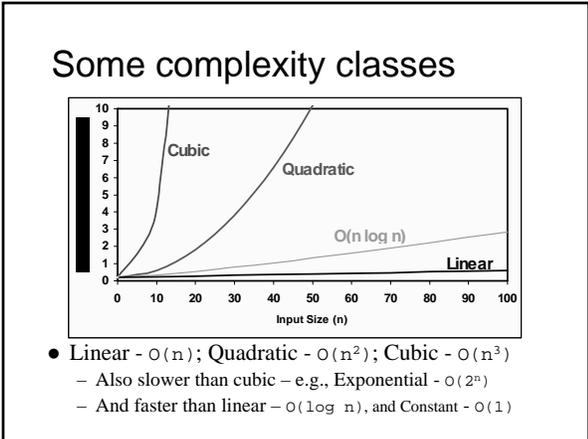
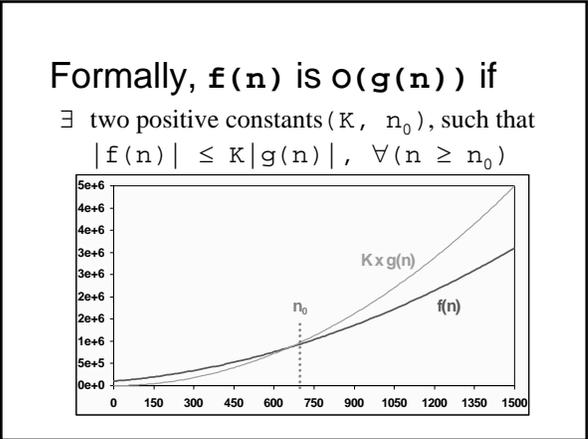


# Monday: 2<sup>nd</sup> Midterm Exam

- ## Algorithm analysis
- Need a way to measure efficiency
    - Regardless of processor speed or compiler implementation
      - Both of which can *greatly* affect processing time
    - And independent of the programming language used
  - Really just need a way to *compare* algorithms
    - i.e., holding constant things that don't matter
    - Question becomes – which algorithm is more efficient on *any computer in any language*?
  - Solution – ‘O’ notation
    - Simplest type is worst case analysis – called Big-Oh
      - Little-oh, Big  $\Omega$  (omega), and Big  $\Theta$  (theta) – not in CS 12

- ## Big-Oh notation
- Strips problem of inconsequential details
    - All but the “dominant” term are ignored
      - e.g., say algorithm takes  $3n^2 + 15n + 100$  steps, for a problem of size  $n$
      - Note: as  $n$  gets large, first term ( $3n^2$ ) dominates, so okay to ignore the other terms
    - Constants associated with processor speed and language features are ignored too
      - In above example, ignore the 3
  - So this example algorithm is  $O(n^2)$ 
    - Pronounced “Oh of n-squared”
      - Belongs to the “quadratic complexity” class of algorithms



- ## Applies to large problems only
- Big-Oh measures asymptotic complexity
    - Mostly irrelevant for small problems
    - But some algorithms become impractical as  $n$  grows
  - Say linear time is 256 microseconds ( $\mu$ secs):
    - $O(\log_2 n)$  time is 8  $\mu$ secs
    - $O(n \log_2 n)$  time is 2.05 milliseconds (ms)
    - Quadratic time is 65.5 ms
    - Cubic time is 16.8 seconds
    - Exponential time (base 2) is  $3.7 \times 10^{63}$  years!!!

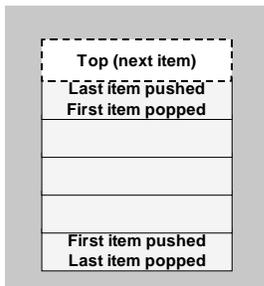
## Efficiency of list functions

- If singly-linked list (like assignment 2):
  - Insert/delete first –  $O(1)$
  - Insert/delete last/random –  $O(n)$ 
    - If pointer to last item – insert last is  $O(1)$
  - Find value –  $O(n)$
  - Retrieve/set  $i^{\text{th}}$  item –  $O(n)$
- Compare to array:
  - Insert/delete first/random, and find value –  $O(n)$
  - Insert/delete last –  $O(1)$  – unless resize, then  $O(n)$
  - Retrieve/set  $i^{\text{th}}$  item –  $O(1)$  – the array's strong point

## What Big-Oh doesn't cover

- Small problems
  - Often dominated by lesser terms or constants
- What to count?
  - Comparisons? Assignments? Reads? Writes?
  - Some operations take longer than others
    - Depends in part on the system, compiler, and so on
- Notice the definition is not restrictive
  - e.g., an algorithm that is  $O(n)$  is also  $O(n^2)$ , etc.
  - So *agree* to express bound as tightly as possible, and to not include lesser terms in  $g(n)$

## Stacks



- LIFO data structure
  - Last In, First Out
- All items except last item pushed are inaccessible
- So has very few possible operations:
  - push, pop, peek, empty, full, size, clear
- Lots of applications

## Applying stacks

- Can be used to eliminate recursion
  - Iteration and stacks instead of recursive calls
    - For each "recursive" step
      - Push `struct` full of critical data values
    - While stack is not empty
      - Pop `struct` – like "return" from recursive call
  - It's how the compiler does it
    - Pushes "activation record" (a.k.a., "stack frame") for every function call, not just recursive ones (see text section 7.7)
- In fact, idea applies to *any nested structure*
  - Recursion is just a nesting of function calls
  - What about nested parentheses in expressions?

## Checking balanced ( ), [ ], { }

- Okay to nest, like  $\{x/[y*(a+b)]\}$
- Not okay to mismatch (or nest improperly)
  - $(a/(x + y))$  is missing a right parenthesis
  - $(x + [y-2])$  is mismatched at [ ]
- Parentheses fully match if the following works:

```
for (each character in the expression) {
    if a left parenthesis - push it on the stack;
    if a right parenthesis
        pop matching left parenthesis from stack
} stack is empty at the end
```
- See program 7.5 in text

## Implementing stacks

- Easy with a list (too easy for programming project):
  - Say `ListPointer list = createList();`
  - Then to push: `insertFirst(item, list);`
  - To pop: `return deleteFirst(list);`
  - To peek: `return firstInfo(list);`
  - To clear: `clearList(list);`
  - `emptyStack: return emptyList(list);`
  - `fullStack: return 0; /* does not fill up */`
- Easy with an array too
  - And it's more efficient – less function overhead