Neural BRDFs: Representation and Operations

JIAHUI FAN, School of Computer Science and Engineering, Nanjing University of Science and Technology, China
BEIBEI WANG†, School of Computer Science and Engineering, Nanjing University of Science and Technology, China
MILOŠ HAŠAN, Adobe Research, USA
JIAN YANG†, School of Computer Science and Engineering, Nanjing University of Science and Technology, China
LING-QI YAN, University of California, Santa Barbara, USA

Fig. 1. We present a neural representation for BRDFs; the latent vectors of this representation support several operations including layering. Our method is able to produce closely matching layered results to the Monte Carlo simulation of Guo et al. [2018] with less cost, and works well with spatially-varying parameters (here we show varying top layer roughness, IOR, bottom layer Fresnel value, macro surface normal and scattering medium properties).

Bidirectional reflectance distribution functions (BRDFs) are pervasively used in computer graphics to produce realistic physically-based appearance. In recent years, several works explored using neural networks to represent BRDFs, taking advantage of neural networks’ high compression rate and their ability to fit highly complex functions. However, once represented, the BRDFs will be fixed and therefore lack flexibility to take part in follow-up operations. In this paper, we present a form of “Neural BRDF algebra”, and focus on both representation and operations of BRDFs at the same time. We propose a representation neural network to compress BRDFs into latent vectors, which is able to represent BRDFs accurately. We further propose several operations that can be applied solely in the latent space, such as layering and interpolation. Spatial variation is straightforward to achieve by using textures of latent vectors. Furthermore, our representation can be efficiently evaluated and sampled, providing a competitive solution to more expensive Monte Carlo layering approaches.

CCS Concepts: • Computing methodologies → Reflectance modeling; Ray tracing; Appearance and texture representations.

Additional Key Words and Phrases: BRDF, Neural representation, Layering

1 INTRODUCTION

Spatially-varying bidirectional reflectance distribution functions (SVBRDFs) are pervasively used in computer graphics to produce vivid and realistic appearance. However, no single BRDF model has succeeded in satisfying all requirements in different scenarios. Analytic models, such as microfacet BRDFs with Beckmann and GGX normal distributions, have computational efficiency but can produce less realistic appearances, due to the discrepancy between the microfacet assumptions and the real-world light-matter interactions. On the other hand, measured SVBRDFs and bidirectional texture functions (BTFs) can faithfully recover the real-world appearance, but have expensive storage and lack flexibility; that is, once measured, these BRDFs are generally fixed. Layering simple analytic models into more complex composites is an attractive alternative explored in recent years, though the rendering solutions for layered materials can be mathematically complex and/or computationally expensive.

In recent years, neural networks for representing SVBRDFs and BTFs has received attention [Kuznetsov et al. 2021; Rainer et al. 2020, 2019; Takikawa et al. 2021]. These neural approaches mostly focus on efficient compression [Rainer et al. 2020, 2019; Takikawa et al. 2021] and query [Kuznetsov et al. 2021]. They have greatly reduced the storage overhead, successfully making high-dimensional SVBRDF and BTF data practically usable in rendering. However, these methods are primarily different ways of representing and compressing measured BRDFs; in our opinion, more operations need
to be supported on the compressed representation to make it truly useful in practice.

Which operations are the most desirable? In a modern rendering framework with multiple importance sampling (MIS), any BRDF must support not only evaluation, answering a point query for a given position and view/light directions, but also importance sampling, distributing outgoing direction samples according to the 2D slice of a BRDF given the incoming direction. Further, BRDFs are often mixed/interpolated to generate a new appearance, texture mapped to specify properties per spatial location, and layered to introduce coatings and other effects.

Our approach is to first compress BRDFs into short latent vectors. Inspired by recent neural approaches that operate on the latent space for geometry compression [Granskog et al. 2021], we train additional networks that operate solely in the latent space, providing individual operations to BRDFs, such as layering. From the outside, these neural networks hide the actual implementation of such operations as if they are the generic operators and our compressed BRDF are operands, leading to a form of “Neural BRDF algebra”.

To achieve spatial variation, we simply use a multi-channel texture (with each texel holding a latent vector) to define SVBRDFs. This SVBRDF map can be efficiently rendered, or combined with other BRDF maps for interpolation and layering to create new SVBRDFs. We show several examples of this black-box style use of our neural operators, as well as demonstrate faster performance compared to previous Monte Carlo techniques.

2 RELATED WORK

Traditional SVBRDF/BTF compression. Due to the high dimensionality of BTFs [Dana et al. 1999], traditional approaches compress BTF, using principal component analysis (PCA) [Weinmann et al. 2014a], linear matrix factorization techniques [Kim et al. 2018; Koudelka et al. 2003; Sattler et al. 2003] or hierarchical tensor decomposition methods [Ruiters and Klein 2009; Wang et al. 2005]. None of these compressing approaches are able to compress a large group of BTFs and lack the ability to operate on the compressed data.

Neural SVBRDF/BTF compression. Kuznetsov et al. [2021] introduce a neural method for representing and rendering a variety of material appearances at different scales. In their method, one neural network is trained per material. More recently, Sztrajman et al. [2021] represent each BRDF with a decoder structure, resulting in better quality, at the cost of more storage for each BRDF. We categorize the aforementioned approaches as specialized methods, because one neural network only represents one material/BRDF in these works. The specialized methods are usually of high quality, but their representation is usually costly to store, and is especially difficult for operations, since the operations will have to take neural networks as inputs and outputs.

The other kind of approaches are generalized methods. Rainer et al. [2019] proposed a neural representation for BTFs, where each per-texel BRDF is represented with a latent vector, resulting in a compact representation of the BTFs. Strictly speaking, this approach is still not fully generalized, since it requires training an autoencoder architecture per BTF and does not generalize across materials. Later, Rainer et al. [2020] extended the work and introduced a unified model to represent all the materials. The generalized methods are more friendly to operations, thanks to the fixed pipeline that converts general BRDFs into the latent space. But as a trade-off, they are often of lower quality. Specifically, neither Rainer et al. [2019] nor Rainer et al. [2020] work well for highly specular materials. Compared to these two works, our method also represents the BRDFs with latent vectors, but our method provides better quality, especially for highly specular BRDFs, thanks to the design of our representation network.

Being a generalized method, our method achieves comparable representation quality as compared to specialized methods, such as Sztrajman et al. [2021], but it requires much less storage, making it more suitable for SVBRDFs’ representation. More importantly, our method not only represents BRDFs with latent vectors, but also supports a rich set of operations on the latent vectors.

Other related neural approaches. Beside BRDF representation, neural networks have also been used for other rendering applications (e.g., glints computation, multiple scattering representation in participating media, etc.) Kuznetsov et al. [2019] propose a generative adversarial model for generalized normal distribution function (GNDF) representation, which avoids the run-time glints computation and texture synthesis. However, the model has to be trained for different groups of normal maps / height fields. Ge et al. [2021] represent the multiple scattering for the entire homogeneous participating media space with a neural network. Zhu et al. [2021] compress a complex luminarie’s light field into an implicit neural representation, which enables efficient BRDF evaluation, importance sampling and probability density function (pdf) computation.

Recently, Mildenhall et al. [2020] learn a radiance field representation (NeRF) via differentiable volume rendering, which inspired many follow-up works. These methods are focused on object capture and do not generally consider materials as separate components, with a few exceptions, e.g., Bi et al. [2020]. Recent neural approaches also propose to operate on the latent space for geometry transformations [Granskog et al. 2021]; our method takes a similar approach to materials.

More applications of neural networks in rendering focus on specific sub-problems in other parts of the material modeling and/or light transport processes. They include function mapping [Yan et al. 2017] which maps fur parameters to participating media, path guiding [Müller et al. 2019] by learning a radiance distribution and learning screen space special effects for buffers [Nalbach et al. 2017] and neural texture [Thies et al. 2019] for deferred rendering.

BRDF layering operations. Layering is an important operation for BRDFs, which has been addressed by several lines of work, including approximate analytic models [Weidlich and Wilkie 2007], Fourier basis functions [Jakob 2015; Jakob et al. 2014; Zeitner and Jakob 2018], Monte Carlo simulation based approaches ([Guo et al. 2018], [Gamboa et al. 2020], and [Xia et al. 2020]) and tracking directional statistics ([Belcour 2018], [Yamaguchi et al. 2019], and [Weier and Belcour 2020]). The Fourier-based methods rely on expensive computation per parameter setting, requiring many coefficients especially for low-roughness surfaces, which makes it difficult to handle spatially-varying textures. The Monte Carlo based methods are able
to produce high-quality results, and support spatially-varying textures, thus we treat them as ground-truth. However, the required random walks lead to extra variance (noise) added to the rendered results. The third group of works expresses the directional statistics (e.g., mean and variance) of a layered BRDF and track the statistical summary at each step, resulting in high performance, even achieving real-time frame rates. However, summary statistics are a fundamentally approximate way of representing the underlying functions.

Compared to all of these works, our method represents the BRDF with a latent vector, and performs the operations on the latent vectors. While supporting other rendering-related operations, such as importance sampling, we specifically treat the layering operation as a complex and challenging task, demonstrating the ability of our black-box operand-operator style approach. Since we use Monte Carlo based approaches as the ground-truth for training, our layering results are very close to Monte Carlo based approaches, while our method av

3 NEURAL BRDFS AND OPERATIONS

In this section, we present our solution to neural BRDF representation and corresponding operations. We first formulate the problem (Sec. 3.1). Then, we analyze the requirements of our Neural BRDF representation, leading to our general-purpose BRDF decoder structure (Sec. 3.2). Finally, we introduce individual neural networks for different neural operations.

3.1 Overview and formulation

We focus on representing individual BRDFs and providing neural operations on them. This is key to our design offering flexibility, and it differentiates our method against previous work that compresses the entire chuck of SVBRDFs/BTFs [Rainer et al. 2019].

A BRDF is a 4D function \( f(\omega_i, \omega_o) \), where \( \omega_i \) and \( \omega_o \) are the incoming and outgoing directions on the unit hemisphere. Note that this definition can be extended to bidirectional scattering distribution functions (BSDFs) by considering full unit spheres for directions. For simplicity, we do not represent BSDFs in this paper. However, we do implicitly consider BSDFs when layering one BRDF atop another: the top BRDF is assumed to transmit all energy that is not reflected, and this affects the layering operation.

We will start from compressing any BRDF in a compact neural form:

\[
\begin{align*}
\text{Representation:} & \quad f(\omega_i, \omega_o) \xrightarrow{N_{\text{rep}}} V_f, \\
\text{Evaluation:} & \quad \{V_f, \omega_i, \omega_o\} \xrightarrow{N_{\text{eval}}} f(\omega_i, \omega_o), \\
\text{Interpolation (blending):} & \quad \{V_f, w_i\} \xrightarrow{N_{\text{interp}}} \sum_i w_i V_{f_i}, \\
\text{Importance sampling:} & \quad \{V_f, \omega_i\} \xrightarrow{N_{\text{sample}}} \omega_o \sim f(\omega_i, \cdot), \\
\text{Layering:} & \quad \{V_{\text{top}}, V_{\text{bottom}}, A, \sigma_T\} \xrightarrow{N_{\text{layering}}} V_{\text{layered}}.
\end{align*}
\]

Above, \( w_i \) represents the weights for the \( i \)-th latent vector, and \( V_{\text{top}} \) and \( V_{\text{bottom}} \) represent the latent vectors for BRDFs at the top layer and the bottom layer respectively. \( A \) and \( \sigma_T \) are the single-scattering albedo and extinction coefficients for the participating medium inserted between the two layers.

These operations cater to the way BRDFs are used in rendering applications. For example, BRDF evaluation comes in the form of point queries, requesting one BRDF value given a pair of incoming and outgoing directions \( \omega_i \) and \( \omega_o \) on a given shading point. Importance sampling requires us to find an efficient (but not necessarily exact) way of sampling an outgoing direction according to the shape of the 2D outgoing BRDF slice given the incoming direction.

Also note that different operations may have different computational cost. The interpolation operation \( N_{\text{interp}} \) is a simple linear blend in latent space and does not require a neural network, while the layering operation \( N_{\text{layering}} \) can be complex.

3.2 Neural BRDF representation and evaluation

We would like to find a general-purpose neural network that is able to compress any input BRDF \( f(\omega_i, \omega_o) \) into a latent vector \( V_f \). We do not want to pre-specify the discretization of the input BRDF. Instead, we opt to define an evaluation network architecture, which takes a latent vector as well as incoming and outgoing directions as input, and returns the corresponding BRDF value. To project a BRDF into the latent space, we simply optimize for a latent vector that gives back the input BRDF at any desired discretization.

We design the architecture of our Neural BRDF evaluation network as shown in Figure 2. It takes a latent vector and an incoming-outgoing pair as query, and outputs the corresponding BRDF value.
we assume that all BRDFs are isotropic for now, mainly for the
we freeze the network parameters and only back-propagate to the
would like to use it to project any new BRDF into the latent space,
when we train the network, we back-propagate the gradients
through routes (1) and (2). When we need the representation of any new
material, we freeze the network’s parameters and use only the back propagate
route (2) to optimize the latent vectors.

The network is trained by back-propagation on a dataset of BRDFs, as
detailed later.

Note that we have two back-propagation routes, one for the latent
vector, the other for the weights of the evaluation network. When
we are training the network, we use all values of BRDFs across the
dataset, and we back-propagate the gradient through both routes,
updating the weights in the network and the latent vectors
simultaneously. In this way, our network learns to use different latent
vectors to represent different BRDFs. Meanwhile, all latent vectors
are interpreted the same way through the evaluation network. On
the other hand, once we have trained the evaluation network and
would like to use it to project any new BRDF into the latent space,
we freeze the network parameters and only back-propagate to the
latent vector. For BRDFs with different roughness, this projection
takes from less than 10 seconds to 45 seconds to converge on an
RTX 2080Ti GPU.

Figure 3 illustrates the detailed architecture of our evaluation
network. Our network is a multi-layer perceptron (MLP), with each
fully connected (FC) layer followed by a layer normalization (LN)
and ReLU activation (except the output layer). We use a bottleneck
residual structure as our basic module in our network, which has
one hidden layer with a half amount of units and residual from the
first layer to the last. We alternatively use the residual blocks and
simple FC+LN+ReLU layers to build our network, and add several
skip connections. This kind of combination is repeated for eight
times in total. The basic number of hidden units is set to 256. The
dimension of the latent vector is set to be 32. We treat every channel
of the RGB color space separately, and we do not clamp any large
high dynamic range (HDR) values.

With our evaluation network, any BRDF can be compressed into
a latent vector. We do not require the BRDFs to be parametric or
measured, nor do we care whether they are already layered or
not. We do however make two assumptions for simplicity. First,
we assume that all BRDFs are isotropic for now, mainly for the
efficiency of the training dataset. Second, we assume that none of
the BRDFs are normal mapped, because this operation is easier to
achieve by altering local shading coordinates during rendering.

Our evaluation network can successfully represent BRDFs from
commonly seen materials. We plot and render with some latent
vectors in Figure 10 using our evaluation operator introducing soon.
In addition to representing a single BRDF, we are able to define a
latent texture, where each texel is a latent vector representing a BRDF.
In this way, we can use this latent texture to describe SVBRDFs, as
will be demonstrated on more examples in Sec. 5.

Discussion. In Table 1, we compare our method against other
three related works, regarding the representation accuracy for specularity,
ability for representing SVBRDFs, and the generality of the model. Regarding representation accuracy, both Sztrajman et
al. [2021] and our method are able to handle sharp specular BRDFs,
while Rainer et al. [2019] and Rainer et al. [2020] are less accurate.
However, Sztrajman et al. [2021] require a decoder for each BRDF
representation, which makes it not applicable for SVBRDF representa-
tion. Regarding the generality, Sztrajman et al. [2021] require
training for each BRDF, and Rainer et al. [2019] require training for
each single SVBRDF.

3.3 Neural BRDF interpolation and mipmapping
By interpolating two or more given BRDFs, a new BRDF can be
obtained, showing a natural transition effect between the input ma-
terials. We interpolate the BRDFs by performing the interpolation of
the latent vectors of two input BRDFs. Figure 4 shows a visualization
of our interpolation, compared to naive linear interpolation of the
BRDF values themselves.

As mentioned earlier, SVBRDFs are represented as latent textures,
where each texel specifies a latent vector. When querying the latent
texture, we perform bilinear interpolation on the latent vectors.
Furthermore, we support building a mipmap for the latent texture,
where texels from higher levels are computed by averaging the latent
vectors of four texels from the previous level. During rendering,
we compute the pixel’s footprint for each shading point, and then
query the mipmapped latent texture with trilinear interpolation,
using the footprint size to find a proper level in the mipmap. Figure
5 shows the results of this interpolation are as expected.

3.4 Neural BRDF importance sampling
Importance sampling is a critical operation for including a BRDF
in a practical path tracing system. Specifically, for a given incom-
ing direction, we want to choose an outgoing direction with a pdf
roughly proportional to the outgoing BRDF lobe as a function on the
hemisphere; we also need to be able to evaluate the sampling
df for a given direction. To introduce a sampling operation for
Neural BRDFs represented in our latent space, our approach is to

Table 1. Comparison of different BRDF representation methods, considering
the ability for representing specularity, SVBRDFs and the generality of the model. The generality means the ability to represent all the materials with
a single network.

<table>
<thead>
<tr>
<th>Method</th>
<th>Specularity</th>
<th>SVBRDFs</th>
<th>Generality</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rainer et al. [2019]</td>
<td>✗</td>
<td>✓</td>
<td>✗</td>
</tr>
<tr>
<td>Rainer et al. [2020]</td>
<td>✗</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>Sztrajman et al. [2021]</td>
<td>✓</td>
<td>✗</td>
<td>✓</td>
</tr>
<tr>
<td>Ours</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
</tbody>
</table>
Neural BRDFs: Representation and Operations

Fig. 3. The structure details of the evaluation network. The purple connection denotes an FC+LN+ReLU combination, while the green one is FC only. The yellow module refers to the residual block. The dark gray arrows mean addition skip connections between layers. All residuals and skip connections are added before the normalization and activation layers. The dimensions of the feature vectors are marked as black numbers in the figure. The detailed structure of a residual block will be illustrated in Figure 8.

Fig. 4. Comparison between our latent space interpolation and linear interpolation (blending/mixture of BRDFs). Our method produces a more natural transition from low roughness to medium roughness then high roughness. But the mixture of BRDFs always keeps two lobes and the highlight remains sharp, which is unnatural.

Fig. 5. Using our method without and with latent texture mipmapping, both rendered at 1 spp. Theipmap is generated from the multi-channel latent BRDF texture as a precomputation, and is queried on the fly in the standard way, using the appropriate level with trilinear interpolation. Theipmap reduces aliasing even with very low sampling rates.

Fig. 6. Comparison between three sampling strategies. Left: sampling the outgoing Lambertian lobe. Middle: sampling according to the GGX lobe with parameters obtained from the top layer. Right: our method, sampling two lobes predicted by our sampling network. All results are produced using BRDF sampling only, with 256 spp. Our method has the least variance.

Fig. 7. Our method can be naturally applied in the MIS framework. We compare between light sampling only, BRDF sampling only and MIS under two different lighting configurations (large light sources vs. a small light source). In both cases, MIS produces the best results, as expected.

Our pdf proxy is defined as

\[
\text{pdf}(\omega_i, \omega_o) = (1 - w)G_\sigma(h_x, h_y) + wL(\omega_o) \tag{6}
\]

where \( (h_x, h_y) \) represents the projected half vector (its z-component is dropped), and \( G_\sigma \) is a Gaussian function with standard deviation \( \sigma \), normalized on the projected hemisphere. \( L \) is the Lambertian pdf on the outgoing hemisphere (i.e., \( \cos \theta_e/\pi \)), where \( \theta_e \) is the angle between the outgoing direction \( \omega_o \) and the macro surface normal.

use an analytic proxy distribution to mimic the actual BRDF lobe. We currently use a weighted sum of a Gaussian lobe and a Lambertian lobe; this approach could be easily extended to include multiple Gaussian lobes if needed.
Fig. 8. The structure of layering network. $A$ and $\sigma_T$ are scalars that represent the albedo and the extinction coefficients. $V_{\text{top}}$ and $V_{\text{bottom}}$ are the latent vectors to represent the top layer and the bottom layer respectively. The rest of notations are the same as Figure 3.

To obtain the parameters, $\sigma$ for the Gaussian function and $w$ for the weight, we propose a sampling network to learn these parameters. To do this, we define the concept of a generalized normal distribution function (GNDF) of the BRDF. The name is chosen because for a microfacet BRDF, its GNDF has a similar (though not identical) shape to its NDF. The GNDF is the normalized average of the BRDF, in half-angle space, over all incoming directions $\omega_i$; it is thus a 2D function of the half-vector. In practice, we estimate the GNDF by uniformly sampling $40 \times 40$ incoming vectors on the upper hemisphere and averaging the resulting 2D BRDF lobes over half-angle space.

We train the importance sampling network by minimizing the difference between our pdf proxy (Equation 6) and the GNDF, in the following sense. Our sampling network is a simple four-layer MLP (with 128, 512, 128 and 32 hidden units individually). It takes any BRDF latent vector and an incoming direction as input, and outputs the sampling parameters $\sigma$ and $w$ of this BRDF. For each latent vector, we generate $40 \times 40$ different incoming directions, then we take the averaged parameters and the averaged pdf $(\sigma_i, \sigma_o)$ predicted by the network from these individual incoming directions. Finally, we match the pdf and the GNDF using a loss to update our network weights.

When we sample a BRDF according to our proxy Equation 6, we firstly generate a random number to choose between the Lambertian and the Gaussian components, with the probability of diffuse ratio $w$. Then we importance-sample the chosen component to obtain the outgoing direction $\omega_o$ (in case of the Gaussian lobe, this is done by first sampling the half vector $h$ and transforming it into outgoing direction). We finally calculate the pdf value for the chosen outgoing direction; this uses the Jacobian term of the half-angle transform, as detailed by Walter et al. [2007]. We validate the results of our sampling methods in Figures 6 and 7.

Note that by definition, our pdf proxy only depends on $\sigma$ and $w$. Hence, even though the importance sampling takes an incoming direction as input, the pdf proxy parameters are independent of it, and can be computed only once using our sampling network for a given BRDF before rendering. Therefore, our importance sampling is very fast, because no network inference is be performed on the fly.

3.5 Neural BRDF layering

Layering BRDFs (Figure 9) includes complex light transport interactions among the layers. The most accurate way to layer BRDFs is using a Monte Carlo random walk [Guo et al. 2018]; however, this is expensive, especially when there are dense volumetric media between the interfaces; the random walk also introduces variance.

We instead propose to learn the layering operation in the latent space. We only consider a two-layer operation, consisting of a top layer with a rough dielectric BSDF (whose transmission component is implied as the energy complement of the top BRDF, with no energy lost in the interface itself) and a bottom layer with any BRDF, and a layer of homogeneous participating media with albedo $A$ and extinction coefficient $\sigma_T$ (assuming isotropic scattering) between the interfaces, and we do not use the extra multiple scattering component that compensates for energy loss in advanced micro-facet models. Note that this two-layer setup can be easily extended into a multi-layered configuration by recursively applying it, as we discuss in Sec. 5.1.

Thanks to the generality of our BRDF latent space, the layered BRDF can also be represented with the latent vector. Thus, the goal of layering is getting a latent vector which represents the layered BRDF, from the input configurations. We propose a layering network to find the mapping between the input component BRDFs and the layered BRDF, as shown in Figure 8. The network has a similar structure with the evaluation network, with fewer layers (stack for only four times) but more hidden units each layer (512 basically).
We generate 300 rough conductor BRDFs and 300 rough dielectric BRDFs. We use the Mitsuba Renderer [Jakob 2010] to generate the training dataset consisting of three types: rough conductor, rough dielectric, and layered BRDFs [Guo et al. 2018]. The dataset could be enriched with other types of BRDFs as needed for the application. All BRDFs have a single channel; RGB color is achieved by independently processing each channel with varying parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Sampling Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roughness for rough conductor/dielectric BRDFs</td>
<td>$\alpha = U(0.216, 1)^3$</td>
</tr>
<tr>
<td>IOR for rough dielectric BSDFs</td>
<td>$\eta = U(1.05, 2)$</td>
</tr>
<tr>
<td>Fresnel for rough conductor BRDFs</td>
<td>$R_0 = U(0, 1)$</td>
</tr>
<tr>
<td>Albedo for layered BRDFs</td>
<td>$A = 1 - U(0, 1)^2$</td>
</tr>
<tr>
<td>Extinction coefficient for layered BRDFs</td>
<td>$\sigma_T = V((0, 1, 2, 5))$</td>
</tr>
</tbody>
</table>

The layering network takes two latent vectors which represents the top layer and bottom layer as input, together with the albedo and extinction coefficients. It directly outputs one target latent vector to represent the layered BRDF. Similar to the evaluation network, our layering network also deals with RGB channels independently.

4 IMPLEMENTATION DETAILS

4.1 Dataset

We use the Mitsuba Renderer [Jakob 2010] to generate the training dataset of BRDFs, consisting of three types: rough conductor, rough dielectric, and layered BRDFs [Guo et al. 2018]. The dataset could be enriched with other types of BRDFs as needed for the application. All BRDFs have a single channel; RGB color is achieved by independently processing each channel with varying parameters. We generate 300 rough conductor BRDFs and 300 rough dielectric BRDFs, together with 12,720 layered BRDFs [Guo et al. 2018] by randomly layering them into 2 layers; additionally, we also generate 1,800 three-layer BRDFs, which means that their bottom layers are already layered BRDFs. We use the three-layer BRDFs to finetune the layering network, after it has been first trained with two layers, as described in Sec. 5.1.

Each rough dielectric BRDF has two parameters: roughness $\alpha_1$ and the index of refraction (IOR) $\eta$. Each rough conductor BRDF also has two parameters: roughness $\alpha_2$ and a Schlick Fresnel approximation with $R_0$ controlling the reflectance at 0 degrees. Therefore, each two-layer BRDF has six parameters: $\alpha_1, \eta, \alpha_2, R_0, A$, and the albedo $A$ and the extinction coefficient $\sigma_T$. In our implementation, we use GGX model as the normal distribution function at interfaces, and only consider isotropic BRDFs, although anisotropic materials could be included. The sampling distributions of different parameters are shown in Table 2.

For each BRDF, we sample 25$^4$ pairs of incoming and outgoing directions. Since we only consider the reflection, we perform a stratified sampling along the elevation angle $\theta$ and azimuth angle $\varphi$ on the upper hemisphere, where $\theta \in [0, \frac{\pi}{2})$ and $\varphi \in [0, 2\pi)$. For each sampled incoming and outgoing direction pair, we compute the BRDF value via microfacet model for rough conductor/dielectric BRDFs or Guo et al. [2018] for layered BRDFs. Then we store the incoming direction, outgoing direction and the BRDF value (without the cosine term).

The generated dataset is used for training the different networks:

**Representation network.** We use 12,000 two-layer BRDFs as our training set, and the other 720 two-layer BRDFs as validation. Note that although we do not use rough conductor/dielectric BRDFs to train this network, they can still be represented, because their appearances could be regarded as special cases of layered BRDFs.

**Layering network.** We project 12,720 two-layer BRDFs and their components (300 rough conductor and 300 rough dielectric BRDFs) from the dataset into the latent space with the trained representation network. Then the projected latent vectors are used for training the layering network, with the same proportions of training and validating set as in the representation network. Also, the 1,800 three-layer BRDFs are used to finetune this network.

**Sampling network.** We randomly choose 3,000 two-layer BRDFs from the dataset for training and another 300 two-layer BRDFs for validation. We first project them into the latent space, similar to the layering network, and then we compute the ground-truth GNDFs, as mentioned in Sec. 3.4.

4.2 Training

The representation network is trained first, as the layering and sampling networks rely on the representation network.

**Representation Network.** During training this network, the shared network parameters and the latent vectors of current input BRDFs are updated simultaneously in every iteration. We calculate the $L_1$ loss, which can better preserve the color and avoid artifacts, compared to the $L_2$ criterion, according to our experiments. The $L_1$ loss is simple

$$\text{Loss} = \frac{1}{N} \sum \left| f_{\text{pred}} - f_{\text{gt}} \right|,$$

where $N$ denotes the number of BRDFs in a batch, $f_{\text{pred}}$ and $f_{\text{gt}}$ represents BRDF values output by our network and the ground-truth. We use learning rates $3 \times 10^{-4}$ for the network weights and $1 \times 10^{-4}$ for the mutable latent vectors in training set. Both learning rates decay by 0.9 after every epoch. We initialize all the latent vectors to 1, and we train the network for 50 epochs in about 40 hours on an RTX 2080Ti GPU.

**Layering Network.** We supervise this network with latent vectors as both inputs and outputs, via the latent vectors obtained from our trained representation network, and optimize it by the $L_1$ loss (Equation 7) with the initial learning rate of $7 \times 10^{-4}$. The learning rate decays by 0.7 for every 50 epochs. It takes us about 10 hours to train this network on an RTX 2080Ti GPU for 1,000 epochs. Additionally, we finetune the layering network with 1,800 three-layer BRDFs.

**Sampling Network.** We sample 40 × 40 points on the ground-truth pdf and our proxy pdf (Equation 6), and then minimize their difference by the Kullback-Leibler divergence (KLD) loss. The KLD loss is defined as

$$\text{KLD loss} = \sum \left( f_{\text{pred}} \log \frac{f_{\text{pred}}}{f_{\text{gt}}} + f_{\text{gt}} - f_{\text{pred}} - f_{\text{gt}} \right).$$
Fig. 10. Comparison of the representation abilities with different BRDF configurations between Rainer et al. [2020], Sztrajman et al. [2021], and our representation network. The visualization of the outgoing radiance and the difference maps are also provided. For single-layer materials, the reference is produced by the microfacet model. For layered materials, the reference images are rendered using Guo et al. [2018]. Both Sztrajman et al. [2021] and our method produce similar results to the reference, while Rainer et al. [2020] is less accurate. Note that, although the method of Sztrajman et al. [2021] can produce smaller numerical error in some cases, it also produces obvious color differences. Also note that we focus on representation in this figure; the multi-layer BRDFs being projected are ground truth, not the outputs of our layering network.

\[ KLD_{\text{Loss}} = \frac{1}{M} \sum_{i=1}^{M} \left( S(f^{gt}) \log S(f^{gt}) - \log S(f^{pred}) \right), \]  

(8)

where \( S \) denotes the softmax function and \( M \) denotes the sample count on a distribution. We start at a learning rate of \( 3 \times 10^{-5} \) and shrink it by \( 0.7 \) for every \( 3 \) epochs. We trained this network for 10 epochs in total, which costs less than 1 hour on an RTX 2080Ti video card.

4.3 Rendering pipeline

Before using our Neural BRDF models for rendering, we do some preparation: for rough conductor/dielectric BRDFs and the components of layered BRDFs, we represent them by the latent vector using our representation network; for layered BRDFs, we perform the layering operation and get the layered latent vector; for SVBRDFs, we prepare a latent texture, where each texel stores a latent vector.
Now, we use our Neural BRDF models in rendering by path tracing. Firstly, we store all incoming and outgoing directions and lighting values of each ray at all intersections into buffers. Secondly, for each buffer pixel with the Neural BRDF type, we infer the representation network for the BRDF value. Finally, we calculate the radiance of path tracing to get output images, applying specific reconstruction filters, such as Gaussian filters.

We also integrate our implementation with the MIS framework. According to the different sampling demands (light sampling, BRDF sampling or MIS), we store all queries and the pdf information for each part above into buffers. Then we calculate the radiance via our network and finally combine the weighted results, if needed.

In order to accelerate the GPU inference, we implement the inference in CUDA via NVIDIA CUTLASS CUDA Template and compile it into Python libraries. Thanks to the delicate optimization in Cutlass, there is no obvious increase in the time cost when the film resolution rises, as long as it doesn’t run out of the GPU memory. We compile several libraries for different buffer sizes in advance, and dynamically decide which to use during rendering. Eventually, the single BRDF evaluation with resolution $1920 \times 1080$ costs 5 ms.

5 RESULTS

We have implemented our method inside the Mitsuba renderer [Jakob 2010] and compared our method with previous works, including Guo et al. [2018] and Belcour [2018]. Specifically, since the method by Guo et al. [2018] does not introduce any approximations other than Monte Carlo noise, we use it as the reference. All the implementations are taken from the authors’ websites. All timings in this section are measured on an Ubuntu Linux workstation with an Intel Xeon E5-2650 v4 @ 2.20GHz CPU (8 cores), 64 GB of main memory and an RTX 2080Ti GPU (11 GB).

5.1 Quality validation

We first validate our individual operations, then demonstrate rendering results on more complex scenes.

**Representation/evaluation network.** In Figure 10, we compare our representation network against Rainer et al. [2020], Sztrajman et al. [2021] and Guo et al. [2018] (reference) on varying materials. We use the pretrained model provided by Rainer et al. [2020] and train the model for Sztrajman et al. [2021] using their released code. Rainer et al. [2020] cannot handle high-frequency materials well, and suffers from visible artifacts.

Although Sztrajman et al. [2021] produces visually similar results to ours, their method has 6× more storage cost than our method (even when using the dimensionality reduction), which makes it less practical for SVBRDFs. Even though Sztrajman et al. [2021] can...
produce lower error in some cases (rows 2–4), there are still obvious color differences from the reference.

Our representation network is suitable not only for analytic BRDF data, but can generalize to measured BRDFs, such as those from the MERL dataset [Matusik 2003]. In Figure 12, we fine-tune our trained network on the MERL dataset for 30 epochs in 3 hours, and we provide the visualization of the outgoing radiance distributions from our representation network. We also show that our representation network is able to represent SVBRDFs/BTFs in Figure 13 (note again that Sztrajman et al. [2021] would be difficult to apply for this purpose).

**Sampling network.** In Figure 6, we compare the rendered results using our sampling network against sampling parametric lobes like Lambertian lobes or GGX, with equal number of samples per pixel. Our method produces the best results. Also note that, since our fitted GNDF is independent of the incoming direction, and only dependent on the underlying BRDF, we can precompute and store the fits as a preprocessing. In this way, we avoid the expensive inference of the sampling network when drawing samples at rendering time. Therefore, our sampling method is as efficient as sampling an analytic BRDF lobe.

Having enabled BRDF sampling, our method automatically enables MIS. In Figure 7, we compare the results rendered with light sampling only, BRDF sampling only, and MIS combining light sampling and BRDF sampling. As expected, MIS further improves the sampling quality.

**Layering network.** In Figure 11, we compare results from our layering network against Guo et al. [2018] (as reference with a high sampling rate) across different BRDF configurations — different roughness for the top and bottom layers and varying albedos for the medium in between. Our results are close to the reference. In Figure 14, we compare our layered materials with Belcour [2018] and Guo et al. [2018]. We can see that our method produces results close to the reference and with less noise, and our shading speed is faster than Belcour [2018] (though note that we utilize the GPU for network inference). This confirms the effectiveness of our layering network.

Our layering network can be applied recursively to obtain materials with multiple (3 or more) layers. In Figure 15, we show the results with three-layer BRDFs using our layering network fine-tuned on 1, 800 of them, and we find our result still close to the reference.

**Interpolation.** Our neural BRDFs support interpolation in the latent space. We compare the lobe visualizations of our method and the linear interpolation (blending/mixture) in Figure 4. Our latent space interpolation gives more natural results. For example, during the interpolation between two BRDFs with low roughness and high roughness, we naturally expect one lobe with intermediate roughness, rather than a mixture of both.

We further extend the BRDF interpolation operation to level-of-detail rendering. Recall that we use a multi-channel texture to define SVBRDFs, where each texel is a latent vector instead of an RGB/RGBA value. In Figure 5, we build a mipmap of our latent texture as a preprocessing, then we use standard trilinear interpolation to query the mipmap at appropriate levels during rendering, which successfully avoids the aliasing even at a low sampling rate (1 samp).

### 5.2 Complex scenes

In Table 3, we report the scene settings (and additional equal time MSE comparison with Guo et al. [2018]). Please also check out the accompanying video, where we show animations of the complex scenes and elaborate the detailed parameters of our layered BRDFs.
Neural BRDFs: Representation and Operations

Fig. 16. Comparison between Guo et al. [2018] and our method on the Globe scene with spatially-varying albedos of the medium between two layers. The difference images show that our method has much less error than Guo et al. [2018].

Fig. 17. Comparison between Guo et al. [2018] and our method on the Teapot scene with spatially-varying albedos of the medium between two layers (and spatially-varying roughness in the video). Again, the difference images show that our method has much less error than Guo et al. [2018].

Fig. 18. Comparison between our method and Guo et al. [2018] in the Shoe scene. In this scene, we apply a normal map on the layered BRDF, and we render both methods with 1 spp. Thanks to our noise-free BRDF layering and evaluation operations, our method has low noise even at 1 spp (noise only comes from the environment lighting and indirect illumination). Again, the cost of our method includes CPU time and GPU time, and the GPU is only used for inference of our neural networks.

Globe. In Figure 16, we show a globe with a two-layer BRDF. The top of the BRDF is a relatively smooth dielectric varnish layer and the bottom is a rough conductor. The medium between two layers has spatially-varying scattering properties. And we define spatially-varying albedos of the interface between two layers. In this scene, we compare our method against Guo et al. [2018] at equal time. We find that our result has much less noise, since our method does not use randomness during BRDF evaluation.

Teapot. In Figure 17, we demonstrate the ability of our method to perform appearance editing by changing the underlying latent texture. The BRDF consists of a varnish layer on the top and a rough conductor layer on the bottom. We can arbitrarily specify spatially-varying scattering parameters (e.g., albedos) in the medium interface between layers (as well as spatially-varying roughness, shown in the accompanying video) to display various patterns. Each edit requires a re-evaluation of our layering network, which is fast compared to the rendering itself. Our method is able to produce results close to the ground-truth for the edited spatially-varying material, and our method produces much less noise than Guo et al. [2018].

Shoe. In Figure 18, we compare our method with Guo et al. [2018] on the Shoe scene under a point light and environment lighting. The surface of the Shoe is defined with a normal mapped BRDF consisting of two layers and a constant medium in between. With only 1 spp, our method is already close to noise-free (since the highlights mostly come from the point light in direct illumination), thanks to our noise-free layering and evaluation operations.
Table 3. We tabulate the scene settings, time consumption (minutes) and error (MSE) in all scenes, compared with Guo et al. [2018].

<table>
<thead>
<tr>
<th>Scene</th>
<th>Resolution</th>
<th>Ours Spp MSE</th>
<th>Guo et al. [2018] Spp MSE</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Still Life (Fig. 1)</td>
<td>1024 × 1024 512 1.0 × 10⁻³</td>
<td>64 2.0 × 10⁻³</td>
<td>4.56</td>
<td></td>
</tr>
<tr>
<td>Globe (Fig. 16)</td>
<td>1024 × 1024 256 9.3 × 10⁻⁴</td>
<td>24 2.3 × 10⁻³</td>
<td>2.16</td>
<td></td>
</tr>
<tr>
<td>Teapot (Fig. 17)</td>
<td>720 × 480</td>
<td>256 6.0 × 10⁻⁴</td>
<td>12 5.4 × 10⁻³</td>
<td>0.87</td>
</tr>
</tbody>
</table>

Still Life. Figure 1 shows a variety of spatially-varying effects, including varying roughness, varying Fresnel, varying albedos of the interface, and normal mapping. Again, we can see that our method produces almost identical results to the reference on all these configurations within much less time.

5.3 Discussion and limitations

Our method is able to represent a large range of single-layer and multi-layer BRDFs with both specular and diffuse appearances, and the latent representation can be easily operated to produce different effects. However, there are some approaches that we have not tried but may be potentially helpful, and we also have identified some main limitations of our method. Below, we briefly discuss the key points.

Bidirectional Transmittance Distribution Functions (BTDFs). When training our layering network, we only use the reflection information from each BRDF layer to get the reflectance of the final layered material. When a BRDF is used as the top interface of a layering network, its corresponding BTDF will be implicitly inferred by the layering network, and is never constructed explicitly. On the one hand, this is an advantage of our method, because we will never need to store and represent BTDFs. On the other hand, an extension to full "Neural BSDFs" may be interesting and useful for other effects (e.g., translucent fabrics).

Scope/types of BRDFs. Currently, we do not train our model on anisotropic or normal mapped BRDFs (from individual layers). Including these types of BRDFs will further improve the practicality of our method, but can also be more challenging to both neural representation and operation, since the dimension of input data will further increase. While we believe our general framework could handle these effects, we leave the exploration of anisotropic and normal mapped BRDFs for future work.

Accumulated error. We have shown that when recursively applied, our layering network can be used to predict BRDFs consisted of multiple layers. However, error will accumulate as more BRDFs are layered together. This could be addressed by networks trained on a larger fixed number of BRDF layers, or exploiting neural network architectures that allow a dynamic number of inputs.

Bias and energy conservation. In practice, any neural network may produce unpredictable error, which cannot be treated as unbiased in the Monte Carlo sense. The error can make the results consistently darker/brighter in some angular regions, introducing bias or violation of energy conservation in rendering. This issue affects all neural rendering solutions; we have not observed artifacts caused by this, but the problem may require future research.

6 CONCLUSION AND FUTURE WORK

In this paper, we have presented a framework for neural BRDFs. We focus on both representation and operations for BRDFs. We use a general neural network to compress BRDFs into short latent vectors, and we train additional networks that operate solely in the latent space, providing individual operations to BRDFs. Our representation network is able to compress a wide range of BRDFs, including typical microfacet BRDFs, layered BRDFs or measured BRDFs, accurately and compactly. And we have demonstrated those operation networks are able to perform common BRDF operations, such as importance sampling, interpolation and layering. Eventually, our Neural BRDFs can be easily used in the rendering pipeline under the MIS framework. And we have shown that shading using our BRDF latent textures and operation neural networks is efficient, especially for layered materials.

We believe that the proposed representation/operations model is novel and practical, leading to a black-box style "Neural BRDF algebra". However, this BRDF algebra is still not complete enough to encompass all common BRDFs and operations on them. Our model is currently trained on isotropic materials and media for now, but it could be extended to anisotropic materials and media, as well as explicit handling of transmissive BTDFs. It would also be interesting to introduce normal mapping operations in latent space.

REFERENCES


Neural BRDFs: Representation and Operations


