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ABSTRACT

We present a constraint caching framework to expedite potentially expensive satisfiability and model-counting queries. Integral to this framework is our new constraint normalization procedure under which the cardinality of the solution set of a constraint, but not necessarily the solution set itself, is preserved. We extend these constraint normalization techniques to string constraints in order to support analysis of string-manipulating code. We use a grouptheoretic framework, which generalizes earlier results, to express our normalization techniques. We also present a parameterized caching approach where, in addition to storing the result of a modelcounting query, we store a model-counter object that allows us to efficiently recount the number of satisfying models for different bounds. We implement these techniques in our tool Cashew, which is built as an extension of the Green caching framework [55], and integrate it with the symbolic execution tool Symbolic PathFinder (SPF) and the model-counting constraint solver ABC. Our experiments show that constraint caching can significantly improve the performance of symbolic and quantitative program analyses. For instance, Cashew can normalize the 10,104 unique constraints in the SMC/Kaluza benchmark down to 394 normal forms, achieve a 10x speedup on the SMC/Kaluza-Big dataset, and an average 3x speedup in our SPF-based side-channel analysis experiments.

CCS CONCEPTS

• **Software and its engineering** → *Formal software verification*;

KEYWORDS

Constraint caching, quantitative program analysis, model counting, string constraints

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1 INTRODUCTION

Improvements in the area of satisfiability modulo theories [10, 12] and powerful SMT solvers [11, 20, 21] have been key technological developments enabling the rise of effective symbolic program analysis and testing techniques in the last decade [15, 27, 32, 48].

Performing symbolic analysis via satisfiability checking, however, is not sufficient for quantitative program analysis, which is an important problem that arises in many contexts such as probabilistic analysis [14, 24, 38], reliability analysis [22] and quantitative information flow [7, 17, 28, 40, 41, 43-45, 50, 53]. The enabling technology for quantitative program analysis is model-counting constraint solvers. A model-counting constraint solver returns the number of solutions for a given constraint within a given bound [6, 8, 39].

Since constraint solving and model counting are heavily used in program analysis, improving performance of these tasks is of critical importance. In this paper, we present a new approach for constraint normalization and constraint caching with the goal of improving the performance of quantitative program analyses.

The key step in constraint caching is normalization of constraints, i.e., reducing constraints to a normal form, where two constraints are reduced to the same form only if they are equivalent (w.r.t. satisfiability or model counting). Using the normal form of a constraint as a key, we can recover results of previous satisfiability or model-counting queries without recomputing them.

Earlier techniques for constraint caching [4, 31, 55] 1) focus only on numeric constraints and do not handle string constraints, 2) use normalization techniques that preserve the exact solution set of a constraint, which reduces cache hits for model-counting queries, and 3) always produce cache misses for model-counting queries if a different bound is used, even if the queried constraint remains the same. In this paper, we extend earlier results in multiple directions:

- We present constraint normalization techniques for model counting under which the solution set of the constraint may not be preserved but its cardinality is.
- · We extend constraint caching to string constraints which is crucial for analyzing string manipulating code.
- · We present a parameterized caching approach where, in addition to the result of a model-counting query, we also cache a counter object in the constraint cache that allows us to efficiently recount the models for different bounds.
- · We formalize our normalization scheme using an extensible group-theoretic framework for constraint normalization that

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generalizes earlier results on constraint normalization for caching.

We implemented these techniques in our tool Cashew, which is built as an extension of the Green caching framework [55]. We integrated Cashew with Symbolic PathFinder (SPF) [42] and the ABC [6] model-counting constraint solver. Our experiments demonstrate that constraint caching can improve the performance of quantitative program analysis significantly.

The paper is organized as follows: In Section 2 we provide some motivating examples for constraint caching. In Section 3 we give an overview of our constraint caching framework. In Section 4 we discuss our group-theoretic normalization scheme. In Section 5 we describe the constraint language we support. In Sections 6 and 7 we present the constraint normalization procedure. In Section 8 we present our experiments. In Section 9 we discuss related work. In Section 10 we present our conclusions. In Section 11 we describe how to obtain and use the implementation.

2 MOTIVATION

The amount of string-manipulating code in modern software applications has been increasing. Common uses of string manipulation include: 1) Input sanitization and validation in web applications; 2) Query generation for back-end databases; 3) Generation of data formats such as XML and HTML; 4) Dynamic code generation; 5) Dynamic class loading and method invocation. In order to analyze programs that use string manipulation, it is necessary to develop techniques for efficient manipulation of string constraints. Recently, there has been significant amount of work in string constraint solving to address this problem [2, 23, 29, 30, 33–36, 47, 52, 57]. One of our contributions in this paper is a constraint normalization and caching framework that can handle string constraints.

Consider the following string constraint *F*:

$$b = ``https" \land prefix_of(b, url) \land c = ``?" \land contains(c, url) \land w \in (0|1)^+ \land index_of(w, url) = 8$$

The solution set of *F* is the set of values that can be assigned to the string variables *b*, *c*, *w*, and *url* for which *F* evaluates to true.

Constraints such as F commonly arise in symbolic program analysis. For example, F might correspond to a path constraint generated during symbolic execution of a string-manipulating program. A fundamental question about a constraint F generated during program analysis is its satisfiability. Symbolic program analysis techniques generate numerous satisfiability queries while analyzing programs. Given that satisfiability checking is computationally expensive, it is crucial to answer satisfiability queries efficiently in order to build scalable symbolic program analysis tools.

On the other hand, quantitative program analysis techniques ask another type of question while analyzing programs. Assume that we bound the length of the string variables b, c, w, and url in constraint F to 5. How many different string values are there for the variable b such that the constraint F is satisfiable within the given bound? These types of queries can be answered by modelcounting constraint solvers. Again, due to the high complexity of model counting, answering model-counting queries efficiently is crucial for quantitative program analysis. T. Brennan, N. Tsiskaridze, N. Rosner, S. Aydin, and T. Bultan

Now, consider the following string constraint *G*:

 $k = "#" \land w = "http: " \land contains(k, var0) \land z \in (1|0)^+$ $\land index_of(z, var0) = 8 \land prefix_of(w, var0)$

Constraint *G* is a constraint on string variables k, z, w, and var0. Assume that constraints *F* and *G* are generated during program analysis and it is necessary to check the number of satisfying solutions and satisfiability of each. Can we avoid making redundant calls to the constraint solver? Note that the solution sets of *F* and *G* are different since different string constants appear in these two constraints. However, the satisfiability and the cardinality of the solution sets for these two constraints are identical. Hence, if we were able to detect the relationship between the number of satisfying models of *F* and *G* and had stored the result of a model-counting query on *F*, then when we see *G* we do not have to call the modelcounting constraint solver again. Same for satisfiability queries.

The problem of reusing information about F to answer our questions about G has now been reduced to finding a fast way to determine that F and G are equivalent with respect to satisfiability and model counting. In this paper, we present a constraint normalization scheme to determine this type of equivalence. Based on our scheme, the normalized form of F and G are identical:

 $v0 = "a" \land v1 = "bccde" \land contains(v0, v2)$ $\land prefix_of(v1, v2) \land v3 \in (f|g)^+ \land index_of(v3, v2) = 8$

Hence, given a constraint, to determine if an equivalent constraint has already been encountered, we normalize it and check if its normal form was seen previously. Using a constraint store to cache the results of prior queries to the solver, we avoid redundant queries for constraints that have the same normalized form.

For both satisfiability and model-counting queries, we can cache the result of the query in a constraint store, use normalization to determine equivalence of constraints, and then reuse the query results from the store when we get a cache hit. However, since model-counting queries come with a bound parameter, in order for the query to match, the bound also has to match. While this limits our ability to reuse results in the most general case, there is a class of model-counting constraint solvers whose results can be reused even is the case of mismatched bounds. Parameterized model-counting techniques [6, 39] not only count the number of solutions for a constraint within a given bound, but also generate a model counter that can count the number of solutions for any given bound. Note that counting the number of solutions with different bounds may be necessary during program analysis. For example, consider the following constraint which has no solutions for bounds less than 5 but has satisfying solutions for higher bounds:

$contains(x, "abcde") \land |y| > |x| \land y \in (ab)^*$

In this paper, we present a parameterized caching approach that utilizes parameterized model-counting constraint solvers. We assume that, in response to a model-counting query, parameterized model-counting constraint solvers return a model-counter object that can be used to count the number of models for any given bound. By storing the model-counter object, we are able to reuse modelcounting query results even for queries with different bounds.



Figure 1: Architecture of Cashew

3 CONSTRAINT CACHING

Our tool Cashew, depicted in Figure 1, is designed to work with a wide range of model-counting solvers to support quantitative program analyses. Algorithm 1 outlines how Cashew handles model-counting queries. Cashew expects a query of the form (F, V, b), where *F* is a well-formed formula, *V* is a set of variables in *F*, and *b* is a bound. The answer to the query, denoted as #(F, V, b), is the number of satisfying solutions for *F* for the variables in *V* within the bound *b*. We normalize the formula, variable(s) and bound using our normalization procedure, NORMALIZE-QUERY, which is described in the following sections. The resulting normalized query is denoted as $\llbracket F, V, b \rrbracket$ = NORMALIZE-QUERY(*F*, *V*, *b*).

Depending on the capabilities of the selected model-counting constraint solver, $[\![F, V, b]\!]$ is queried differently. Algorithm 1 outlines the normalization and query process. Typical model-counting constraint solvers [16, 37, 51], return a single count value (#(F, v, b)) after receiving a query of the form (F, V, b). For such solvers, our caching algorithm first sends the query $[\![F, V, b]\!]$ to the cache store. If there is a cache hit, the result is returned to the client. If not, the normalized query is sent to the model-counting solver, and the result is stored under $[\![F, V, b]\!]$ and returned to the client.

We call a model-counting constraint solver *paramaterized* if it returns a model-counter object that can be used to compute the number of satisfying solutions for an arbitrary bound. ABC [6] is a parameterized model-counting constraint solver where the model-counter object is the transfer matrix of an automaton that accepts all satisfying models of the given constraint. SMC [39] and barvinok [54] are also parameterized model-counting constraint solvers where the model-counter object is a generating function.

For parameterized solvers, the store is queried as follows: First, $\llbracket F, V, b \rrbracket$ is queried. On a hit, the result (#(F, V, b)) is returned to the client. In the case of a miss, an additional query for $\llbracket F, V \rrbracket$ is made. If this results in a hit, the model-counter object for $\llbracket F, V \rrbracket$ is recovered from the store. This model-counter object is sent to the model-counter evaluator which evaluates #(F, V, b) based on $\llbracket b \rrbracket$. The result returned by the model-counter evaluator is stored under $\llbracket F, V, b \rrbracket$ and is returned to the client. If both queries are misses, the selected solver is called, the model-counter object is computed and cached under the key $\llbracket F, V, b \rrbracket$, and #(F, V, b) is evaluated based on $\llbracket b \rrbracket$, stored under $\llbracket F, V, b \rrbracket$ and returned to the client.

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In order to use Cashew's parameterized caching functionality and reuse cached model-counter objects, a service that is able to take a model-counter object (such as a transfer matrix or a generating function) and evaluate it for a particular bound is required. This service is referred to as the model-counter evaluator.

Algorithm 1 CONSTRAINT-CACHING(*F*, *V*, *b*):

Input: A query (*F*, *V*, *b*).

Output: The number of satisfying solutions of V in F under the length bound b.

- 1: $\llbracket F, V, b \rrbracket$ = Normalize-Query(F, V, b)
- 2: if Hit on [[F, V, b]] then
- 3: return #(F,V,b)
- 4: end if
- 5: if Hit on [F, V] then
- Evaluate the model-counter object for bound [[b]] using the model-counter evaluator:
- 7: **Store** the result under $\llbracket F, V, b \rrbracket$
- 8: return #(F,v,b)
- 9: end if
- 10: Translate [F, V, b]] and send it to the selected model-counting solver
- 11: **Store** the returned model-counter object under [[F, V]]
- 12: **Store** #(F,V,b) under [[F, V, b]]
- 13: **return** #(*F*,*V*,*b*)

4 GROUP-THEORETIC FRAMEWORK

The goal of normalization is to reduce constraints equivalent under some property to the same form. This objective is shared by work in constraint programming, where detecting symmetries in constraints leads to a more efficient search [18, 19, 25]. Symmetrybreaking for constraint programming is expressed using concepts from group theory [3, 26, 49], a formalization we find fitting and intuitive for our purposes and adopt.

Our framework provides a means for constructing normal forms of constraints based on groups of property-preserving transformations. For different analysis problems, it might be necessary to preserve the entire solution set, the cardinality of the solution set, or only the satisfiability of constraints, each corresponding to a different level of normalization. Our framework is equally applicable, regardless of the desired level of normalization. Our framework is also not restricted to a constraint language, but is equally applicable to any background theory on which a group of property-preserving transformations can be defined.

Symmetry Groups. A group (\mathcal{G} , op) is a set of elements together with a binary operator that satisfies the four group axioms: closure, associativity, identity, and invertibility. For example, the set of all transpositions on the natural numbers, \mathbb{N} , under the binary operator function composition form a group. The transposition from \mathbb{N} to itself defined by the relation {(1, 2), (2, 1)} is an example of an element of this group which maps 1 to 2, 2 to 1 and all other elements of \mathbb{N} to themselves.

A subset of a group is called a *subgroup* if it also forms a group under the same binary operator. We construct the group of cardinality-preserving transformations under composition (\mathcal{G}_{card} , \circ) by introducing its generating subgroups. As composition is the only binary operator we consider, we simply refer to this group as \mathcal{G}_{card} throughout the remainder of the paper.

Solution-Set-Preserving Subgroups of \mathcal{G}_{card} . A solution-set-preserving transformation is one under which the solution set is mapped

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to itself. Any solution-set-preserving transformation is trivially cardinality-preserving. Each generating subgroup acts on a particular domain related to some feature of a constraint. The first generating subgroup we introduce acts on I, the domain of all possible indices of conjuncts in a constraint. Here, we consider the index of a conjunct to be its position in that constraint when read from left-to-right, making I simply the set of natural numbers. The subgroup acting on I is the group mentioned previously — that of all transpositions on \mathbb{N} or identically, the permutation group whose elements fix all but a finite number of numbers.

Intuitively, this subgroup captures our understanding that the solution set of a constraint is independent of the order of the conjuncts in it. Under the transposition $\{(1, 2), (2, 1)\}$, for example, the formula $x > 0 \land y < 0$ is mapped to $y < 0 \land x > 0$, making the two orderings equivalent modulo the action of this group.

Our second solution-set-preserving subgroup is the transposition group acting on \mathbb{V} , the infinite domain of all allowable variable names. Since the solution set of a constraint is independent of the choice of variable names, two constraints that are equivalent modulo the action of this group have the same solution set. As a simple example, realize that both *w* and *x* are elements of \mathbb{V} and that the number of solutions for $x < 7 \land x > 2$ is the same as that of its mapping under the relation $\{(x, w), (w, x)\}: w < 7 \land w > 2$.

Cardinality-Preserving Subgroups of \mathcal{G}_{card} . Preserving only the cardinality of the solution set of a constraint enables the use of subgroups with less constrained group actions. Under these groups, the solution set of a constraint is bijectively mapped to the solution set of another constraint, leaving the number of solutions unchanged.

Our first family of cardinality-preserving subgroups are given by the Euclidean groups E(n) (symmetry groups on Euclidean space) acting on the solution space of linear integer arithmetic constraints. The elements of these groups are Euclidean motions such as translations, rotations and indirect isometries such as reflection. Under these symmetries of Euclidean space, the volume captured by the corresponding polytope remains unchanged.

Though this volume is preserved under any action of the Euclidean group, some actions impact the number of lattice points in the polytope. Because we are often interested in the number of integer solutions to a constraint, we limit ourselves to considering only those transformations that preserve the number of lattice points as well as those that can be easily reflected through changes in the syntax of the constraint. In particular, our normalization scheme uses the subgroup of integral translations in Euclidean space as a generating subgroup for \mathcal{G}_{card} . Integral translations can be reflected syntactically in integer constraints through changes in the constant terms of each conjunct. Each constant term must be identically shifted by an integral amount. For example, shifting each constant term of the constraint $x + y = 2 \land x \ge 0 \land y \ge 0$ by 2 results in the constraint $x + y = 4 \land x \ge 2 \land y \ge 2$ which has the same number of integer solutions (6) as the original.

For any arithmetic constraint, F, the *shift* of F, denoted **Shift**(F), is the vector composed of the constant terms of each of its conjuncts. SH denotes the domain of all possible shifts. The subgroup of integral translations thus acts on SH. For string or mixed constraints, we do not apply transformations from this subgroup and we say that **Shift**(F) of such constraints is \emptyset .

Our second cardinality-preserving subgroup is given by the permutation group on the string alphabet, Σ . The solution set of a string constraint can be canonically represented by an automaton that accepts exactly the set of solutions to that constraint. Transitions between states are made based on a set of allowed alphabet symbols. Permuting the alphabet symbols thus changes the strings accepted by that automaton but not the cardinality of the accepted set. As a simple example, the number of solutions of the constraints F := x.contains("ac") and F' := x.contains("bd") is the same.

Orbits under the Symmetry Group \mathcal{G}_{card} . These subgroups generate \mathcal{G}_{card} in the following sense: the domain of any element of \mathcal{G}_{card} is the union of the domains of the subgroups, making it the Cartesian product $I \times \mathbb{V} \times S\mathcal{H} \times \Sigma$. Every element of a subgroup acts as an element of \mathcal{G}_{card} by acting as the identity on every domain element on which it is not defined. Any element of \mathcal{G}_{card} can be written as a composition of elements from these subgroups.

For a constraint *F*, the **orbit** of *F* under \mathcal{G}_{card} is the set of constraints obtained by applying any element $\sigma \in \mathcal{G}_{card}$ to *F*.

The problem of choosing a normalized form for *F* can now be formulated as choosing a representative constraint from the orbit of *F* under \mathcal{G}_{card} . We do this by defining a strict ordering on constraints and choosing the well-defined lowest ordered constraint within the orbit as the representative for all constraints within the orbit.

While we have spoken generally about cardinality-preserving group actions, our application of interest is in *parameterized* modelcounting which involves finding the number of satisfying solutions to a constraint for any given bound. While most of the group actions defined above preserve the number of solutions for a given bound, the elements of the Euclidean group may not. For example, $x + y = 2 \land x \ge 0 \land y \ge 0$ has 6 solutions given a bound of 2 but $x + y = 4 \land x \ge 2 \land y \ge 2$, which is in the same orbit under \mathcal{G}_{card} , has only one solution for the same bound. In order to preserve the parameterized model count, the bound is translated according to the same group action as the constraint. In the example above, bound 2 is translated to bound 4 by the same integer translation (2) that translated the shift, resulting in 6 satisfying models.

In a similar vein, it's interesting to note that though not all of our transformations preserve the solution set of a constraint, all of them are invertible. This means that the solution set of a constraint can be obtained from the solution set of its normal form by applying the inverse transformations of those applied to Σ and SH when normalizing the constraint to the solution set of its normal form. This enables our transformations to be used even for analyses that require the solution sets of constraints.

5 CONSTRAINT LANGUAGE

We focus on constraints over *strings* and *linear integer arithmetic*. We define three types of terms: string terms \mathcal{T}_S , regular expression terms \mathcal{T}_R , and LIA terms \mathcal{T}_A , as described in Figure 2. We consider three types of constraints over these terms, which we call *conjuncts* throughout this paper: string conjuncts S, regular membership conjuncts R, and LIA conjuncts A. The conjuncts are built using comparators as described in Figure 3. L is a language defined over these conjuncts. Input constraints to our normalization procedure are assumed to be in conjunctive form, with each conjunct from L.

$$\begin{split} \mathcal{T}_{S} &:= c \mid v_{S} \mid \mathcal{T}_{S} \cdot \mathcal{T}_{S} \mid char_at(\mathcal{T}_{S}, \mathcal{T}_{A}) \mid int_to_str(\mathcal{T}_{A}) \mid \\ replace(\mathcal{T}_{S}, \mathcal{T}_{S}, \mathcal{T}_{S}) \mid substr(\mathcal{T}_{S}, \mathcal{T}_{A}, \mathcal{T}_{A}) \\ \mathcal{T}_{R} &:= \epsilon \mid s \mid (\mathcal{T}_{R}) \mid \mathcal{T}_{R} \cdot \mathcal{T}_{R} \mid \mathcal{T}_{R} \mid \mathcal{T}_{R} \mid \mathcal{T}_{R}^{*} \\ \mathcal{T}_{A} &:= n \mid v_{A} \mid -\mathcal{T}_{A} \mid (\mathcal{T}_{A}) \mid \mathcal{T}_{A} + \mathcal{T}_{A} \mid \mathcal{T}_{A} - \mathcal{T}_{A} \mid \mathcal{T}_{A} \times n \mid \\ n \times \mathcal{T}_{A} \mid |\mathcal{T}_{S}| \mid index_of(\mathcal{T}_{S}, \mathcal{T}_{S}) \mid str_to_int(\mathcal{T}_{S}) \end{split}$$

Figure 2: Here $c \in \Sigma$, $n \in \mathbb{Z}$, $s \in \Sigma^*$, v_S and v_A denote an unbounded string variable and an integer variable, resp.

$$\begin{split} \mathsf{L} &\coloneqq \top \mid \bot \mid \mathsf{S} \mid \mathsf{R} \mid \mathsf{A} \\ \mathsf{S} &\coloneqq \mathcal{T}_{\mathsf{S}} = \mathcal{T}_{\mathsf{S}} \mid \mathcal{T}_{\mathsf{S}} \neq \mathcal{T}_{\mathsf{S}} \mid \mathsf{contains}(\mathcal{T}_{\mathsf{S}}, \mathcal{T}_{\mathsf{S}}) \mid \mathsf{prefix_of}(\mathcal{T}_{\mathsf{S}}, \mathcal{T}_{\mathsf{S}}) \mid \\ & \mathsf{suffix_of}(\mathcal{T}_{\mathsf{S}}, \mathcal{T}_{\mathsf{S}}) \mid \mathsf{not_contains}(\mathcal{T}_{\mathsf{S}}, \mathcal{T}_{\mathsf{S}}) \mid \\ & \mathsf{not_prefix_of}(\mathcal{T}_{\mathsf{S}}, \mathcal{T}_{\mathsf{S}}) \mid \mathsf{not_suffix_of}(\mathcal{T}_{\mathsf{S}}, \mathcal{T}_{\mathsf{S}}) \mid \\ \mathsf{R} \coloneqq \mathcal{T}_{\mathsf{S}} \in \mathcal{T}_{\mathsf{R}} \mid \mathcal{T}_{\mathsf{S}} \notin \mathcal{T}_{\mathsf{R}} \\ \mathsf{A} \coloneqq \mathcal{T}_{\mathsf{A}} = \mathcal{T}_{\mathsf{A}} \mid \mathcal{T}_{\mathsf{A}} < \mathcal{T}_{\mathsf{A}} \mid \mathcal{T}_{\mathsf{A}} \leq \mathcal{T}_{\mathsf{A}} \mid \mathcal{T}_{\mathsf{A}} \neq \mathcal{T}_{\mathsf{A}} \end{split}$$

Figure 3: The language L: conjuncts of string (S), regular expression (R) and LIA (A) types.

Let S_{op} be the set of string operators, i.e. the operators used to build the \mathcal{T}_S terms. Let S_{comp} be the set of string comparators, i.e. the comparator used to build S conjuncts. Similarly, let R_{op} be the set of regular expression operators used in \mathcal{T}_R ; R_{comp} – the set of regular expression comparators used in R; A_{op} – the set of the LIA operators used in \mathcal{T}_A ; and A_{comp} – the set of LIA comparators used in A. Let a function TYPE:S $\cup R \cup A - > S_{comp} \cup R_{comp} \cup A_{comp}$ be a function that takes in a conjunct and returns the comparator of this conjunct.

6 CONSTRAINT ORDERING

Assume a strict total ordering on constraints, \prec . A constraint *F* is a normal form if for every other constraint *F'* in its orbit under \mathcal{G}_{card} , $F \prec F'$. There are many ways to impose an ordering on constraints. We present one possible ordering below.

Our ordering is produced compositionally, with strict orders defined over various components of our language which are composed to yield an ordering on constraints. To start, we define an ordering on each element of the domain of \mathcal{G}_{card} .

The ordering on both \mathbb{V} and Σ is lexicographical. The ordering on \mathcal{I} is that induced by the natural numbers. We define the ordering on \mathcal{SH} , the domain of constant shifts, after we introduce an ordering on vectors. We consider vectors over strict totally ordered sets and denote by \prec_{vec} an order on such vectors.

Let *X* be a strict totally ordered set, and \prec_X be a strict total order on *X*. Let $\boldsymbol{v} = (v_0, \ldots, v_n)$ and $\boldsymbol{u} = (u_0, \ldots, u_m)$ be two vectors over *X*, then \prec_{vec} is defined as:

$$\boldsymbol{\upsilon} \prec_{\boldsymbol{\upsilon}ec} \boldsymbol{u} \Longleftrightarrow \begin{cases} m < n, \text{ or} \\ m = n, \exists i \forall j : j < i < n, \upsilon_j = u_j, \upsilon_i \prec_X u_i \end{cases}$$

This defines ordering on \mathcal{SH} since shift vectors are built over integer constants.

Our normalization procedure relies on the following auxiliary functions that given a constraint return, as vectors, various structural and syntactic components characterizing the constraint. These vectors are built over the domains of \mathbb{V} , Σ and \mathbb{Z} , i.e. over strict totally ordered sets.

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VI(F) – returns *a vector of the indices of variables* as they occur in *F* relative to other variables, constants and operators. The indices are compared according to the "<" operator over \mathbb{Z} .

Int(F) – returns *a vector of integer constants* occurring in F from left to right, ignoring all elements of **Shift**(F). The vectors are compared according to the "<" operator on \mathbb{Z} .

 $\mathbf{V}(F)$ — returns *a vector of variable names* occurring in *F* from left to right. These vectors are compared according to the lexicographical order on \mathbb{V} .

 $\Sigma(F)$ — returns *a vector of string characters* occurring in *F* from left to right. The vectors are compared according to the lexicographical order on Σ .

Next, we define strict total orderings on operators and (separately on) comparators, listing them in the order of the increasing precedence. Both operators and comparators, are ordered with precedence to S, then R, and A.

- Sop: •, the rest of the string operators in the lexicographic order according to their names in Figure 2;
- R_{op}: ordered according to the standard precedence order on regular expression operators;
- A_{op}: +,-, ×, ||, (), the rest of the LIA operators in the lexicographic order according to their names in Figure 2.
- S_{comp}: =, ≠, the rest of the string comparators in the lexicographic order according to their names in Figure 3;
- $R_{comp}: \in, \notin;$
- $\mathsf{A}_{comp} \colon =, <, \leq, \neq;$

The ordering on comparators allows to define an order \prec_{type} on the types of the conjuncts Type, based on the type of the comparator occurring in the conjuncts. The strict total ordering on operators allows to introduce *vectors of operators* of constraints and compare them with \prec_{vec} :

Op(F) - a vector of string, regular and LIA operators occurring in *F* from left to right.

Note all auxiliary vectors and their orderings introduced in this section are defined for constraints and are naturally applicable to conjuncts – as to a special type of constraints with a single conjunct.

In the future, when we compare two elements of the same type we will drop the subscript notation and use \prec to represent comparison between them.

We are now ready to build a strict total order on conjuncts. We define the ordering hierarchically: the structural or syntactic aspects of the conjuncts are compared one at a time in a fixed order, until a tie-breaking aspect is found. This order can be selected in any way. We present one intuitive order below to distinguish conjuncts with more significant differences as early as possible. The conjuncts are first compared based on their type TYPE, then based on their length || ||, then the total number of variables #Var, then their vectors of operators *Op*, followed by the vectors of indices of variables *VI*, their vectors of integer coefficients *Int*, their vectors of variable names V, then vectors of string constants Σ , and finally based on their constant shifts *Shift*. This order is described in Algorithm 2.

This order is strict and total. Two conjuncts are equal if and only if they are the same conjunct. This allows us to extend the ordering to constraints as follows:

(i) Order constraints based on their total number of conjuncts.

Algorithm 2 C-LESSTHAN(C_1, C_2): Conjunct Comparison

| Input: Two conjuncts $C_1, C_2 \in L$ |
|---|
| Output: True if $C_1 \prec C_2$, otherwise FALSE |
| 1: for each $f \in [Type, , #Var, Op, VI, Int, V, \Sigma, Shift]$ do |
| 2: if $f(C_1) \prec f(C_2)$ then |
| 3: return True |
| 4: end if |
| 5: end for |
| 6: return False |

- (ii) Then order constraints by comparing their conjuncts elementwise according to the order imposed on *I*. This is equivalent to comparing conjuncts pairwise from first to last.
- (iii) A constraint F is lower ordered than a constraint G if the first differing conjunct of F is lower ordered than that of G.

This order is described in Algorithm 3.

Algorithm 3 F-LESSTHAN(F, G): Constraint Comparison

| Input: Two constraints $F = F_1 \land \ldots \land F_m$ and $G = G_1 \land \ldots \land G_n$ |
|---|
| Output: True if $F \prec G$, otherwise FALSE |
| 1: if $m = n$ then |
| 2: for $i \leftarrow 1$, n do |
| 3: if C-LESSTHAN(F_i , G_i) then |
| 4: return True |
| 5: end if |
| 6: end for |
| 7: end if |
| 8: return $m < n$ |
| |

7 NORMALIZATION PROCEDURE

The normal form of a constraint *F* is the lowest constraint in the orbit of *F* under \mathcal{G}_{card} . In this section, we present a normalization procedure to find the normal form of a constraint.

Given a transformation $\sigma \in \mathcal{G}_{card}$, we define $\sigma[F]$, the *action of* σ *on* F, as a composition of elements of four categories corresponding to each of the components of the domain of \mathcal{G}_{card} :

 $I: \sigma_I[F]$ gives the constraint resulting from re-ordering the conjuncts of *F* according to σ_I .

 \mathbb{V} : $\sigma_{\mathbb{V}}[F]$ gives the constraint resulting from renaming the variables of *F* according to $\sigma_{\mathbb{V}}$;

 Σ : σ_{Σ} [F] gives the constraint resulting from permuting the alphabet constants in *F* according to σ_{Σ} ;

SH: $\sigma_{SH}[F]$ gives the constraint resulting from shifting each element of *F*'s shift according to σ_{SH} .

We first present an expensive but complete procedure for normalization in Algorithm 4 and give guarantees for its termination and correctness. Given a constraint F, this procedure probes each permutation F' of conjuncts in F, building and applying a composite σ from transformations specific to the domains \mathbb{V} , Σ , and SHwhich reduces F' until the only transformations that can reduce it further involve an action on I. The results among all permutations of F are compared and the lowest-ordered result is chosen as the normal form of F.

The procedure uses auxiliary functions to build the minimizing domain-specific transformations:

MIN- σ - $\mathbb{V}(F')$ constructs $\sigma_{\mathbb{V}}$ compositionally — it proceeds through the conjuncts of F' from left to right renaming the variables of F'

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in order of appearance. Each time a new variable is encountered a transposition is added to the composition that permutes the name of the encountered variable and the lowest-ordered variable name that no other variable of F' has been renamed to yet. At the start of the procedure, σ_V is initialized to the identity transposition on \mathbb{V} .

MIN- σ - $\Sigma(F')$ similarly constructs σ_{Σ} — it proceeds through the conjuncts of F' from left to right, this time permuting string characters. Each time a new string character is encountered, a transposition is added to the composition that permutes the encountered string character with the lowest-ordered character that no other character in F' has been mapped to yet. σ_{Σ} is initialized as the identity transposition on Σ .

MIN- σ -SH(F') returns σ_{SH} — the transformation on Shift(F) that translates the constant coefficient of the first appearing (from left to right) linear integer arithmetic conjunct in F' to 0. If F contains variables that are shared between string and LIA constraints, σ_{SH} is the identity transformation.

| Alg | orithm 4 Complete-Normalization(F) | |
|--------------|---|--|
| Inpu Outr | it: A constraint <i>F</i> put: The normalized form of <i>F</i> | |
| 1: I | $F_{min} := F$ | |
| 2: f | For each permutation F' of conjuncts in F do | |
| 3: | $\sigma_{\mathbb{V}} := M_{\text{IN}} - \sigma - \mathbb{V}(F')$ | |
| 4: | $\sigma_{\Sigma} := \operatorname{Min} \sigma - \Sigma(F')$ | |
| 5: | $\sigma_{\mathcal{SH}} := \operatorname{Min} \sigma - \mathcal{SH}(F')$ | |
| 6: | $F' := \sigma_{\mathbb{V}} \circ \sigma_{\Sigma} \circ \sigma_{\mathcal{SH}}[F']$ | |
| 7: | if F-LessThan (F', F_{min}) then | |
| 8: | $F_{min} := F'$ | |
| 9: | end if | |
| 10: e | end for | |
| 11: r | eturn F _{min} | |

THEOREM 7.1. Algorithm 4 terminates.

PROOF. Given a constraint F, there are finitely many permutations of conjuncts F'. Consequently, there are finitely many executions of the "for each" loop. Construction of each permutation F' is linear in the length of F. Construction of each of the domain-specific transformations within a single "for each" call is performed in a single pass through the conjuncts of F', thus, is linear in the length of F, too. The final transformation on F' is also linear in the length of F. Thus, COMPLETE-NORMALIZATION terminates.

THEOREM 7.2. Algorithm 4 returns the normal form of F.

PROOF. Assume G = COMPLETE-NORMALIZATION(F) is not the normal form of F. Then either G is not in the orbit of F under $\mathcal{G}_{\text{card}}$ or there is some constraint H in the orbit of F such that $H \neq F$ and $F \not\prec H$. We show that both result in a contradiction.

Assume *G* is not in the orbit of *F*. *G* is the result of permuting the conjuncts of *F*, the action of some σ_I , composed with domain specific transformations. Each domain-specific transformation has an inverse in \mathcal{G}_{card} as does any permutation of the conjuncts of *F*. Therefore, there exists some σ in \mathcal{G}_{card} such that $\sigma[G] = F$.

Now assume that there is some *H* in the orbit of *F* such that $H \neq G$ and $G \not\prec H$. The order of conjuncts in *H* is given by some transposition of the indices of *F*. This means that there is some iteration of the for loop of Algorithm 4 in which the conjuncts of

the considered permutation of *F* are ordered identically to those of *H*. By construction, our choices of $\sigma_{\mathbb{V}}$, σ_{Σ} and $\sigma_{S\mathcal{H}}$ reduce this constraint to the lowest-ordered constraint that maintains the same ordering of conjuncts. Therefore either G = H or $G \prec H$.

Algorithm 4 gives a normalization procedure which is *sound* (each orbit has at least one fixed point) and *complete* (there is exactly one fixed point for each orbit). In practice, however, such a brute force exploration is very expensive. For our implementation, we use a sound but not complete normalization procedure given in Algorithm 5. Given *F*, NORMALIZATION(*F*) returns the semi-normal form on F — a constraint within the orbit of *F* which, though not necessarily the lowest in the orbit, is not higher ordered than *F*.

Algorithm 5 simplifies COMPLETE-NORMALIZATION procedure in that instead of brute-forcing all permutations of conjuncts in F, it inexpensively chooses a permutation by ordering the conjuncts of Faccording to C-LESSTHAN up to the point when further refinement involves comparison over the domains \mathbb{V} , Σ , or SH. In other words, the conjuncts are not compared according to their variable names, string constants or shifts. It is possible that two conjuncts in Fare equal by this comparison, in which case their initial order in F is preserved. The resulting permutation of conjuncts defines a transposition on I. We apply this transposition to F, resulting in a constraint F'. $\sigma_{\mathbb{V}}$, σ_{Σ} , and σ_{SH} are generated by the same auxiliary functions as in Algorithm 4, composed, and applied to F'. The result is the semi-normal form of F.

| Algorithm 5 Normalization(F) |
|---|
| Input: A constraint <i>F</i> Dutput: A semi-normal form of <i>F</i> |
| 1: $F' := \mathbf{Permute}$ conjuncts of F according to Algorithm 2 up until \mathbf{V} 2: $\sigma_{\mathcal{V}} := M_{\mathbb{N}} \cdot \sigma \cdot \mathbb{V}(F')$ 3: $\sigma_{\mathcal{\Sigma}} := M_{\mathbb{N}} \cdot \sigma \cdot \mathcal{\Sigma}(F')$ 4: $\sigma_{\mathcal{S}\mathcal{H}} := M_{\mathbb{N}} \cdot \sigma \cdot \mathcal{S}\mathcal{H}(F')$ 5: $[\![F]\!] := \sigma_{\mathbb{V}} \circ \sigma_{\Sigma} \circ \sigma_{\mathcal{S}\mathcal{H}}[F']$ 6: $\mathbf{return} [\![F]\!]$ |
| THEOREM 7.3 Algorithm 5 is sound |

THEOREM 7.3. Algorithm 5 is sound.

PROOF. Each action on *F* is the action of an element of \mathcal{G}_{card} . By definition, the resulting formula is in the orbit of *F* under \mathcal{G}_{card} .

The procedure given in Algorithm 5 is not complete. There are orbits for which not every constraint is reduced to the same form. Though this potentially increases the number of misses to the cache, our experimental results demonstrate the large number of formulas mapped to the same semi-normal form by Algorithm 5.

Queries to Cashew are of the form (F, V, b) where V is the set of variables on which to count, and b is the maximum length of a satisfying solution. To ensure that the cardinality of the solution set is preserved after normalizing F, both V and b must be normalized according to the same transformations applied to F during Algorithm 5. Algorithm NORMALIZE-QUERY(F, V, b) implements this query normalization.

8 EXPERIMENTAL EVALUATION

We implemented our tool, Cashew, as an extension of the Green [55] caching framework. This allows Cashew to use any of the existing Green services, and it allows Green users to benefit from our normalization procedure. We experiment with Cashew-enabled satisfiability and model-counting services, which support string

| Algorithm 6 Normalize-(| Duery(| <i>F</i> , | V, | <i>b</i>) | |
|-------------------------|--------|------------|----|------------|--|
|-------------------------|--------|------------|----|------------|--|

Input: A query (F, V, b)Output: A normalized query $\llbracket F, V, b \rrbracket$ 1: $\llbracket F \rrbracket := \text{NORMALIZATION}(F)$ 2: $\sigma :=$ the transformation used to normalize F3: $\llbracket V \rrbracket := \sigma[V]$ 4: $\llbracket b \rrbracket := \sigma[b]$ 5: return ($\llbracket F \rrbracket, \llbracket V \rrbracket, \llbracket b \rrbracket$)

constraints and linear integer arithmetic. They also support *mixed* constraints, i.e., those involving both string and arithmetic operations. In this evaluation, we used ABC [6] as our constraint solver. As we explained in Section 3, other model-counting constraint solvers can be integrated instead of ABC.

All the experiments were run on an Intel Core i7-6850 3.5 GHz computer running Linux 4.4.0. The machine has 128 GB RAM, of which 4 GB were allocated for the Java VM.

8.1 Model Counting over the SMC/Kaluza String Constraint Dataset

The Kaluza dataset is a well-known benchmark of string constraints that are generated by dynamic symbolic execution of real-world JavaScript applications [47]. The authors of the SMC solver [39] translated the satisfiable constraints to their input format: one contains 1,342 big, while the other contains 17,554 small where big and small classification is done based on the constraint sizes in the Kaluza dataset. We shall refer to the former as the original SMC-Big and to the latter as the original SMC-Small.

Duplicate Constraints. While inspecting the results of our normalization, we found out that many of the files within each dataset are identical (indistinguishable by diff). Due to the presence of duplicates, even trivial caching (without any normalization) will yield some benefit on the original datasets. After removing all duplicate files, only 359 of the 1,342 constraints in SMC-Big and 9,745 of the 17,554 constraints in SMC-Small were found to be unique. As we discuss below, our normalization procedure allows further reductions in this dataset, increasing the benefits of caching well beyond what can be achieved with trivial caching.

Model Counting. Since these constraints correspond to path conditions from symbolic execution, counting the number of satisfying models of each one could be necessary for quantitative analysis. We model-counted all constraints in each set as a simple way to emulate the behavioral pattern (w.r.t. caching) of one or more users performing quantitative analyses on the original programs.

When counting the models of a constraint over strings, to avoid infinite counts one needs to set a bound on the length of strings. In this experiment, we set the bound to 50 characters for both sets. We model-counted each constraint in the dataset. We first did this without normalization or caching, and then again with Cashew normalization and caching. In non-caching mode, each constraint was sent unmodified to the model-counting solver. In caching mode, the cache was cleared before running SMC-Big, and again before running SMC-Small. Since these path constraints were produced by an external symbolic executor, in this experiment we did not use SPF. Note that since all constraints were model-counted, the order in which we traverse the datasets does not matter: each normalized

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| SMC-Big | | | | | | | | : | SMC-Sr | nall | | | | | | | | | | | |
|---------|-----|----|----|----|----|----|-------|------|--------|------|-----|-----|----------|-----|-----|-----|-----|------|-----|---|---|
| | | | 42 | 42 | 4 | 10 | 40 | | | 197 | 5 | 10 | 74 | 10 | 120 | | | | | | |
| | 253 | | 40 | 39 | 3 | 8 | 38 | 2543 | 2543 | 107: | 5 | 10 | 74 | | 120 | | | | | | |
| | | | 39 | 38 | 36 | 36 | 35 | | | | | | 736 | 399 | 345 | 323 | 216 | ; | | | |
| | 00 | | | | | _ | _ | | | | | | | | | | 374 | 1951 | 152 | Γ | Γ |
| | 99 | 43 | 39 | 38 | 34 | 28 | 27 | 2537 | | 729 | 374 | 186 | | Ē | Ш | | | | | | |
| | 00 | | | | | 2 | 7 13 | | | | 3/4 | 168 | 73 | 躙 | 鼺 | | | | | | |
| | 99 | | 39 | 37 | 32 | 1 | 5 6 5 | | | 445 | 371 | 155 | 72 57 | | | | | | | | |

Figure 4: Orbit sizes for the original SMC datasets.

Table 1: Model counting SMC-Big and SMC-Small.

| 0.82 s | 10.00v |
|---------------|--|
| 04 s 0.82 s | 10.00 |
| | 10.90X |
| 2 s 40.13 s | 3.03x |
| 5 s 293.21 s | 10.94x |
| 2 s 0.05 s | 2.40x |
| 9 s 1.12 s | 0.97x |
| 9 s 552.56 s | 2.19x |
| 32 s 0.26 s | 89.70x |
| 2 s 40.13 s | 3.03x |
| 00 s 358.17 s | 87.38x |
| .3 s 0.05 s | 2.60x |
| 9 s 1.12 s | 0.97x |
| 01 s 971.50 s | 2.29x |
| | $\begin{array}{cccc} & & & & & & & & & & & & & & & & & $ |

constraint will fall within some orbit, and for each orbit, the full cost will be paid exactly once (first cache miss).

Results. Table 1 shows the total, maximum and average modelcounting time, as well as the speedups obtained by Cashew on each of these metrics, for the two datasets with and without duplicates. On the SMC-Big set, Cashew achieved a speedup over 10x. On the SMC-Small set, which is a rather bad case for the caching tradeoff because it contains a large number of very small constraints, Cashew still achieved a 2.19x speedup.

For the original datasets, these numbers (e.g., a 87x speedup) are largely due to the presence of duplicates, which makes even caching with no normalization very effective. We report the results because the original datasets are widely used, and because the duplicates might indeed have been genuinely generated by symbolic execution of various different (yet similar) JavaScript programs.

Figure 4 depicts the effect of our normalization procedure on the original benchmarks. The area of each orbit is proportional to its size. Labels indicating orbit size are shown only when they fit in the available space. For the original SMC-Small set, the 17,554 original constraints are reduced to 360 orbits. For the SMC-Big set, the 1,342 original constraints are reduced to just 34 orbits.

We do not compare Cashew with Green because the original Green (without Cashew) cannot handle string constraints.

Note that the largest constraint in SMC-Small takes slightly more time after normalization. We cannot infer much from this, because the largest constraint in SMC-Small barely takes one second; the small difference (about 30 msec) could be due to noise. However, the maximum time for SMC-Big decreased by 3x with caching enabled, from 122 to 40 seconds. This is due to normalization. The constraint that (without normalization) requires maximum time to be model-counted falls within some orbit. It does not matter which constraint in that orbit will be the one to cause a cache miss once T. Brennan, N. Tsiskaridze, N. Rosner, S. Aydin, and T. Bultan

Table 2: Effect of transformations on orbit refinement.

| Transformations enabled | #Orbits (SMC-Big) | #Orbits (SMC-Small) |
|----------------------------------|-------------------|---------------------|
| None | 359 | 9754 |
| All transformations | 34 | 360 |
| All except σ_I | 72 | 376 |
| All except $\sigma_{\mathbb{V}}$ | 344 | 9645 |
| All except σ_{Σ} | 35 | 841 |
| All except removeVar | 34 | 361 |
| All except removeConj | 40 | 386 |

caching is enabled — only one of them will, and as they are all normalized to the same normal form, any of them would take the same model-counting time. What is interesting is that said time can be significantly smaller than the maximum pre-normalization time.

Table 2 shows the number of orbits that are achieved by different subsets of the transformations in our normalization procedure. Since some transformations can benefit from others, instead of considering them in isolation, we measured the effect of disabling each one. We did not include σ_{SH} as it doesn't apply to the string domain. The removeVar and removeConj transformations are preprocessing steps that remove redundant variables and conjuncts, respectively. These results indicate that all transformations yield some benefit, and that σ_V is the most beneficial transformation. For SMC-Small, removing σ_{Σ} more than doubles the number of orbits. The same is true of σ_I for SMC-Small. This shows that different transformations can be more effective for different datasets.

8.2 SPF Analysis of String-Handling Code

In this second part of the experimental evaluation we use Symbolic PathFinder [42] with Cashew, to symbolically execute Java programs that operate on strings. In order to support model-countingbased quantitative analyses, we are interested in obtaining a model count for each leaf path constraint.

As an example of quantitative information flow analysis, we study some possible applications of Cashew to side-channel analysis. We consider four Java programs in which a side channel can allow an attacker to gain information about a hidden secret. PasswordCheck1 contains a method that checks whether or not a user-given string matches a secret password. Due to the way the program is written, the attacker can deduce that the longer the program executes, the longer a prefix of the hidden password was matched. PasswordCheck2 is another variant that attempts to mitigate that vulnerability by requiring a certain number of characters to be compared before returning, even if a mismatch has already been found. This yields a more interesting side channel, which can still be exploited but is much noisier and less predictable. Obscure is a Java translation of the obscure.c program used in [39], which is a password change authorizer. Given an old password and a new one, Obscure performs a series of tests to determine whether the new password is different enough from the old one. CRIME is a Java version of a well-known attack, Compression Ratio Info-leak Made *Easy* [9, 46]. This is a side channel in space - the secret is concatenated with a string that can be controlled by the attacker, and both are compressed together before encryption. Thus, the attacker can try various strings and observe the changes in the size of the compressed payload to infer, from the compression rate, the level of similarity between the secret and the injected content.

1.243 s

2.158 s

1.965 s

3.005 s

2,941 s

1,067 s

609 s

Cashew

Cashew

Cashew

None No norm

None No norm

Obscure

CRIME

| Program | Caching | Total time | Speedup | #Hits | #Misses | H/M |
|-----------|---------|------------|---------|--------|---------|------|
| Password1 | None | 297 s | - | - | - | - |
| | No norm | 258 s | 1.15x | 17,547 | 56,173 | 0.31 |
| | Cashew | 106 s | 2.80x | 62,797 | 10,923 | 5.75 |
| Password2 | None | 3,364 s | - | - | - | - |
| | No norm | 3,379 s | 0.99x | 30,448 | 824,832 | 0.04 |

2.71x

1.10x

3.54x

1.02x

2.82x

659.804

2.000

44,893

31 884

78,289

195.476

59.000

16,107

84.127

37,722

3.38

0.03

2.79

0.38

2.08

Table 3: SPF-based quantitative analyses of string programs.

In symbolic execution, it is not always desirable to make all arguments of a method symbolic. This is often the case due to scalability issues. It can also be due to the need to explore a nonstandard distribution of some parameter. Consider, for instance, a situation where a list of passwords from a website is unwillingly disclosed to the public. As a consequence, users are strongly encouraged to change their passwords, and an algorithm similar to the Obscure program is employed to ensure that they are sufficiently different from the stolen ones. We might be interested in measuring the amount of leakage of the algorithm over that particular list of passwords. By running SPF on Obscure with the new password as a symbolic string, and the old password as a concrete string, we can measure the leakage for that particular stolen password. By repeating this for various passwords from the list, we can quantify the algorithm's leakage for that list's particular distribution. Doing so requires running SPF repeatedly on the same code, but with different secret strings. This will affect many path conditions in fundamental ways, but others might be unaffected, or changed in such a way that Cashew can still normalize them down to a previously seen one.

RockYou. The RockYou1K dataset is a sample of 1,000 real-world passwords taken from the RockYou leak [56] without duplicates. The sample consists of 1,000 unique passwords that cover all lengths between 6 and 16 characters, and can include any ASCII symbols.

Results. For each of the four programs under analysis, we ran 1,000 symbolic-execution-based side-channel analyses, using as the secret each of the 1,000 passwords in the RockYou1K dataset. For PasswordCheck1 and PasswordCheck2, the secret is the password, which is concrete, and the user's guess is a symbolic string. For Obscure, the roles are reversed: what we made concrete is the old password, which is no longer secret, whereas the user-chosen new password (which is secret) is symbolic. For CRIME, we used a concrete secret (session ID) and a symbolic user-injected payload.

Table 3 shows execution time, hits and misses for three execution modes. The first mode uses neither normalization nor caching. In the second mode, only caching without normalization is performed, which measures the extent to which syntactically identical path conditions (akin to the duplicates mentioned in Section 8.1) are generated. In the third mode, Cashew's normalization is enabled. Note that each symbolic execution generates many path conditions. The tables show the aggregated results over all path conditions of each execution and the 1,000 executions of each mode. As in the previous section, we do not compare Cashew with Green in ESEC/FSE'17, September 4-8, 2017, Paderborn, Germany

Table 4: Cashew normalization and caching costs.

| | Total | Total | Total | Total | Average | Total |
|-----------|------------|----------|-------|---------|---------|--------|
| | time | time | norm. | norm. | norm. | cache |
| | (no cache) | (Cashew) | time | calls | time | size |
| SMC-Big | 3,209 s | 293 s | <3 s | 359 | 8 ms | 54 KB |
| SMC-Small | 1,211 s | 553 s | 31 s | 9,745 | 3 ms | 104 KB |
| Password1 | 297 s | 106 s | 20 s | 73,720 | 275 µs | 2.9 MB |
| Password2 | 3,364 s | 1,243 s | 94 s | 855,280 | 110 µs | 58 MB |
| Obscure | 2,158 s | 609 s | 19 s | 61,000 | 300 µs | 5.1 MB |
| CRIME | 3,005 s | 1,067 s | 47 s | 116,011 | 400 µs | 8.8 MB |

these experiments because the original Green (without Cashew) cannot handle string constraints. The results show that, for these experimental subjects, Cashew achieved an average speedup of nearly 3x, while caching without normalization only achieved 1.06x (and, for PasswordCheck2, was in fact slower than no caching). The hit/miss ratios improve dramatically when switching to Cashew.

Costs of Caching and Normalization. A caching scheme involves overheads and space/time trade-offs. Normalization overhead must be kept low, since its cost must be paid not only for each hit, but also for each miss. Cache size must also be kept within reasonable limits. Cashew is implemented on top of Green and, like Green, uses the in-memory Redis [1] database by default. This allows extremely fast queries, but competes with the client application for available RAM. As Table 4 shows, the average time to normalize a constraint in our SPF symbolic execution experiments was only a few hundred microseconds. It was about 8 milliseconds for the largest formulas (the SMC-Big set, with an average size before normalization of about 10 KB of text per constraint). Finally, as shown in Table 4, the total cache memory usage was very reasonable for these experiments.

8.3 Parameterized Caching

In this last part of the experimental evaluation we present some experiments for evaluating parameterized caching—that is, caching that leverages parameterized model-counting solvers.

The motivation behind these experiments is that users of Cashew who are targeting quantitative information analysis techniques often perform their analyses with various different bound values. For example, in side-channel analysis, one may want to compute the amount of information leakage for different lengths of a symbolic secret or input. This requires using different bounds when counting models. In scenarios where we have reason to believe that there is potential for reusing already-created model-counting objects for multiple values of *b*, we can try to amortize the time required to construct them by caching them.

String Constraints: SMC/Kaluza. Recall the SMC-Big and SMC-Small datasets from Section 8.1. We ran these two datasets several more times, starting with the string length bound *b* at 10 characters and raising it up to 100 characters. Since our goal was to evaluate the usefulness of caching model-counting objects, we did not clear the cache between successive values of *b*. Again, we did not compare with Green in these experiments because Green (without Cashew) does not support constraints over strings.

Figure 5 shows the cumulative time spent running SMC-Big and SMC-Small, respectively, for $b \in \{10, 20, 30, ..., 100\}$ characters. We did this twice for each dataset. The upper lines (red) correspond to



Figure 5: SMC datasets for increasing bounds. Cashew: nonparameterized (red) and parameterized (blue) caching.



Figure 6: Symbolic execution of sorting/searching programs for increasing bounds. Green (green) vs. Cashew (blue).

Cashew with parameterized caching disabled (model-counting objects are not cached). The lower lines (blue) correspond to Cashew with parameterized caching enabled. In this mode, an extra cost is paid to cache the model-counting objects, but doing so enables the possibility of reusing them later on. The left chart shows that caching model-counting objects is indeed beneficial for SMC-Big. This is an idealized amortization scenario, since all stored model-counting objects are reused on each successive bound value. Nevertheless, it is useful to confirm that for this dataset, running even one additional bound is profitable, and that this profit becomes larger each time we run the dataset for an additional value of *b*. The right chart shows a similar phenomenon for SMC-Small, but although the gap does increase, the lines are so close together that caching model-counting objects would probably not be worth its cost. This is consistent with a large number of small problems.

Arithmetic Constraints. The goal of these experiments is to evaluate the usefulness of Cashew's parameterized caching when symbolically executing Java code whose branch conditions involve linear integer arithmetic operations. Green can handle arithmetic constraints, so we can use it as the baseline for these experiments.

One well-known class of algorithms that involve integer arithmetic constraints and give rise to nontrivial path conditions are classical sorting algorithms. For these experiments we ran an SPF-based quantitative analysis (symbolic execution and model counting on complete path conditions) on the following algorithms: BubbleSort, InsertionSort, SelectionSort, QuickSort, HeapSort, and MergeSort.

Figure 6 shows the cumulative time spent in the analysis of each of the seven Java programs, for $b \in \{16, 20, 24, \dots 64\}$. Since

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we are counting over the integers, the bound b now denotes the maximum number of bits that may be used to represent an integer. We ran each series twice. The upper curve (green) corresponds to Green, with caching enabled, using its normalization procedure for integer arithmetic constraints. The lower curve (blue) corresponds to Cashew with parameterized caching enabled.

The magnitude of the gap between both curves varies for different programs. In most cases, the initial run on an empty cache (for b = 16) is slightly more costly for Cashew due to the overhead of having to store all the model-counting objects in the cache. This is compensated as soon as they are reused at least once, and in all cases we see that the gap between the curves grows as the model-counting objects are reused further. This confirms that parameterized caching is beneficial for these programs if there is a reasonable chance that the model-counting objects may be reused.

9 RELATED WORK

Our work builds on top of Green [55], an external framework for caching the results of calls to satisfiability solvers or model counters developed by Visser et al. Other caching frameworks include Green-Trie [31], an extension of Green and Recal [4], both of which are able to detect some implications between constraints. Recal transforms a LIA constraint to a matrix, canonizes it, and uses the result as the constraint's normal form. A different approach is taken by the tool Utopia [5] which identifies past satisfying solutions likely to be shared with new formulas. This enables results to be reused across formulas that share at least one solution, regardless of their structural resemblance.

Cashew differs notably from these previous caching frameworks. First, we present a parameterized model counting approach for quantitative program analysis which allows us to cache and reuse a model-counter object in addition to the results of model counting queries. This allows us to reuse results for model-counting queries across different bounds. Cashew also exploits more expressive normalization techniques with reductions that preserve only the *number* of solutions of a constraint instead of their solution set. This allows us to reuse information that the above caching frameworks can not. Cashew is also able to handle string constraints, a unique contribution amongst the above mentioned tools.

10 CONCLUSIONS

We presented a caching framework for quantitative program analysis built on constraint normalization techniques that preserve the cardinality of the solution set for a given constraint but not necessarily the solution set itself. We augmented our framework with parameterized constraint caching techniques that can reuse the result of a previous model counting query even if the bounds of the queries do not match and extended our framework to support string constraints and combinations of string and arithmetic constraints. Our experiments exemplify how, when supplemented with our constraint normalization techniques, constraint caching can significantly improve the performance of quantitative program analyses.

Table 5: Classes implementing each transformation

| Transformation | Class name |
|-----------------------|----------------------------|
| σ_I | OrderingService |
| $\sigma_{\mathbb{V}}$ | VariableRenamer |
| σ_{Σ} | AlphabetRenamer |
| removeVar | VariableRemover |
| removeConj | RedundantConstraintRemover |

11 IMPLEMENTATION

Cashew is built on top of Green, and like Green, it acts as a wrapper around constraint solvers and model counters. In other words, it sits between the client application (typically a verification tool based on constraint satisfiability and/or model counting) and the actual constraint solver and/or model counter. Besides the caching strategy and mechanism, it provides a standard interface for the client application to create constraints and request solving/counting services; this enables switching solvers without modifying the client.

Constraints for Cashew are constructed using the same class hierarchy as in Green; the main change is that we extended that hierarchy with new objects that represent operations on strings.

Cashew also inherits the storage abstraction from Green. The default store is a Redis database, but other back ends can be used.

11.1 Obtaining Cashew

Cashew can be obtained from the GitHub repository located at https://github.com/vlab-cs-ucsb/cashew/

11.2 Configuring Cashew

Cashew can be configured via key/value pairs, using the standard Java Properties mechanism. Each of the transformations shown in Table 2 is implemented by a class in the service.canonizer package, as shown in Table 5. Layers can be enabled and disabled, for both constraint satisfiability and model counting, by means of the green.service.sat and the green.service.count properties, respectively. As in the Green framework, these properties can specify a composition of services using a parenthesized syntax. Examples of this can be found in the sample configuration files included in the Cashew repository.

11.3 Cashew Integration Examples

A Model-Counting Tool for SMC/Kaluza Benchmark Problems. We used Cashew to implement a simple model counter for SMC/Kaluza constraints, as shown in Section 8.1, expressed using a subset of the SMT-LIB format [13].

This tool is essentially a translator that parses that input syntax, maps it to Cashew's constraint representation, and then invokes the model counter service. This implementation is included in the Cashew repository as RunCashewKaluza.java.

Cashew as a Back End for SPF. We also used Cashew as the back end for Symbolic PathFinder, as shown in Section 8.2. The integration of SPF with Cashew was done much in the same way as it was with Green: the SPF codebase is modified in the few places where it calls the constraint solver or model counter, so that it calls Cashew instead. A translator class is added in order to translate

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SPF's constraint language (i.e., abstract syntax tree class hierarchy) to Cashew's before making the call.

The Cashew repository includes a sample working version of SPF modified in this way.

Also, Cashew option configuration properties are read through the JPF configuration property space, which allows the user to control Cashew-specific behavior from the same . jpf configuration file used by JPF and SPF. Examples can be found in the sample configuration files included in the Cashew repository.

Cashew as a Back End for Your Own Tool. Cashew can be integrated with your client application just like Green; see the Green documentation and examples for more details.

If you would like to use string operations in your constraints, please see the Operation, StringConstant, and StringVariable classes in the green.expr package.

Adding Your Own Solver to Cashew. Cashew has already been integrated with the ABC constraint solver and model counter. You can add a new SMT solver to Cashew in the same way as you would add one to Green. At a minimum, you will need to write a translator from Cashew's constraint representation to your solver's input format. The simplest way to do this is to have your translator class extend the Visitor class in the green.expr package.

Adding a new model counter is done similarly as well, but in this case we augmented the interface to allow for storing model-counter objects. Besides the getModelCount method, Cashew also supports the getModelCounter method, which does not require a bound, and returns a model-counter object rather than a number, and the getModelCountUsingCounter method, which takes a model-counter object and a bound, and returns a number. You may want to implement these methods if your solver supports parameterized model counting. Model-counter objects are stored by Cashew as raw binary objects (byte[]), so they can contain anything.

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