MetaLayer: A Meta-learned BSDF Model for Layered Materials

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Reproducing the appearance of arbitrary layered materials has long been a critical challenge in computer graphics, with regard to the demanding requirements of both physical accuracy and low computation cost. Recent studies have demonstrated promising results by learning-based representations that implicitly encode the appearance of complex (layered) materials by neural networks. However, existing generally-learned models often struggle between strong representation ability and high runtime performance, and also lack physical parameters for material editing. To address these concerns, we introduce MetaLayer, a new methodology leveraging meta-learning for modeling and rendering layered materials. MetaLayer contains two networks: a BSDFNet that compactly encodes layered materials into implicit neural representations, and a MetaNet that establishes the mapping between the physical parameters of each material and the weights of its corresponding implicit neural representation. A new positional encoding method and a well-designed training strategy are employed to improve the performance and quality of the neural model. As a new learning-based representation, the proposed MetaLayer model provides both fast responses to material editing and high-quality results for a wide range of layered materials, outperforming existing layered BSDF models.
1 INTRODUCTION

Real-world materials are mostly layered, containing multiple layers with varying compositions (e.g., coated metals, varnished woods, glazed ceramics, and metallic paints). The complex interactions between the light and layers give rise to visually rich and diversified appearance characteristics that are not exhibited by single-layer materials. Unfortunately, due to the complexity of subsurface light transport, realistically rendering these layered materials has long been a daunting and challenging task in computer graphics [Bati et al. 2019; Weidlich and Wilkie 2009, 2011], bottlenecking many rendering engines.

General and accurate layered BSDF (Bidirectional Scattering Distribution Function) models either rely on per-material precomputation [Jakob et al. 2014; Zeltner and Jakob 2018] or resort to stochastic evaluation [Gamboa et al. 2020; Guo et al. 2018; Xia et al. 2020]. Recent precomputation-based models [Jakob et al. 2014; Zeltner and Jakob 2018] succeed in capturing aggregate scattering behaviors for layered materials with various layer components using the adding-doubling strategy [van de Hulst 1980]. However, they require long per-material precomputation time and large storage, making them impractical for spatially-varying cases. Stochastic layered BSDF models, pioneered by Guo et al. [2018], are free from costly precomputation, but suffer from low efficiency and high variance, since Monte Carlo sampling is involved in the estimation of the light scattering inside layers.

With the advent of deep neural networks, learning-based BSDF models [Fan et al. 2022; Hu et al. 2020; Kuznetsov et al. 2021, 2022; Rainer et al. 2019; Tongbuasirilai et al. 2022; Zheng et al. 2022] have emerged as a preferable choice for modeling very complex appearance behaviors compared to conventional models. Deep neural networks are adept at learning robust priors on large-scale reflectance data, allowing us to reach an unprecedented level of realism in visual appearance. However, these learned BSDF models often struggle between strong representation ability (large networks with many parameters) and high runtime performance (small networks with few parameters). Without additional efforts (e.g., designing and training another network [Hu et al. 2020]), they also usually lack physical or perceptual parameters for convenient material editing or effective inverse rendering [Bati et al. 2021]. This is particularly important for layered materials since many graphical applications need the ability to adjust the physical parameters of each layer to reach the desired aggregate appearance. Moreover, these models usually have low generalization ability due to the limited scale of material datasets [Dupuy and Jakob 2018; Filip and Vávra 2014; Matusik et al. 2003].

To tackle the above issues and to make learning-based layered BSDF models more practical, we propose MetaLayer which introduces meta-learning [Hospedales et al. 2022; Thrun and Pratt 1998] into layered material modeling and rendering. The key idea behind MetaLayer is learning to learn a neural representation for any layered BSDF. This is a typical hypernetwork design [Ha et al. 2017] which is a special category of meta-learning [Hospedales et al. 2022]. Specifically, MetaLayer involves a BSDFNet to compactly encode layered materials into implicit neural representations and a MetaNet to establish the mapping between the physical parameters of each material and the weights of its corresponding neural representation. Such a weight generation scheme allows weight sharing across layers of networks [Ha et al. 2017]. To retain high-frequency details and eliminate annoying artifacts, a new positional encoding method named Rusinkiewicz spherical harmonics encoding is used in BSDFNet.

Once trained jointly via a well-designed training strategy, MetaNet is expected to generate the specific network weights of BSDFNet for any unseen layered material through only one feed-forward propagation, operating in milliseconds. Material editing is enabled by directly changing the input of MetaNet, i.e., the physical parameters of layered materials.

To summarize, the main contributions of this work are:

- a meta-learning framework, i.e., MetaLayer, for layered material modeling, providing convenient material editing and better generalization than existing learning-based models,
- a specially-designed training strategy to train BSDFNet and MetaNet in two phases, enabling stable convergence,
- a new positional encoding method named Rusinkiewicz spherical harmonics encoding to retain high-frequency details for directional distributed BSDF data,
- an efficient integration of our MetaLayer within any physically-based renderer, demonstrating high-speed evaluation, little precomputation overhead, and convenient material editing.

2 RELATED WORK

Approximate Layered BSDF Models. Reproducing physically correct appearance for layered materials requires solving a very complex 1D radiative transfer equation [Hanrahan and Krueger 1993; Pharr and Hanrahan 2000]. Generally, interaction phenomena take place not only at the surfaces, but also within any point of the medium. To reduce the computational burden, many practical models resort to certain approximations, in particular, the simplified computation of the light transport within layered materials. For instance, some layered BSDF models lack proper evaluation of multiple scattering inside layers [Gu et al. 2007; Hanrahan and Krueger 1993] considering the high computational overhead of multiple scattering. Others even completely ignore any scattering event within individual layers [Dai et al. 2009; Guo et al. 2017; Weidlich and Wilkie 2007, 2009, 2011]. A prominent layered BSDF model in this category is the statistical framework of Belcour [2018] which approximates the surface reflectance as the summation of multiple lobes derived from directional albedo, incident direction, and roughness. Later, much work has been dedicated to extending this statistical approach to handle anisotropy [Weier and Belcour 2020; Yamaguchi...
et al. 2019], diffuse interfaces [de Dinechin and Belcour 2022] or arbitrary scattering volumes [Ran drivianandrasana et al. 2021]. There are also many approximate models targeting specific layered materials such as dusty surfaces [Gu et al. 2007], metallic patinas [Dorsey and Hanrahan 1996], paper [Papas et al. 2014], leaves [Baranowski and Rokne 2001] and human skin [Stam 2001]. Usually, these approximate models make a compromise between physical accuracy and computing time.

Precomputation-based Layered BSDF models. The difficulty in designing general layered BSDF models resides in correctly accounting for multiple scattering within the layered structures. For efficient evaluation, one flourishing way is to precompute the angular distribution of the materials and store it using some compact representations. The first generic layered BSDF model based on precomputation is proposed by Jakob et al. [2014] which relies on an expensive angular-Fourier mode matrix representation. This model can be seen as a significant extension to Stam’s discretization approach [Stam 2001] and was later further extended by Zeltner and Jakob [2018] to handle anisotropic interfaces. Ergun et al. [2016] extended Jakob et al.’s model to predict the appearance of car paint from the paint composition. Despite their high accuracy and efficiency at runtime, these models are generally impractical for spatially-varying structures due to long per-material precomputation time and significant storage overhead. They also easily suffer from ringing artifacts, especially at grazing angles. In contrast, our meta-learning-based solution is free from costly per-material precomputation, while still guaranteeing excellent visual effects for any layered material.

Stochastic Layered BSDF models. To achieve accurate evaluation of layered BSDFs with arbitrary compositions, another promising strategy is to use the Monte Carlo simulation which accounts for all light transport paths naturally [Novák et al. 2018]. However, directly applying the Monte Carlo simulation to layered material rendering is prohibitively expensive, since a large number of scattering events may happen at the layer interfaces or inside the internal medium. Guo et al. [2018] proposed a position-free Monte Carlo method that leverages a path-space simplification tailored to the layered material context. The proposed model is accurate, unbiased, and general, but is still plagued with high variance on account of the stochastic nature, leading to a very long convergence time. Several subsequent studies tried to reduce variance by developing more efficient Monte Carlo methods [Gamboa et al. 2020; Xia et al. 2020]. Gamboa et al. [2020] presented an efficient path construction method to sample and evaluate high-throughput, low-variance paths through an arbitrary number of interfaces and media layers. Xia et al. [2020] introduced pair-product sampling and multi-product sampling to better take advantage of the layered structure and reduce variance compared to Guo et al.’s approach. Despite these efforts for variance reduction, a straightforward implementation of these stochastic models is rather inefficient and impractical for the production purposes.

Learning-based Appearance Modeling. Recent years have witnessed great progress in reproducing visual appearance using deep learning [Dong 2019]. A series of neural methods have been developed from different perspectives for appearance modeling. Some existing neural methods aim at recovering physically-plausible material maps from one or a small number of input images using end-to-end trained neural networks [Aittala et al. 2016; Deschaintre et al. 2018, 2019; Guo et al. 2021; Li et al. 2017, 2018]. Others try to exploit a low-dimensional latent space from the material data, so as to intelligently reduce the dimensionality of the data for measured BRDF [Fan et al. 2022; Hu et al. 2020; Zheng et al. 2022], spatially-varying BRDF [Gao et al. 2019; Guo et al. 2020], bidirectional texture function (BTF) [Kuznetsov et al. 2021, 2022; Rainer et al. 2020, 2019], etc. After compressing raw high-dimensional material data using material-specific neural networks, each material is represented as a low-dimensional latent code. However, these latent codes usually lack physical parameters for intuitive material editing or effective inverse rendering [Bati et al. 2021]. Recently, Xu et al. [2022] encoded BRDF, visibility, and lighting using a set of neural basis functions.

Unlike these methods, we encode each layered material within the weights of a trained neural network called BSDFNet. The weights are predicted by a meta-network called MetaNet, given some physically meaningful material parameters such as surface roughness and extinction coefficient of the medium. The weight prediction is a typical hypernetwork design, one of the meta-learning strategies in neural networks [Hospedales et al. 2022; Hu et al. 2019]. This facilitates the compression, rendering, and editing of arbitrary layered materials. Hypernetworks have also been used in modeling appearance maps [Maximov et al. 2019] and 3D faces [Bi et al. 2021].

A similar meta-learning idea is also mentioned in the work of Sztrajman et al. [2021] in which each BRDF is overfitted to the weights of a small neural network and is further compressed into a low dimensional embedding. However, the small scale of the neural network limits its representation ability, and the choice of overfitted weights makes their method only support BRDF interpolation. Different from that work, our neural representation of layered materials has stronger expressiveness and robustness thanks to a weight sharing strategy introduced in BSDFNet. It also significantly expands the material editing ability due to the special design of MetaNet and the training strategy. More recently, a Metapositional model is proposed by Fischer et al. [2022] which also leverages meta-learning for visual appearance reproduction. However, their meta-learning paradigm is significantly different from ours. They chose a model-agnostic meta-learning framework to improve the inference accuracy of trained models, while our goal is to use a meta-network to produce weights of another network, thus supporting convenient material editing and fast evaluation.

3 THE METALAYER MODEL
In this section, we describe our MetaLayer model and its implementation details.

3.1 Motivation and Overview
Recent learning-based BSDF models typically need to train the networks for every new material, and the material is encoded in the
network parameters [Sztrajman et al. 2021] or a fixed-length latent vector [Fan et al. 2022; Hu et al. 2020; Zheng et al. 2022] after training for an enormous number of iterations. Generally, each of these models is restricted to representing only materials within its learned latent space, potentially limiting its ability to express previously unseen materials. More critically, these methods are hard for material editing, since no connection is established between the materials’ neural representations and their physical parameters. Consequently, only material interpolation is readily supported by most existing neural methods. However, the ability of explicit parameter tuning is important for layered materials since many graphical applications, including both forward rendering [Belcour 2018] and inverse rendering [Bati et al. 2021], need the ability to adjust the physical parameters of each layer to determine the desired aggregate appearance.

We address the above limitations with the proposed MetaLayer model, a meta-learning-based method for modeling arbitrary layered materials. The basic idea is illustrated in Fig. 2. Specifically, we represent the BSDF of any layered material as a parameter function $F(\omega_i, \omega_o; \Theta_F)$ with the trainable parameters $\Theta_F$. Currently, $F$ is realized as a fully-connected multi-layer perceptron (MLP) with positional encoding. This network, named BSDFNet, is optimized to map from a pair of input directions $\omega_i$ and $\omega_o$ to the RGB reflectance value at that pair of directions. Theoretically, such a coordinate-based neural representation is continuous and naturally has an infinite resolution.

Meta-learning is normally used to train a meta network to produce the weights of another network. In our context, we construct a meta neural network, named MetaNet, to generate the weights of BSDFNet (taken as the base network). MetaNet, also realized as an MLP $M$ with its trainable weights $\Theta_M$, takes a set of physical parameters $\Gamma$ of a layered material and produces the partial weights (\(\Theta_F^*\)) of the corresponding BSDFNet. These partial weights ($\Theta_F^*$), together with other weights of BSDFNet which are frozen after training and are shared across all layered materials, are expected to faithfully reproduce the appearance of that layered material. This weight sharing strategy is adopted to reduce the scale of the neural BSDF model, while still preserving strong expressiveness and high generalization ability.

Overall, our meta-learned layered BSDF model is formally given by the following equations:

$$M(\Gamma; \Theta_M) = \Theta_F^*$$  

$$F(\omega_i, \omega_o; \Theta_F) = \hat{f}_2(\omega_i, \omega_o, \Gamma)$$  

where $\Theta_F^*$ denotes a subset of $\Theta_F$ which is generated by the MetaNet $M$ and $\hat{f}_2(\omega_i, \omega_o, \Gamma)$ returns the actual BSDF value of the corresponding layered material with physical parameters $\Gamma$ evaluated at $\omega_i$ and $\omega_o$. Both BSDFNet and MetaNet are trained together on $N = N_f \times N_{\omega_i} \times N_{\omega_o}$ samples. In particular, the weights $\Theta_F$ are optimized such that $F$ matches $\hat{f}_2$ as closely as possible for all coordinates $\omega_i, \omega_o$, i.e.,

$$\Theta_F = \arg \min_{\Theta_F} \sum_{i=1}^{N_f} \sum_{m=1}^{N_{\omega_i}} \sum_{n=1}^{N_{\omega_o}} L(\hat{f}_2(\omega_i^{(m)}, \omega_o^{(n)}; \Theta_F), f(\omega_i^{(m)}, \omega_o^{(n)}, \Gamma^{(i)}))$$

where $L$ is a task-specific loss measuring the error between $f_2$ and $F$. Once trained, we are able to generate the specified network parameters of BSDFNet through one feed-forward propagation in the MetaNet, given a set of physical parameters of a layered material. Then, this specific BSDFNet can be integrated into any renderer, working as a standard parametric BRDF model.

The specific design of this BSDF model leads to the following benefits:

- It is efficient and possesses low variance since Monte Carlo sampling is not required in evaluating this model.
- It supports convenient material editing with physically meaningful parameters.
- It does not rely on any costly precomputation and hence is friendly to spatially-varying cases.
- It is a general model which supports a wide range of layered materials.

### 3.2 BSDFNet

In our MetaLayer model, every layered material is represented as a deep neural network $F$ which takes as input a pair of normalized directions $\omega_i$ and $\omega_o$. By encoding data into this coordinate-based network, the appearance of a layered material will be essentially...
represented using the weights (or parameters) of the network. One key design choice of this network is that some weights ($\Theta_i$) are inferred from a set of physical parameters $\Gamma$ by another deep neural network, while others are shared (by the weight sharing strategy) across all materials.

The detailed architecture of BSDFNet is depicted in the right panel of Fig. 3. As seen, this network consists of five hidden layers with 64 neurons per hidden layer, except the last one which only has 32 neurons. ReLU is adopted as the activation function. Let $v_i$ be the output of the $i$-th layer. Note that $v_i$ in each layer (except the first and last layers) can be subdivided into three parts which are visualized as different colors in Fig. 3:

- $v^+$: values predicted directly by MetaNet during the inference stage,
- $v^-$: values computed by the frozen (shared) weights ($W^+$ and $b^+$) of BSDFNet,
- $v^*$: values computed by predicted weights ($W^*$ and $b^*$) from MetaNet.

According to the above rules, layer $i$ of the network is computed as

$$v_{i+1}^+ = a(W_i^+(v_i^+ \odot v_i^+ \odot v_i^*) + b_i^+)$$  \hspace{1cm} (4)

$$v_{i+1}^- = a(W_i^-(v_i^- \odot v_i^- \odot v_i^*) + b_i^-)$$  \hspace{1cm} (5)

where $a(\cdot)$ is the element-wise activation function and $\odot$ denotes element-wise concatenation. Currently, we opt to predict the different channels of reflectance/transmittance independently. Therefore, the output of the last layer is only a scalar. We observe that this can reduce the risk of color drifting.

In our current design of BSDFNet, not only its partial weights ($W^*$ and $b^*$) are predicted by MetaNet, but also some neurons’ values, i.e., $v^*$. These neurons serve as important connections between BSDFNet and MetaNet, enabling valid back-propagation of gradients from BSDFNet to MetaNet. Without these neurons, gradients may vanish since the activation functions could enforce some outputs to be zero. In this case, the weights $W^*$ and $b^*$ have little impact on the back-propagation of gradients. More detailed derivations and discussions are provided in the supplemental material.

The splitting of $v$ and the weight sharing strategy adopted in each hidden layer are specially designed to significantly reduce the storage cost and avoid overfitting. With the weight sharing strategy, only 293 parameters ($32 \times 4$ for $v^+$, $32 \times 5$ for $W^*$ and 5 for $b^*$) should be stored for each layered material. A large portion of network parameters are frozen and shared across different materials. The reduced dimensionality of the predicted parameter space also stabilizes the training process and speeds up convergence.

Comparison with Prior Representations. This network has over 13K parameters which are sufficient to reproduce the complex appearance of a wide range of layered materials. In comparison, NBRDF proposed by Sztrajman et al. [2021] only has two small hidden layers for a total of 675 parameters which are further compressed into 32 values. DeepBRDF [Hu et al. 2020] generally adopts a 10-dimensional latent code to represent each measured BRDF. From this, our BSDFNet has a much stronger representational ability than these previous models. This is visually validated in Fig. 4. As seen, NBRDF fails to preserve high-frequency glossy highlights, due to its limited representation ability. Even if we increase the scale of NBRDF (i.e., NBRDF+ in Fig. 4) to match the number of trainable parameters as our BSDFNet, it still produces sub-optimal results as highlighted in the error maps, due to the lack of proper positional encoding as explained in the next subsection. Note that the difficulty of training for meta-learning is closely related to the number of weights to be predicted. NBRDF enables easy convergence by reducing its scale, but at the cost of low representative ability. We guarantee both strong representative ability and easy convergence via weight splitting and sharing. Fan et al. [2022] recently adopted a neural network (NLBRDF) with over 1G trainable parameters to encode layered BRDFs. Without specially-designed acceleration with GPUs, such a large network will incur significant overhead to existing renderers. In comparison, our meta-learning design guarantees the strong expressiveness of BSDFNet with far fewer parameters, and also allows convenient material editing which is not easily supported by Fan et al.’s work.

3.3 MetaNet

State-of-the-art neural BSDF models (e.g., DeepBRDF, NBRDF, and NLBRDF) often lack the ability to quickly generalize in a sample efficient manner to new unseen materials. They also lack editability. For instance, handling a new material for NLBRDF requires extracting the latent code from this material, which comes with a certain cost of generating training examples and optimizing the latent vector with some additional back-propagate steps. In contrast, our MetaNet is designed and trained to predict the partial weights of our coordinate-based network (BSDFNet). This makes our approach more expressive than prior works, allowing it to represent a wider range of appearance. The editability is realized by the mapping between explicit material parameters and BSDFNet’s partial weights. Specifically, we represent the material variability by an explicit material parameter vector $\Gamma$. In our current setting, $\Gamma$ includes the surface properties of two interfaces (the surface roughness: $\alpha_1$...
we adjust \( \sigma \) and replace its relative index of refraction with the corresponding internal medium's properties. Although coordinate-based MLPs (like BSDFNet and MetaNet in ACM Trans. Graph., Vol. 42, No. 6, Article 221. Publication date: December 2023), provide an efficient way to encode complex scattering behaviors of layered materials, they have difficulty in learning extrapolation (e.g., the materials outside the dashed yellow box in Fig. 3). The architecture of MetaNet is shown in the left panel of Fig. 3. It has 16 hidden layers, each of which has 256 neurons. As aforementioned, we currently predict independently for each RGB channel. This results in 6 neurons for the input layer.

We train MetaNet and BSDFNet using a specially-designed training strategy. Once converged, MetaNet directly maps a set of physical parameters \( \Gamma \) to a vector of network parameters of BSDFNet including \( W^\ast, b^\ast \) and \( v^\ast \), through only a forward pass. This is quite different from some gradient-based meta-learning methods [Andrychowicz et al. 2016; Finn et al. 2017; Fischer and Ritschel 2022] which require solving an optimization problem to fine-tune the weights at test time and is convenient for material editing. We illustrate the ability of convenient material editing using MetaNet in Fig. 5. Here, we adjust \( \sigma_1 \) and \( \sigma_2 \). New layered materials can be generated immediately and their appearance varies smoothly. Note that the strong generalization ability of meta-learning even allows appearance extrapolation (e.g., the materials outside the dashed yellow box in Fig. 5) which is not supported by previous models (e.g., DeepBRDF and NLBRDF).

### 3.4 Rusinkiewicz Spherical Harmonics Encoding

Although coordinate-based MLPs (like BSDFNet and MetaNet in our framework) provide an efficient way to encode complex scattering behaviors of layered materials, they have difficulty in learning high-frequency functions, such as the near specular reflections for very smooth surfaces. Recent studies have shown that this spectral bias [Basri et al. 2020; Rahaman et al. 2019] can be overcome by using positional encodings [Mildenhall et al. 2020; Müller et al. 2021; Tancik et al. 2020] which significantly improve the representation ability of MLPs.

To allow our BSDFNet to learn high-frequency spherical signals on \( S^2 \) better, we adopt a new positional encoding method named Rusinkiewicz Spherical Harmonics Encoding. This method firstly converts the input coordinates of BSDFNet (i.e., \( \omega_i \) and \( \omega_o \)) into the Rusinkiewicz coordinates [Rusinkiewicz 1998]: \( \omega_h \) and \( \omega_d \). The Rusinkiewicz coordinate system adopts an efficient sampling strategy for tabulation by allowing dense sampling near specular highlight regions, thus providing a much better suited set of variables to encode specular lobes. Then, the following mapping is applied to both \( \omega_h \) and \( \omega_d \):

\[
y(\omega) = \left[ \omega, Y_0^0(\omega), Y_{-1}^1(\omega), Y_1^1(\omega), Y_{-1}^0(\omega), Y_1^0(\omega), ..., Y_m^m(\omega), ... \right]^T
\]  

\(^{(6)}\)
to map them to a higher-dimensional space. Here, \( Y_m^l(\omega) \) is a series of spherical harmonics (SH) basis functions of varying order \( l \) and degree \( m \). Note that our Rusinkiewicz spherical harmonics encoding is deterministic and allows our network to bias towards data that has more frequency content along \( \omega_d \) and \( \omega_h \). We currently choose up to ninth order SH basis functions for positional encoding, thus resulting in a total of 168 input dimensions to BSDFNet.

To show the effectiveness of our Rusinkiewicz spherical harmonics encoding method, we compare predicted BSDFs using different
positional encoding methods in Fig. 6. As expected, the fitted BSDFs without any positional encoding method fail to recover high-frequency signals of glossy highlights due to the low dimensionality of the input. Incorporating positional encodings, such as 2D sinusoidal encodings widely used in previous work [Abadi et al. 2020; Müller et al. 2021], may alleviate this problem. However, sinusoidal encodings will cause distracting ghosting artifacts along the glossy lobes. In comparison, our proposed encoding method is free from these artifacts and achieves high-quality results that are much closer to the reference.

3.5 Two-phase Training Strategy

To speed up convergence, our networks are trained in a two-phase manner, as summarized in Algorithm 1. In the first phase, BSDFNet and MetaNet are trained jointly using the dataset described below. This stage is designed to help the training process to be initially more stable, since BSDFNet and MetaNet have different objectives.

In the second phase, the training steps of BSDFNet and MetaNet are interleaved in a meta-training manner, as specified in lines 9-24 in Algorithm 1. During this phase, each time we sample a layered material from the dataset, its sample set \( X \) (with \( N_{\omega_i} \) varying incident direction \( \omega_i \) and \( N_{\omega_o} \) varying outgoing direction \( \omega_o \)) is split into two subsets: \( X_1 \) and \( X_2 \). \( X_1 \) is first used to train BSDFNet for \( K_1 \) steps, while freezing the weights in MetaNet. These training steps aim to stabilize the shared weights in BSDFNet. Then, \( X_2 \) is used to train MetaNet for \( K_2 \) steps, updating \( \Theta_M \) only. This training phase lets our framework generalize to new materials more easily.

3.6 Training Details

We train our networks with TensorFlow [Abadi et al. 2015] on a server with eight NVIDIA 2080Ti GPUs. We use the Adam optimizer with default parameters and an initial learning rate of 0.0005 to train all networks. The learning rate decays by 0.99 for every 8 epochs. For layered materials with reflective/conductive base layers, we train a single model with 225 epochs (100 epochs for the first training phase and 125 epochs for the second training phase), taking roughly 50 hours. For layered materials with transmissive/dielectric base layers, we train two models for the BRDF part and the BTDF part separately. Each model is trained with 200 epochs (100 epochs for the first training phase and 100 epochs for the second training phase), taking roughly 48 hours.

Loss Function. The loss function for training our networks is inspired by the reverse Huber loss which has shown great success in the dense depth prediction problem [Laina et al. 2016; Wang et al. 2020]. Specifically, our loss function is defined as

\[
L(f, f^t) = \begin{cases} \frac{|T(f) - T(f^t)|}{\mu + |T(f) - T(f^t)|} & |T(f) - T(f^t)| \leq t \\ \frac{|T(f) - T(f^t)|}{t} & |T(f) - T(f^t)| > t \end{cases} \tag{7}
\]

where \( t \) is a positive threshold and \( T \) is the \( \mu \)-law transformation [Kalantari and Ramamoorthi 2017] used to compress the high dynamic range of the reflectance value:

\[
T(f) = \text{sign}(f) \frac{\log(1 + \text{abs}(f)\mu)}{\log(1 + \mu)} \tag{8}
\]

Algorithm 1 Two-phase training

**Input:** A training dataset \( D \) with \( N = N_{\Gamma} \times N_{\omega_i} \times N_{\omega_o} \) samples

**Output:** Trained MetaNet \( M(\Theta_M) \) and BSDFNet \( F(\omega_i, \omega_o, \Theta_F) \)

1. Randomly initialize \( \Theta_M \) and \( \Theta_F \)
2. for iterations in the first phase do
3. Sample a material from \( D \) with a sample set \( X \)
4. for samples in \( X \) do
5. Feed-forward propagation of \( M(\Theta_M) \) and \( F(\Theta_F) \)
6. Evaluate the loss \( L \) and update both \( \Theta_M \) and \( \Theta_F \)
7. end for
8. end for
9. for iterations in the second phase do
10. Sample a material from \( D \) with a sample set \( X \)
11. Split \( X \) into \( X_1 \) and \( X_2 \)
12. for \( K_1 \) steps do
13. for samples in \( X_1 \) do
14. Feed-forward propagation of \( F(\Theta_F) \)
15. Evaluate the loss \( L \) and update \( \Theta_F \)
16. end for
17. end for
18. for \( K_2 \) steps do
19. for samples in \( X_2 \) do
20. Feed-forward propagation of \( M(\Theta_M) \) and \( F(\Theta_F) \)
21. Evaluate the loss \( L \) and update \( \Theta_M \)
22. end for
23. end for
24. end for

Table 1. Sampling functions used to generate layered materials for the LayeredBRDF and LayeredBTDF datasets. \( U \) denotes the uniform distribution and \( \mathcal{V} \) means sampling the set with the discrete uniform distribution.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Sampling</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roughness for top interface</td>
<td>( a_1 )</td>
<td>( U(-3, -0.5) )</td>
</tr>
<tr>
<td>Roughness for bottom interface</td>
<td>( a_2 )</td>
<td>( U(-3.0) )</td>
</tr>
<tr>
<td>IOR for dielectric interface</td>
<td>( \eta_1, \eta_2 )</td>
<td>( U(1.05, 2) )</td>
</tr>
<tr>
<td>Fresnel for conductive interface</td>
<td>( R_0 )</td>
<td>( U(0, 1) )</td>
</tr>
<tr>
<td>Single-scattering albedo for medium</td>
<td>( \rho )</td>
<td>( 1 - U(0, 1)^2 )</td>
</tr>
<tr>
<td>Extinction coefficient for medium</td>
<td>( \sigma_t )</td>
<td>( \mathcal{V}([0, 1, 2, 5]) )</td>
</tr>
</tbody>
</table>

with \( \mu \) controlling the amount of compression. We currently set \( t = 0.1 \) and \( \mu = 32 \). Empirically, this loss function provides a good balance between L1 error and L2 error. In our context, L2 aims to reconstruct the potential large values at highlight regions while L1 is responsible for preserving the long tail of the layered BSDF. Moreover, this loss function is continuous and first order differentiable at the threshold \( t \) where the switch from L1 to L2 occurs.

Dataset Preparation. To train the proposed networks, we collect two datasets: a LayeredBRDF dataset for layered materials with reflective/conductive base layers and a LayeredBTDF dataset for layered materials with transmissive/dielectric base layers. Both datasets are generated according to Guo et al.’s method, using a sampling
rate of 128 spp. The LayeredBRDF dataset contains $N_T = 12,000$ BRDFs and the LayeredBTDF dataset contains $N_T = 10,000$ BSDFs. The distributions of their parameters are listed in Table 1. Currently, we use GGX as the normal distribution function at interfaces, resulting in two roughness parameters $\alpha_1$ and $\alpha_2$ for either conductive or dielectric interfaces. For conductive base layers, we adopt the Schlick Fresnel approximation with $R_0$. The inside medium is described by the extinction coefficient $\sigma_1$ and single-scattering albedo $\rho$.

For each BRDF in the LayeredBRDF dataset, we sample $25^4$ pairs of spherical angles $(\theta, \phi)$ of the $\omega_b$ and $\omega_d$ vectors in the Rusinkiewicz parameterization [Rusinkiewicz 1998]. We perform stratified sampling along the elevation angle $\theta$ and azimuth angle $\psi$ on the upper hemisphere, where $\theta \in [0, \frac{\pi}{2})$ and $\phi \in [0, 2\pi)$. For BTDFs in the LayeredBTDF dataset, the elevation angle $\theta$ covers the whole sphere, i.e., $\theta \in [0, \pi]$, resulting in $4 \times 25^4$ pairs of spherical angles.

4 RENDERING WITH METALAYER

Renderer Integration. Integrating our Metalayer model into existing renderers is quite easy and straightforward, which can be seen as another benefit of this model. Once BSDFNet and MetaNet converge, BSDFNet can be used as similarly as other parametric BSDF models since BSDFNet in our current design is lightweight and portable. Consequently, the learned BSDFNet can run without the support of GPU resources, thus neglecting any workload from data transfer between CPU and GPU. Except for positional encodings which are precomputed and stored in a look-up table, BSDFNet only contains matrix multiplication/addition operations and ReLU activation functions that are easy for data-level parallelism. In practice, we parallelize these operations via the Intel Advanced Vector Extensions 512 (AVX-512) instruction set [Intel 2023].

For MetaNet, it should run only once for a given material, although it contains much more parameters than BSDFNet. This design significantly improves the performance of our model during runtime, while still preserving its strong representation ability by transferring much computation to the precomputation step. To support spatially-varying layered BSDFs, only the parameters predicted by MetaNet are stored in textures. Other trainable parameters in BSDFNet are fixed and shared across all layered materials.

Importance Sampling. The usage of a new BSDF model in a ray/path tracing-based renderer also requires the ability to properly sample the BSDF and to estimate the probability of this sampling. Considering that the appearance of layered materials typically has multiple dominant lobes, we adopt the following multi-lobe probability distribution, inspired by [Belcour 2018]:

$$p(\omega_o | \omega_i) = \frac{E_{\text{all}}}{\sum_{i=0}^{N} E_i} \sum_{i=0}^{N} E_i \rho_i(\alpha_i)$$

(9)

where $E_i$ is the energy for the $i$-th lobe, $E_{\text{all}}$ is the total energy, $\rho_i$ is the probability density function (PDF) of sampling the visible normals [Heitz and d’Eon 2014], and $\rho_i$ is the PDF of the $i$-th microfacet model. Currently, we select two lobes (R and TRT) for layered materials with reflective base layers and select three lobes (R, TRT, and TT) for layered materials with transmissive base layers. Please refer to [Belcour 2018] for more details on the estimation of the parameters. During rendering, we randomly selected one lobe based on $E_i$ and importance sample the visible normals [Heitz and d’Eon 2014].

Summary of Abilities. Our Metalayer model has many desired properties when integrated into existing renderers. Table 2 compares the abilities of the proposed Metalayer model against several existing models. Currently, only our model fully supports layered BTDFs with two transmissive interfaces. It seems that other models may also be extended to allow the evaluation of transmittance, but the extension is not that straightforward. Supporting textured or spatially-varying material parameters is also important for BSDF models, which is enabled by our model and NLBRDF [Fan et al. 2022]. Perhaps the main advantage of our model, as compared with existing learning-based models, is its convenience in material editing. NLBRDF [Fan et al. 2022] also allows material editing, but needs significant efforts to fine-tune the latent codes of unseen materials. Another benefit of our model is that it can run with pure CPU resources, thanks to the lightweight design of BSDFNet. Therefore, porting this model to different platforms is relatively easy, and running the model does not involve time-consuming CPU-GPU data transfer.

5 RESULTS AND DISCUSSION

We have implemented our Metalayer model in the Mitsuba renderer [Jakob 2010] as a new BSDF plugin. In this section, we demonstrate the effectiveness and efficiency of our method on layered materials with various combinations of parameters. All test materials in this section are new and never appear in the training dataset. All results are generated on a workstation with an Intel Core i9-9900X processor and 64GB RAM. As aforementioned, our lightweight BSDF model does not require any GPU resource at runtime. Reference images are rendered using Guo et al.’s bidirectional method [Guo et al. 2018] at a high sampling rate (2048 spp by default). Please refer to the accompanying video for animated versions of several scenes.

5.1 Comparison on Reflective Layers

We first compare our method with previous work on modeling layered materials with reflective base layers. Fig. 7 compares our neural method to Belcour’s efficient model based on statistical operators [Belcour 2018]. As a typical approximate model, it has many
limitations such as inaccuracy for very rough interfaces and ignorance of multiple scattering. As expected, our method produces the appearance of layered materials much closer to the reference than the Belcour’s model, especially for rough interfaces ($\alpha_1 = 0.1, \alpha_2 = 0.3$) shown in Fig. 7.

In Fig. 8, we compare our method to the model of Guo et al. [2018] on an equal sampling rate (64 spp). Closeups in the second row highlight the high variance caused by stochastic evaluation in Guo et al.’s BSDF model. Note that our BSDFNet, as a parametric BSDF model, runs much faster than Guo et al.’s model at the same sampling rate for this scene. The last row shows the evolution of RMSE of both methods with respect to the sampling rate (Spp).

rendering at the same sampling rate (64 spp). It also achieves low variance as highlighted in the closeups, implying that rendering with our neural BSDF model converges much faster. The convergence curves in the last row clearly show that our method converges faster than the model of Guo et al.

In Figs. 9 and 10, we make comparisons to Fan et al.’s NLBRDF model [Fan et al. 2022] which also leverages neural networks to represent layered materials. Compared with our neural method, NLBRDF generally has two limitations in practice. First, NLBRDF needs to prepare BRDF data (roughly 55 minutes) for materials with any unseen parameters and optimize their latent codes using the data before rendering. This restricts it to only support material interpolation within BRDFs with known data and latent codes. In particular, the surface properties (e.g., surface roughness) are not allowed to be freely edited. Therefore, spatially-varying surface properties
are not supported by NLBRDF \(^2\). With our MetaNet, the weights of each material can be determined in less than 1 second. This allows us to freely edit any material parameters and easily support spatially-varying cases, as shown in Fig. 9. Second, the CPU-GPU collaborative rendering strategy in Fan et al.’s method is difficult to handle path tracing with long paths, such as the case in the second row of Fig. 10. Again, our method is free from this limitation and can efficiently run in a wide range of complex scenes.

Table 3 further demonstrates the advantage of our model by quantitatively comparing against NBRDF [Sztajman et al. 2021] and its variant on 100 randomly selected layered BRDFs from the test set. More visual comparisons are provided in the supplemental material.

To further verify the efficiency and high fidelity of our model, we make a series of pair-wise comparisons with Guo et al.’s method on the Dragon scene with varying extinction coefficient \( \sigma_t \). Fig. 11 shows the results when \( \sigma_t \) increases from 0.0 to 3.0. As seen, our method produces visually similar appearance to Guo et al.’s method on different layered materials. The absence of Monte Carlo sampling in our neural model helps us to achieve lower-variance results than Guo et al.’s on different configurations, at the same sampling rate (64 spp). Quantitative evaluations in terms of root mean square error (RMSE), as compared with high-quality reference images, further show the benefit of our model in reducing the variance. It should be noted that the runtime cost of Guo et al.’s model increases prominently as \( \sigma_t \) increases, since a larger \( \sigma_t \) incurs more scattering events in the medium. This is clearly shown in Fig. 12 where we plot the time spent by layered materials with varying extinction coefficient \( \sigma_t \). The comparisons tell that our neural model has a constant runtime cost since the architecture of BSDFNet is fixed. When \( \sigma_t = 5.0 \), our method achieves nearly 6x runtime acceleration as compared with Guo et al.’s method on this Dragon scene at the same sampling rate.

### 5.3 Spatially-varying Cases

The lightweight design of our BSDFNet allows us to support spatially-varying BSDFs, without any GPU assistance. When the parameters of a layered material are encoded in textures, we run MetaNet for each texel and the resulting weights of BSDFNet are stored in a look-up table (LUT). This LUT is then retrieved at rendering time, with each slot representing a layered material. We currently use the nearest neighbor search to retrieve the LUT, without introducing additional storage and computational overhead. However, our method supports linearly interpolating the LUT. Fig. 15 shows our results of the Globe scene with spatially-varying BRDFs. Here, we show an equal-time comparison with Guo et al.’s bidirectional method. As seen, our method is able to produce high-quality result with much lower variance as compared with Guo et al.’s method. Even at the same sampling rate (64 spp), our method still outperforms its competitor due to the intrinsic smoothness and robustness brought by our trained neural representation.

In Fig. 16, we edit the Kettle scene with spatially-varying layered materials (reflective base layers). Processing these textures takes less than one minute with MetaNet. The processing time increases linearly with the resolution of the texture and is much lower than the rendering time. Editing of transmissive layered materials is demonstrated in Fig. 17 where we edit either the surface roughness or the albedo of the medium, with spatially-varying parameters.

Concerning memory consumption, our method currently requires a 293D vector for each material. For instance, the material in the left image of Fig. 16 requires roughly 1.7GB memories. In comparison, Fan’s method only requires a 32D latent code per material. However, this 32D code should be re-optimized for each unseen material and relies on a very large network (1G parameters) for decoding.

### 5.4 Validation of Network Design

Our networks have several key design choices. To validate their effectiveness, we report the performance of our complete model as

<table>
<thead>
<tr>
<th>NBRDF</th>
<th>NBRDF+</th>
<th>Ours</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>0.891</td>
<td>0.873</td>
</tr>
<tr>
<td>STD</td>
<td>1.960</td>
<td>2.488</td>
</tr>
</tbody>
</table>

Table 3. Quantitative comparison in terms of mean and standard deviation (STD) against NBRDF and an extended version of NBRDF (NBRDF+). The values (RMSE) are counted over 100 layered BRDFs with random parameters, lit by a single point light. Best scores are highlighted in **bold**.

<table>
<thead>
<tr>
<th>Sinusoidal</th>
<th>Sinusoidal</th>
<th>SH</th>
<th>SH (Ours)</th>
</tr>
</thead>
<tbody>
<tr>
<td>((\omega_i, \omega_o))</td>
<td>((\omega_i, \omega_o))</td>
<td>((\omega_h, \omega_d))</td>
<td>((\omega_h, \omega_d))</td>
</tr>
<tr>
<td>Mean</td>
<td>1.249</td>
<td>1.265</td>
<td>1.230</td>
</tr>
<tr>
<td>STD</td>
<td>2.847</td>
<td>2.241</td>
<td>2.833</td>
</tr>
</tbody>
</table>

Table 4. Quantitative evaluation in terms of mean and standard deviation (STD) of different positional encoding methods. The values (RMSE) are counted over 100 layered BRDFs with random parameters, lit by a single point light. Best scores are highlighted in **bold**.
\[
\sigma_t = 0.0 \\
\sigma_t = 0.5 \\
\sigma_t = 1.0 \\
\sigma_t = 2.0 \\
\sigma_t = 3.0
\]

\[\text{RMSE} = 0.079\]
\[\text{RMSE} = 0.048\]
\[\text{RMSE} = 0.042\]
\[\text{RMSE} = 0.040\]
\[\text{RMSE} = 0.040\]

\[\text{RMSE} = 0.092\]
\[\text{RMSE} = 0.059\]
\[\text{RMSE} = 0.048\]
\[\text{RMSE} = 0.044\]
\[\text{RMSE} = 0.043\]

Fig. 11. Impact of the extinction coefficient \(\sigma_t\) of the medium. We compare our method to Guo et al. [2018] on the Dragon scene with increasing \(\sigma_t\). RMSE values are provided for each image. Closeups in the second row and their corresponding error maps in the third row (left: Ours, right: Guo et al.) highlight the benefit of method in variance reduction.

Fig. 12. Variations of the runtime cost (at 64 spp) of the Dragon scene with respect to the extinction coefficient \(\sigma_t\).

As an important building block in our framework, the Rusinkiewicz spherical harmonics encoding method has already shown its advantage in preserving high-frequency details for some typical glossy lobes in Fig. 6. In Table 4, we further validate its superiority by quantitatively comparing against some other encoding methods on 100 randomly selected layered BRDFs from the test set. More visual comparisons are provided in the supplemental material.

5.5 Validation of the Loss Function
We also validate the effectiveness of the loss function, as compared with the conventional L1 loss and L2 loss. Our loss function combines the benefits of both L1 loss and L2 loss. This allows the trained model to preserve both low-frequency information (diffuse reflection) and high-frequency information (glossy highlights). Table 5 reports the prediction accuracy in terms of RMSE for models trained on different loss functions. We evaluate the accuracy using the rendered images under either point lighting or environmental lighting. The model trained with our loss function achieves the lowest error in either case. A typical example is shown in Fig. 19. The error occurs mainly at the highlight regions, while our loss function is beneficial for reducing this error, as clearly shown by the scan line comparisons.

5.6 Validation of the Two-phase Training Strategy
We finally validate the effectiveness of the proposed two-phase training strategy in Fig. 20. As compared with the traditional one-phase training strategy that always trains BSDFNet and MetaNet:
\[ \sigma_t = 0.0 \]
\[ \sigma_t = 1.0 \]
\[ \sigma_t = 2.0 \]

Fig. 13. Rendering the Frosted Glass scene \((\alpha_1 = \alpha_2 = 0.02)\) using our MetaLayer model (the top row) and Guo et al.’s model (the bottom row), respectively. RMSE values are provided for each image. The last row shows the evolution of RMSE of both models on the transmissive case \((\sigma_t = 2.0)\) with respect to the sampling rate (Spp).

Fig. 14. Variations of the runtime cost (at 64 spp) of the Frosted Glass scene with respect to the extinction coefficient \(\sigma_t\).

Table 5. Quantitative evaluation (in terms of RMSE) of different loss functions used to train our networks. The values are averaged over 100 layered BRDFs with random parameters, lit by a single point light and an environment light respectively. Best scores are highlighted in bold.

<table>
<thead>
<tr>
<th></th>
<th>L1 loss</th>
<th>L2 loss</th>
<th>Our loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>Point light</td>
<td>0.096</td>
<td>0.106</td>
<td><strong>0.092</strong></td>
</tr>
<tr>
<td>Environment light</td>
<td>0.018</td>
<td>0.018</td>
<td><strong>0.017</strong></td>
</tr>
</tbody>
</table>

Fig. 15. Visual comparison to the method of Guo et al. [2018] on the Globe scene with spatially-varying layered materials.

Fig. 16. Editing reflective layered materials with spatially-varying (textured) parameters. The resolution of each texture and the processing time of MetaNet are shown for each case.

Fig. 17. Editing transmissive layered materials with spatially-varying (textured) parameters. The resolution of each texture and the processing time of MetaNet are shown for each case.
Fig. 18. Training loss versus epochs for different variants of our model.

Fig. 19. Validation of different loss functions. Here, we compare the error of intensity (as compared with reference) along the red scan line.

Fig. 20. Evolution of RMSE (evaluated on 100 randomly selected layered BRDFs from the test set) with respect to the training epoch, for two different training strategies.

jointly, our specially-designed training strategy makes the training more stable and allows the trained model to recover layered BSDFs with lower errors.

6 DISCUSSION, LIMITATION AND FUTURE WORK

Smooth Surfaces. Our MetaLayer model may incur large errors for very smooth surfaces with near-specular reflection, possible due to the $\mu$-law transformation and the limited accuracy of floating-point operations in the networks. As shown in Fig. 21, when the surface roughness approaches 0.001, large errors appear at the highlight region, resulting in inconsistent shading as compared with the reference.

Multiple Layers and Anisotropy. Our model currently handles a single layer with two interfaces. The extension to multiple layers is straightforward. We only need to generate the training examples from multi-layered materials and expand the parameter set $\Gamma$ (as well as the input nodes of MetaNet) by including other layers’ properties. Similarly, our model can also be extended to handle anisotropic interfaces [Weier and Belcour 2020] by adjusting the parameter set and training set. However, as the number of parameters increases, training our networks becomes difficult. We leave this as the future work.

Optimal Importance Sampling. Importance sampling is the key to ray/path tracing-based renderers. The proposed multi-lobe sampling algorithm is simple, efficient, and satisfies many layered materials. However, this is not the optimal importance sampling algorithm for layered materials since layering multiple interfaces would result in more than two lobes. Consequently, investigating an optimal and robust importance sampling strategy for arbitrary layered materials (including anisotropy and multiple layers) deserves further study.

Measured Materials. Adopting data-driven BRDF models using real material measurements has always been the pursuit of many physically-based renderers. However, extending our MetaLayer model to support measured materials is not that straightforward, since MetaNet requires explicit parameters of the material as input. A possible solution is to compress measured materials into a low-dimensional latent space (like DeepBRDF [Huet al. 2020]), and then feed the latent code to MetaNet. Nevertheless, one major goal of the proposed layered BSDF model is convenient artistic design for layered materials which is not compatible with measured materials.

Energy Conservation. As a neural representation based on neural networks, our model does not guarantee energy conservation since the trained networks may produce unpredictable error. However, in practice, we never observed any artifact that is caused by the violation of energy conservation. Investigating neural BSDF models that always conserve energy would be an interesting future work.
7 CONCLUSION

Layered materials are ubiquitous in the natural world. This paper has proposed a new method, named as MetaLayer, to reproduce the complex appearance from layered materials, with high visual quality, low runtime cost, and strong editing ability. The key idea is incorporating meta-learning into layered appearance modeling, which addresses several tough issues of previous neural appearance models, making learning-based appearance models more practical. Besides, several novel designs, including a new positional encoding method, a well-designed training strategy and a weight sharing strategy, further improve the effectiveness and efficiency of the proposed model. To our best knowledge, this is the first layered material model that incorporates meta-learning. We believe the new methodology behind our MetaLayer model can be applied to other complex appearance modeling/rendering scenarios.

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