-based methods. Several works have employed learning-based approaches for rendering tasks. To enhance the efficiency of rendering BSSRDFs, neural networks have been employed to predict the exit point position of an object after internal scattering [Vicini et al. 2019], or to directly estimate the contributions of all possible paths between two specific points in homogeneous media [Leonard et al. 2021]. Mildenhall et al. [2020] utilize neural radiance fields to represent scenes and perform rendering through ray marching. Neural radiance fields are further utilized to accelerate the convergence of path tracing [2021]. These methods offer
We then demonstrate how to decompose the transmittance fields with ray-marching. The task of the network may be streamlined (RTE) [Kajiya and Herzen 1984] by reformulating it as the sum of

\[ L(x, \omega) = L_e(x, \omega) - \mu_t(x)L(x, \omega) + \mu_a(x) \int_\Omega p(\omega, \omega_1)L(x, \omega_1) d\omega_1. \]  

The right-hand side of RTE breaks down into 3 terms:

1. **Self-emission term.** \( L_e \) represents the differential increment of light contributed by the particles, such as chemiluminescence and nuclear luminescence, which are rare in real life. We ignore this term for the sake of simplicity.

2. **Extinction term.** The extinction term is defined by the total amount of light being absorbed or out-scattered, where \( \mu_t = \mu_a + \mu_s \) is the extinction coefficient; \( \mu_a \) and \( \mu_s \) are the absorption and scattering coefficients, respectively.

3. **In-scattering term.** The in-scattering term collects the in-bound light scaled by the phase function \( p \) from the spherical neighbor \( \Omega \).

We use the term albedo (denoted by \( \zeta \)) to refer to the amount of light being re-scattered rather than absorbed when a collision occurs. We assume that the albedo of the medium is constant through the space, i.e. \( \frac{\mu_t(x)}{\mu_a(x)} \equiv \zeta \). Ignoring the emission term, the integral form [Arvo 1993] of Eq. (1) is simplified to:

\[ \frac{d}{d\omega}L(x, \omega) + \mu_a(x) \int_\Omega p(\omega, \omega_1)L(x, \omega_1) d\omega_1 \]  

In the following sections, we will first demonstrate how to extract the multiple features from the Radiance Transport Equation (RTE) [Kajiya and Herzen 1984] by reformulating it as the sum of contributions from paths of different lengths. The results indicate that the extracted features may be useful in network estimation. We then demonstrate how to decompose the transmittance fields (see Sec. 3.2), which is necessary for network compacting. Then, in order to support configurable shading parameters, we extract phase and albedo (see Sec. 3.3). Following that, we propose a new frequency-aware stencil for collecting data from the sample point’s surrounding discrete points while achieving better shadow boundaries (see Sec. 3.4). Finally, we present the lightweight radiance prediction framework (see Sec. 3.5).

**ALGORITHM 1: MRPNN::Render\((x, \omega, l)\)**

\[ L \leftarrow 0 \]

for \( N := 1 \) to TotalSamples do

\( (u, hit) \leftarrow \text{GetSamplePointWithDeltaTracking}(x, \omega) \)

if \( hit \) is true then

\[ s \leftarrow \text{ApplyStencil}(u, \omega, l) \]

\( \text{descriptor} \leftarrow \text{SampleAndGenerateDescriptor}(s) \)

\( L \leftarrow L + \text{PredictRadiance}(\text{descriptor}) + \text{DirectLight}(x, l) \)

else

\( L \leftarrow L + \text{SampleSkyBox}(\omega) \)

end if

end for

return \( L/\text{TotalSamples} \)

### 3.1 RTE

We begin the theoretical investigations of the RTE by reviewing its classic formulation. The RTE depicts the differential change of the radiance \( L \) traveling through a medium at position \( x \) in direction \( \omega \):

\[ \frac{d}{d\omega}L(x, \omega) = L_e(x, \omega) - \mu_t(x)L(x, \omega) + \mu_a(x) \int_\Omega p(\omega, \omega_1)L(x, \omega_1) d\omega_1. \]  

where \( z = \lim_{\varepsilon \to 0} x - t \cdot \omega \), \( L_z \) is the in-coming radiance from \( z \) toward \( \omega \), and the transmittance term \( T \) is:

\[ T(x, y) = e^{-\int_{x}^{y} \mu(u) du}, \]
and the integral part of the in-scattering term $S$ is:

$$S(x, \omega) = \int_{\Omega} p(\omega, \omega) L(x, \omega) d\omega. \quad (4)$$

Here we assume that the lights are distant (e.g., the sun). Other light sources may be effective, but they are out of our scope. Under this condition, the $L_s$ term from Eq. (2) can be written as:

$$L_s(x, \omega) = \delta((l, \omega) + 1) \cdot I,$$ \quad (5)

where $\delta((l, \omega) + 1)$ is the Dirac function asserting that light is only coming from direction $I$, and $I$ is the light intensity. We will also use $T(x, \omega)$ in short of $\lim_{k \to 0} T(x, x + b \cdot \omega)$. Plugging Eq. (2) and Eq. (5) into Eq. (4), we get:

$$S(x, \omega) = \int_{\Omega} \left[ p \left( \int_{x}^{z} T \mu S d\omega \right) + p TL_s \right] d\omega = \zeta \int_{\Omega} p \left( \int_{x}^{z} T \mu S d\omega \right) d\omega + p(\omega, I) T(x, I) \cdot I. \quad (6)$$

Note that the $S$ term appears on the both side of Eq. (6). Following the notation of Veach [1998], we employ an operator $K$ which is defined as $\langle K \mu \rangle(x, \omega) = \int p \int T \mu b(x, \omega) d\omega d\omega$ and a set of in-scattering intensity fields $S_{i, I} \geq 0$ being the order of scattering. The RTE can be reformulated as:

$$S_0 = p(\omega, I) T(x, I) \cdot I, \quad S_i = KS_{i-1},$$

$$S = \sum_{i=0}^{\infty} \zeta^i S_i = S_0 + \zeta S_1 + \zeta^2 S_2 + \zeta^3 S_3 \cdots. \quad (7)$$

Eq. 7 shows that the RTE can be rewritten as an additive series. When given approximated $S_i$ as hints, the network can infer the final result $S$ more easily.

**Splitting the in-scattering field.** To approximate $S_i$, we immediately hit the first problem. Note that for $i > 0$, the operator $K$ involves intricate integration over both position $x$ and direction $\omega$, raising a problem of too many dimensions, which causes difficulties during both training and runtime. To simplify the problem, we’d better separate the directionally invariant part $S'_i$ and the remaining part $P_i$, where $S_i(x, \omega) = P_i(x, \omega) \cdot S'_i(x)$. Note that $P_i$ is impossible to be separated through formulation; its intention is a scale factor that accounts for the phase function (directionally invariant part), which will be later discussed.

**Directionally invariant part.** According to Eq. (7), the phase term $p$ in operator $K$ involves intricate integration over both position $x$ and direction $\omega$, raising a problem of too many dimensions, which causes difficulties during both training and runtime. To simplify the problem, we’d better separate the directionally invariant part $S'_i$ and the remaining part $P_i$, where $S_i(x, \omega) = P_i(x, \omega) \cdot S'_i(x)$. Note that $P_i$ is impossible to be separated through formulation; its intention is a scale factor that accounts for the phase function (directionally invariant part), which will be later discussed.

$$S'_i = T(x, I) \cdot I, \quad S'_i = K'(S'_{i-1}),$$

$$S = \sum_{i=0}^{\infty} \zeta^i P_i S'_i. \quad (8)$$

Eq. (8) reveals the three valuable physically-based features hidden beneath the RTE: the directionally invariant part $S'_i$, phase $P_i$ and albedo $\zeta^i$. It should be noted that $S$ is not a simple combination of the extracted features, but a neural network conditioned on these features that can well approximate $S$. To this end, our next goal is to extract features from the three terms.

3.2 **Transmittance Field**

To approximate the directionally invariant part $S'_i$ in Eq. (8), we propose to generate certain features by applying $T(x, l)$ (defined in Eq. (3)) to density fields. Fig. 2 demonstrates our intuition, integrating the scattering field over a homogeneous volume with a constant density field. In this simple setting, an unbiased estimator produces non-constant radiance. Given that the input is spatially constant, it would be hard for a network to infer the relationship (e.g., RPNN). Considering that light travels farther into the media due to diffusion, which is similar to traveling through a down-scaled density volume, we first increasingly down-scale the constant density field. Then we generate a set of fields by applying $T(x, l)$ to those down-scaled density fields. The scattering field can be easily approximated using a linear combination of the generated fields, indicating that we can leverage $T(x, l)$ and the scaled density fields to approximate $S'_i$. Furthermore, as the diffusion operator $K'$ in Eq. (8) could be approximated by applying $T(x, l)$ to density mipmap [Wrenninge et al. 2011], we propose to use scaled density mipmaps instead of scaled density fields.

Given the above analysis, we apply $T(x, l)$ to scaled density mipmaps, yielding the so-called **transmittance field**:

$$\tilde{S}_i = e^{-\int_{x}^{y} \beta(i+1) \mu(u) du}, \quad (9)$$

where $\mu$ denotes the $i$-th level of mipmaps generated from the density field, which is down-scaled by a hyper-parameter $\beta(i+1)$ ($0 < \beta < 1$). Therefore, we can use our transmittance fields $\tilde{S}_i$ to hint the directionally invariant part $S'_i$. This intuition will be further validated by experiments. By providing transmittance fields, the network better understands the mapping. Since the approximated transmittance fields are being increasingly smoother in the spatial domain, we can use gradually reduced spatial resolution to calculate and store them, yielding the so-called **mipmaps**. More details will be addressed in Sec. 4.1.

3.3 **Phase and Albedo**

The remaining components of Eq. (8) to be addressed are the phase term $P_i$ and albedo term $\zeta^i$.

**Phase.** Ruminant that the goal of the phase feature is to determine a scale factor to assist the network in learning the contribution.
of phase functions. In practice, we adopt \( P_l = P'(v_l - u) \cdot p'(v_l - u, l) \) as the phase feature \(^1\), where \( v_l \) is the \( l \text{th} \) stencil point and \( p'(v_l - u) \) is the cumulative version of phase function (detailed implementation will be given in the supplementary material) over the volume of the point.

**Albedo.** In Eq. (8), those powers of albedo \((\zeta^i)\) will only appear as the weights of the combination of the \( S_i \). We use \( \zeta \) as the feature of the albedo (and the remaining \((\zeta^i, \zeta^2, \ldots)\) are superfluous).

We should mention that by separating the features as in Eq. (8), the phase and albedo are configurable parameters that can be dynamically adjusted in testing.

### 3.4 Frequency-Sensitive Stencil Pattern

Inputting the entire field into the network can lead to difficult optimization and over-parameterization of the network. To solve this problem, we need a stencil pattern sampling to collect information from the sample point’s surrounding discrete points. We design a frequency-sensitive stencil pattern to decompose the distribution of global-local multiple scattering [Zinke et al. 2008]. Our stencil has two parts, one for high-frequency shadow boundary and the other for low-frequency diffusive scattering. We use stratified uniform spherical distributions for the low-frequency part, and use a cone shape towards light direction for the high-frequency part. Compared to a naïve uniform stencil pattern (e.g., the grid-lattice used in RPN), our frequency-sensitive method can better predict non-cloud shaped media and shadow boundaries.

The \( l \text{th} \) layer in the stencil is denoted by \( Q_l = \{q_{l,1}, q_{l,2}, \ldots, q_{l,N_l}\} \), where \( q_{l,j} \) is the \( j \text{th} \) stencil point in the \( l \text{th} \) layer and \( N_l \) is the number of the points in this layer. Our stencil consists of totally \( K = 12 \) layers, which is split into a low-frequency part \( Q_1, \ldots, Q_M \) and a high-frequency part \( Q_{M+1}, \ldots, Q_K \) where \( M = 8 \). Each layer corresponds to a mip-level \( m_l \). The details of each single layer of stencil design will be given in the supplementary material.

### 3.5 Two-Stage Network

Our design motivation is based on the network’s ability for estimating the in-scattering radiance, where the network is a function:

\[
\overline{S}_l(z, \Theta) : \mathbb{R}^d \rightarrow \mathbb{R},
\]

which maps a descriptor \( z \) and a set of parameters \( \Theta \) to an estimated radiance value in the spectral channel \( x \).

To adapt the proposed multi-feature inputs and frequency-sensitive stencil, we separate the entire network into two stages, namely the *feature* and the *albedo* stage (see Fig. 3). \( S'_l \) (transmittance field) and \( P'_l \) (phase) are responsible for estimating \( S_l \) and will be fed into the first stage. \( \zeta^i \) is responsible for combining \( S_l \) of different spectra and will be fed into the second stage. Because the feature stage is albedo-independent, it only needs to be run once in spite of the number of spectral channels, which reduces the computational cost of the network. As we use the RGB color space, the albedo stage will be executed 3 times to compose the final RGB output (i.e., for each of \( \zeta^i, x, \zeta^i, r, g, b \)). Note that thanks to the assistance of RTE-based features, our network is light-weight, contains only \( \sim 50k \) parameters (approximately 83% of LeNet-5’s, 0.2% of ResNet-50’s and 0.03% of VGG-16’s), and has fast inference speed (frame cost \( \leq 33.3 \text{ms} \)). More details can be found in Sec. 4.3.

### 4 IMPLEMENTATION DETAILS

In this section, we will first show how to implement feature extraction (Sec. 4.1). Then, we demonstrate the detailed construction of the network’s inputs (Sec. 4.2). Following that, we present the architecture of our lightweight network (Sec. 4.3). Finally, we display our training details (Sec. 4.4).

#### 4.1 Feature Extraction

**Density mipmaps.** The map layer is generated efficiently by the hardware’s bi-linear interpolation. In our case, the 9 layers of mipmaps begin at the input \( m_0 \) fields with a resolution of 256\(^3\) and end at \( m_0 \) with a resolution of 1\(^3\).

**Transmittance fields.** We employ the ray-marching [Drebin et al. 1988] technique to compute the transmittance fields. For each voxel, we generate several uni-spaced sample points towards the light source depending on the voxel resolution. The above process is executed on each mip-level \( i \) of the density maps, where the density field is scaled by \( \beta^{(i+1)} \) \((0 < \beta < 1)\) during the estimation (which is suggested in Sec. 3.1), and we empirically set \( \beta = 0.578 \).

**Phase function.** We use the Henyey-Greenstein (HG) phase function as the volume-averaged phase function. The HG phase function is dynamically controlled by a hyper-parameter \( G \). In addition to the HG phase function, our framework is capable of rendering other phase functions, e.g., the Lorenz-Mie phase function (see Fig. 9). Detailed implementation will be given in the supplementary material.

#### 4.2 Descriptor

In response to the stencil, the descriptor is constructed utilizing features that describe a point and its illumination context in the volume. The \( l \text{th} \) feature output of stencil \( Q_l \) (or \( q_{l,j} \)) is:

\[
F_{i,j} = \{P_{i,j}^d, P_{i,j}^s, P_{i,j}^p\},
\]

where \( P_{i,j}^d \) and \( P_{i,j}^s \) are the density and the scaled-transmittance samples at the stencil point \( v_{i,j} = u + q_{i,j} \) with the corresponding mip-level \( m_l \), and \( P_{i,j}^p \) is the phase. In practice, we use \( \log \left( P_{i,j}^p + 1 \right) \).
and \( \log \left( \frac{1}{N} + 1 \right) \) to compress the ranges of the values (which is trivial and will be omitted in the rest).

The features in each stencil layer form a single-layer descriptor
\[
\Sigma_i = \{F_{i1}, F_{i2}, \ldots, F_{iN}\},
\]
and finally the descriptor is established through:
\[
z = \{\Sigma_1, \Sigma_2, \ldots, \Sigma_M, \Sigma_{M+1}, \ldots, \Sigma_K, G, \zeta, \gamma\},
\]
where \( G \) is the parameter of the HG phase function, \( \zeta \) is the albedo, \( \alpha \) is a hyper-parameter (detailed in Subsec. 4.4), and \( y = \cos^{-1} (\omega \cdot l) \) is the angle between the view and the light. We assume that the density outside the volume boundary is 0. However, the scaled-transmittance fields should be given special consideration. More information can be found in the supplement file.

4.3 Network Architecture

Feature processing. We have introduced multi-features (density, scaled-transmittance, and phase) as the input to the network. To handle these inputs more efficiently, we employ the Squeeze-and-excitation Module (a.k.a., the SE module [Hu et al. 2018]) for each layer. The ablation tests in Sec. 5.2 show that the SE module produces more stable and better results than other methods (e.g., fully-connected layers).

Feature stage. Its purpose is to compute the latent space vectors for the input feature. We introduce a two-part network in the feature stage to fuse stencils from different frequencies in order to investigate the high- and low-frequency parts separately. It is based on 2 individual sub-networks in connection with the low-frequency part of the descriptor \( \Sigma_1, \ldots, \Sigma_M \) and the high-frequency part \( \Sigma_{M+1}, \ldots, \Sigma_K \). Each layer of descriptor is first passed into the SE module, then is combined with the output of the former block by addition. We feed individual stencil layers progressively to the network with a residual connection.

Albedo stage. In this stage, our goal is to introduce albedo to the network, fuse the low- and high-frequency information and compute the final output. We first use a SE module to scale the input latent vectors from the previous stage. In order to accelerate the inference process, a dimension reduction operate is perform. Finally we use several fully-connected layers with residual connection to compute the output.

We will provide the low-level details of network architecture and hyper-parameter setting in the supplementary material.

4.4 Training

To train our network, we employ a supervised learning scheme. We define the collection of descriptors and labels (ground-truth) by:
\[
\mathcal{D} = \{(z_1, S(u_1, l_1)), \ldots, (z_N, S(u_N, l_N))\},
\]
where \( N \) is the size of the collection. Our goal is to find a \( \Theta \) that minimizes the average loss between predicted and target values:
\[
\Theta^* \in \arg\min_{\Theta} \frac{1}{N} \sum_{i=1}^{N} \mathcal{L} \left( \tilde{S}^a(z_i; \Theta), S(u_i, l_i) \right).
\]
Table 1: Bias and performance test results. Note that the neural network-based approaches are cost-consistent with change of light direction, whereas the reference (MC estimator) fluctuates in time. In the convergence test, we used 64SPP for both RPNN and MRPNN, and adaptive samples depending on the noise for the reference. Note that rendering takes much less time (≤ 0.5ms) than network inference. (See supplementary material for full table)

<table>
<thead>
<tr>
<th>Model</th>
<th>Light Dir.</th>
<th>Bias</th>
<th>Frame Cost (ms)</th>
<th>Convergence Boost</th>
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<tbody>
<tr>
<td></td>
<td></td>
<td>Ours</td>
<td>RPNN</td>
<td>Ours</td>
</tr>
<tr>
<td>Cloud0</td>
<td>Side</td>
<td>1.55e-2</td>
<td>1.85e-2</td>
<td>5.2</td>
</tr>
<tr>
<td></td>
<td>Front</td>
<td>2.21e-2</td>
<td>1.75e-2</td>
<td>4.28e-2</td>
</tr>
<tr>
<td></td>
<td>Back</td>
<td>1.85e-2</td>
<td>2.49</td>
<td>2.18</td>
</tr>
<tr>
<td>Model0</td>
<td>Side</td>
<td>1.80e-2</td>
<td>2.18e-2</td>
<td>5.0</td>
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<tr>
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<td>1.86e-2</td>
<td>2.20e-2</td>
<td>6.83e-2</td>
</tr>
<tr>
<td></td>
<td>Back</td>
<td>2.08e-2</td>
<td>89.4×</td>
<td>628.1×</td>
</tr>
</tbody>
</table>

Table 2: Parameter scale and feature comparisons. Supported features are marked ✓ and unsupported X. Note that the LUTs column refers to whether a variant uses the volume-averaged phase function.

<table>
<thead>
<tr>
<th>Model</th>
<th>Parameters</th>
<th>µ</th>
<th>S</th>
<th>P</th>
<th>LUTs</th>
<th>High Freq.</th>
<th>SE-Module</th>
</tr>
</thead>
<tbody>
<tr>
<td>MRPNN (Ours)</td>
<td>49.7 k</td>
<td>✓</td>
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<tr>
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<td>MRPNN-Var4</td>
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<tr>
<td>RPNN</td>
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<tr>
<td>RPNN-Var1</td>
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<td>✓</td>
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</table>

Objective 2: real-time performance. In the last four columns of Tab. 1, we tested MRPNN’s performance against RPNN and the reference. Each frame’s cost is made up of the network’s inference time and the rendering time. It’s worth noting that rendering time for MRPNN and RPNN is nearly identical, which is significantly less (frame cost ≤ 0.5ms) than inference time. Our MRPNN was able to render in real time (frame cost ≤ 33.3ms), and is order(s) of magnitude faster than both RPNN and the reference, which is to be expected given the network’s compact design.

In addition, Tab. 2 compares the parameter scale for MRPNN and RPNN. The variations of both approaches differ in the descriptors and structure, which will be used in later ablation tests. The parameter scale of MRPNN is only approximately 3.8% of RPNN’s, which explains the faster inference speed.

Objective 3: generalization ability in varying shading parameters. With an initial intent to generalize the shading parameters which were previously hardcoded into the network in RPNN, we tested our framework under various phase parameters G and albedos as listed in Tab. 3. Note that RPNN does not handle non-uniform (G ≠ {1.0, 1.0, 1.0}) albedos or varying G and is marked “n/a”.

Table 3: Check experiment of the biases with different shading parameters.

<table>
<thead>
<tr>
<th>Model</th>
<th>Parameter</th>
<th>Side</th>
<th>Front</th>
<th>Back</th>
<th>Correspondent</th>
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<tbody>
<tr>
<td>RPNN</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>RPNN-Var1</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>RPNN-Var2</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>RPNN-Var3</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
</tbody>
</table>

Objective 4: ability of generalization in non-cloud objects. In the second row of Tab. 1, we test an artist-created model, which is a non-cloud object with regular boundaries. By comparing the RMSE biases with that of the reference, we can see that in the majority of cases MRPNN quality is better than that of RPNN. Also we achieve the same level of bias as clouds for rendering non-cloud objects. It can therefore be said that MRPNN outperforms RPNN in the generalized rendering of non-cloud objects.

Faster convergence. We tested MRPNN and RPNN’s training convergence based on the same number of nodes (200 as the original RPNN), AdaBCE optimizer, initial learning rate and weight decay, data configuration, training set size, and validation sets with the split ratio of 4:1:1. Fig. 5 shows the results, where our MRPNN achieves apparently better convergence. This profits from the parameter scale of our network: RPNN uses approximately 1.3 million trainable parameters due to the density-only design, while MRPNN contains only about 50,000 trainable parameters. Consequently, MRPNN learns faster while converging with less error.

5.1 Examining the SE Modules

In Sec. 4.3 we propose to use SE modules to help the network fuse the feature channels. To support this, we implement two other networks. MRPNN-Narrow is achieved by removing the SE Module in MRPNN, and MRPNN-Wide is achieved by replacing the SE Module in MRPNN with fully-connected layers, detailed architectures are listed in the appendix.

As shown in Fig. 5, MRPNN-Narrow has no evident quality or speed change in runtime, but its convergence is slower than MRPNN. In MRPNN-Wide, features are fused at each layer by brute force using large matrices, causing a 2 ~ 3 times slower runtime performance. Also, due to considerably increased trainable weights, the training convergence is slower. Given the above, the SE module can better fuse the inputting features.

5.2 Ablation Tests

In addition to the wide and narrow variants, we implemented several more variants, each of which disables some features while ensuring the same number of parameters (as detailed in Tab. 2). Fig. 6 presents the results.
Volume-averaged phase functions (LUTs for short). MRPPN-Var1 with non-volume-averaged phase converges slightly slower, indicating that LUTs provide the network with more precise context.

Transmittance fields. We removed the transmittance fields in MRPPN-Var2 and MRPPN-Var4. Note that both variants are considerably harder to converge, which again supports our proposal to introduce the transmittance fields.

Split stencil. We removed the high-frequency part of the stencil in MRPPN-Var5. As expected again, the convergence rate decreases. The high-frequency part not only addresses the shadow boundary, but also speeds up the training.

Modified RPN. In addition to our network, we integrate the features into the RPN to validate their effectiveness. We implement (approximately) the same number of trainable parameters. Based on the results, we can conclude that our proposals are even effective in the original RPN architecture. This again supports our claims.

6 DISCUSSION AND FUTURE WORK

In this paper, we offer a novel framework to render high-fidelity participating media in real-time, which is near 2 orders of magnitude faster than the state-of-the-art thanks to the compact network architecture and fewer required samples. Also, our stencil design addresses the shadow boundary. Furthermore, our framework is able to generalize different shading parameters by concatenating new features, as suggested by our investigation into the RTE.

Our approach has limitations. First, the use of mipmaps may cause issues in highly fragmented portions of the volume, resulting in more biased brightness (see Fig. 7). Introducing new auxiliary features, such as the variance of downscaled densities, may aid in addressing this issue. Second, because the scaled transmittance fields in our case are directionally consistent, stochastic progressive sampling and denoisers are disabled (if any) (see Fig. 8). Designing new ambient-oriented features, such as spherical harmonics encoded with lighting information [Kaplanyan and Dachsbacher 2010], could be a solution. Finally, we assumed that the albedos and phase parameters are homogeneous over the entire volume, which could not fulfill all potential types of materials. A more in-depth examination of the RTE and a better design of the descriptor may alleviate this issue.

ACKNOWLEDGMENTS

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Jinkai Hu, Chengzhong Yu, Hongli Liu, Lingqi Yan, Yiqian Wu, and Xiaogang Jin.


Figure 4: Render configurations and comparisons. All scenes are rendered with $\zeta = RGB(1.0, 1.0, 1.0)$, $G = 0.857$ (except $\zeta = RGB(0.8, 0.9, 1.0)$ in CLOUD2 and $G = 0.5$ in MODEL1).

Figure 5: Convergence of validation errors (log-transformed).

Figure 6: Validation errors of the ablation tests.
Figure 7: Because of mipmapping, the network assumes fragmented volumes to be continuous lower-density volumes, resulting in imprecise overall illuminance.

Figure 8: MRPNN produces random overall biases before convergence in ambient lighting, which can’t be addressed by denoisers.

<table>
<thead>
<tr>
<th>Cloud 5</th>
<th>Cloud 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ground Truth</td>
<td>Ground Truth</td>
</tr>
<tr>
<td>Isotropic</td>
<td>HG($g = 0.857$)</td>
</tr>
<tr>
<td>MRPNN(Ours)</td>
<td>MRPNN(Ours)</td>
</tr>
</tbody>
</table>

Figure 9: MRPNN renders with configurable phase functions on the fly, avoiding the need to retrain the network. The results show promising compatibility of MRPNN in phase functions. CLM is an abbreviation for Chopped Lorenz-Mie.

Figure 10: Framework overview. The system takes a density field, phase function, and albedo as inputs. Then, in pre-processing, we recursively down sample the density field and generate the corresponding transmittance fields. The volume-averaged phase function’s LUT is also generated in this phase. Finally, in runtime, we sample the density and transmittance fields and the phase with the stencil, and the assembled descriptor is then passed to MRPNN network for estimation.