

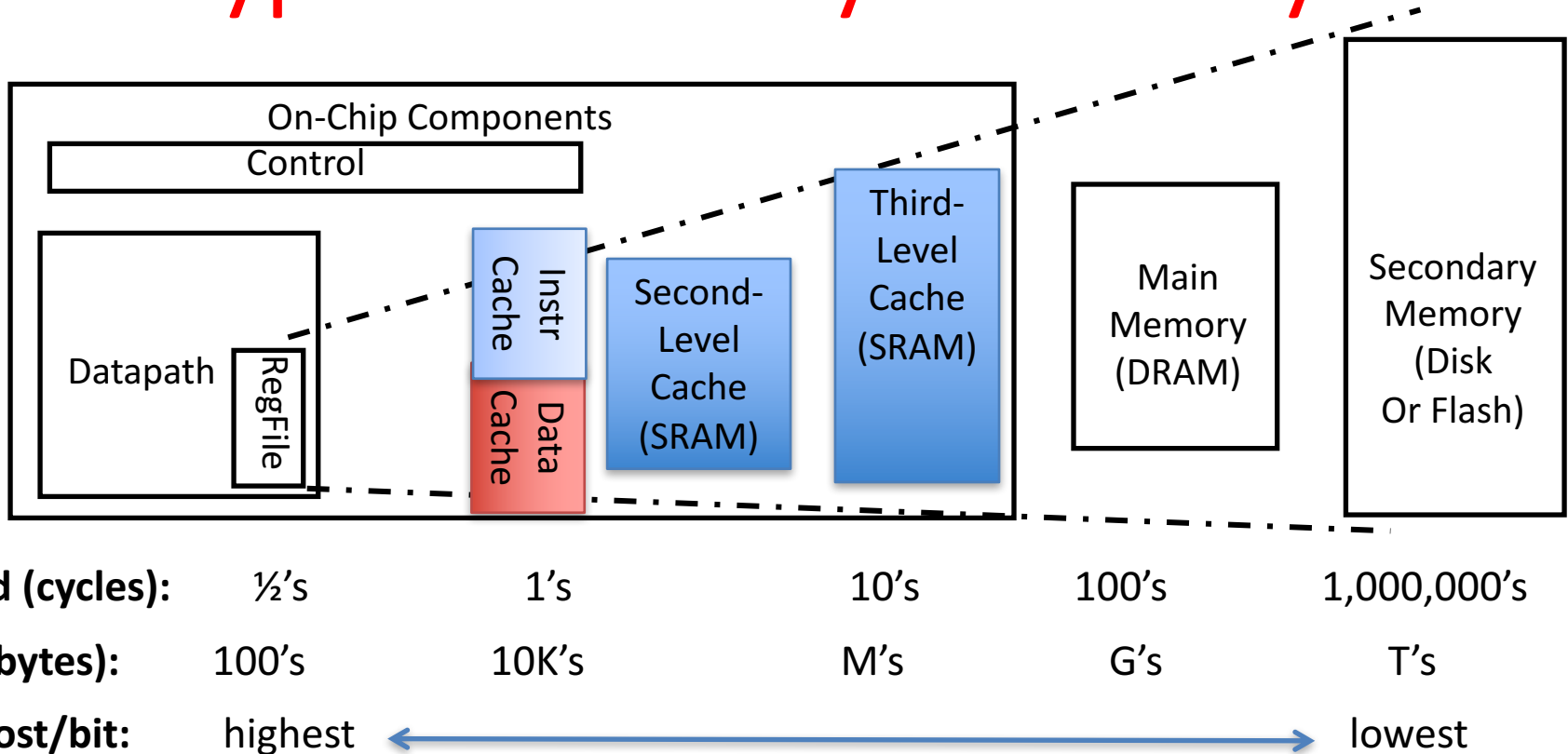
Caches and Memory Hierarchy: Review

UCSB CS240A, Fall 2017

Motivation

- Most applications in a single processor runs at only 10-20% of the processor peak
- Most of the single processor performance loss is in the memory system
 - Moving data takes much longer than arithmetic and logic
- Parallel computing with low single machine performance is not good enough.
 - Understand high performance computing and cost in a single machine setting
- Review of cache/memory hierarchy

Typical Memory Hierarchy



- **Principle of locality + memory hierarchy** presents programmer with \approx as much memory as is available in the *cheapest* technology at the \approx speed offered by the *fastest* technology

Idealized Uniprocessor Model

- Processor names bytes, words, etc. in its address space
 - These represent integers, floats, pointers, arrays, etc.
- Operations include
 - Read and write into very fast memory called registers
 - Arithmetic and other logical operations on registers
- Order specified by program
 - Read returns the most recently written data
 - Compiler and architecture translate high level expressions into “obvious” lower level instructions

$$A = B + C \Rightarrow$$

Read address(B) to R1

Read address(C) to R2

$R3 = R1 + R2$

Write R3 to Address(A)

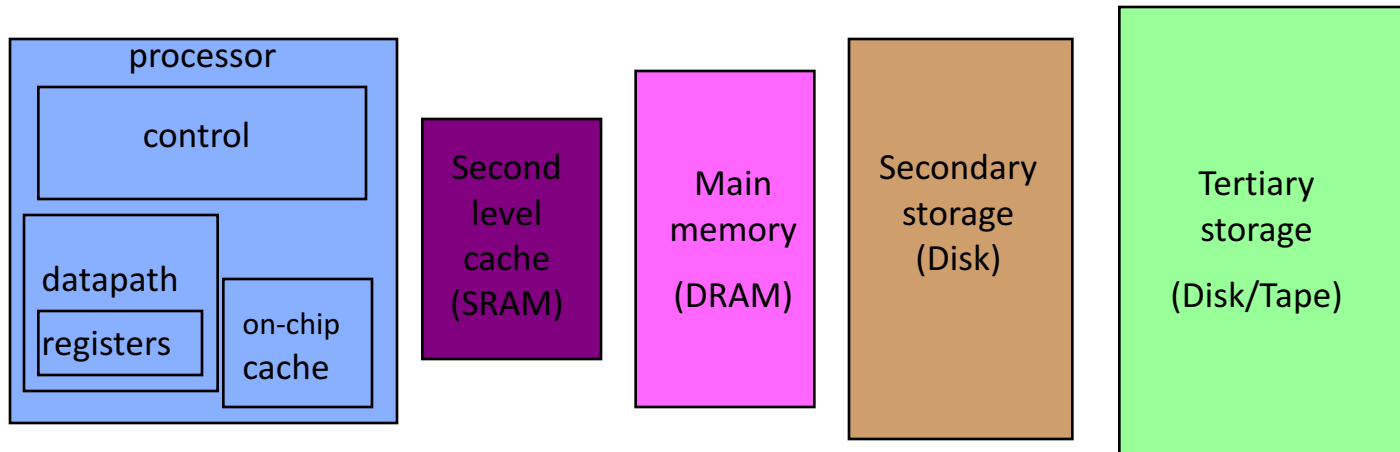
- Hardware executes instructions in order specified by compiler
- *Idealized Cost*
 - Each operation has roughly the same cost
(read, write, add, multiply, etc.)

Uniprocessors in the Real World

- **Real processors have**
 - **registers and caches**
 - small amounts of fast memory
 - store values of recently used or nearby data
 - different memory ops can have very different costs
 - **parallelism**
 - multiple “functional units” that can run in parallel
 - different orders, instruction mixes have different costs
 - **pipelining**
 - a form of parallelism, like an assembly line in a factory
- **Why is this your problem?**
 - In theory, compilers and hardware “understand” all this and can optimize your program; in practice they don’t.
 - They won’t know about a different algorithm that might be a much better “match” to the processor

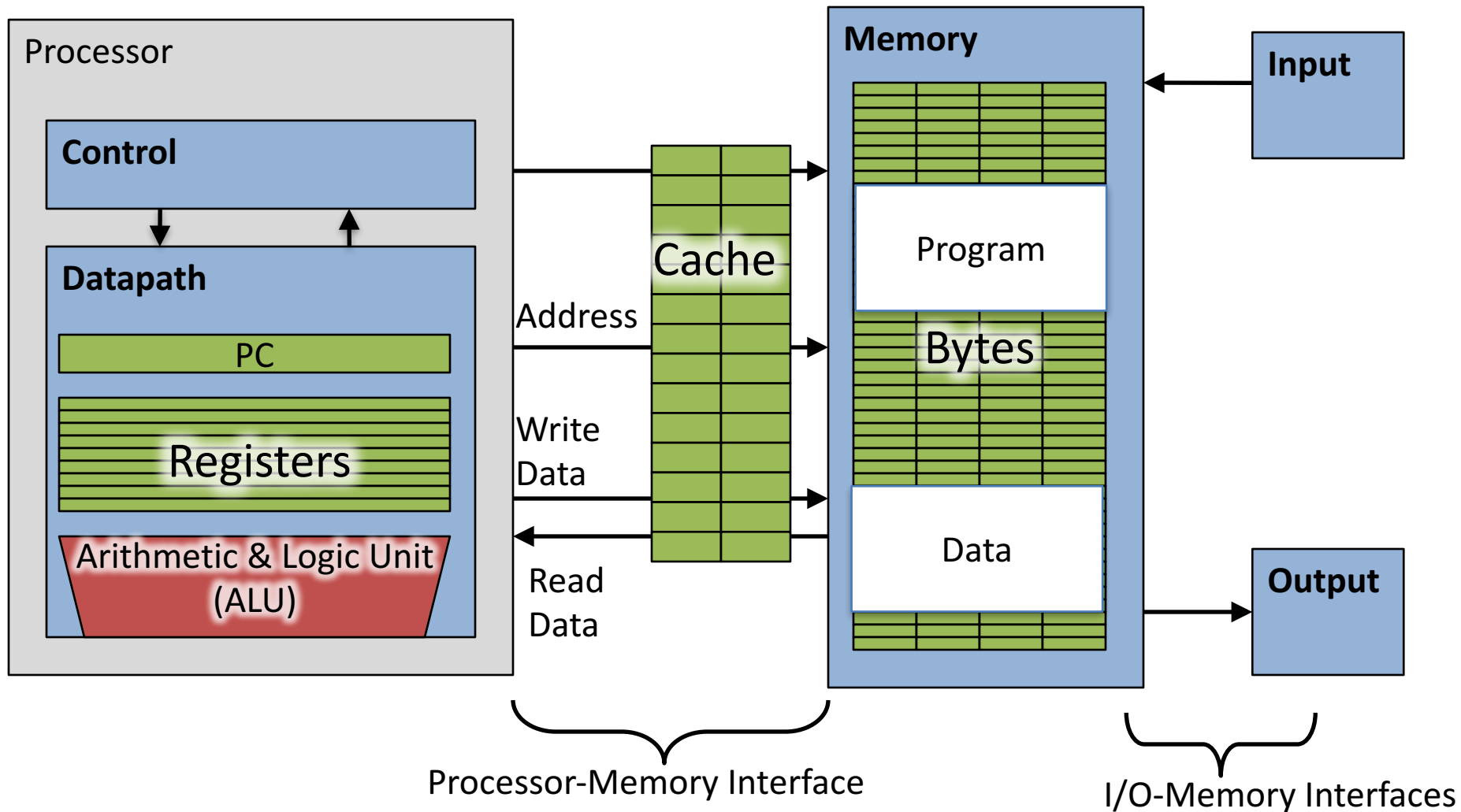
Memory Hierarchy

- Most programs have a high degree of **locality** in their accesses
 - **spatial locality**: accessing things nearby previous accesses
 - **temporal locality**: reusing an item that was previously accessed
- Memory hierarchy tries to exploit locality to improve average



| | | | | | |
|-------|-----|------|-------|--------|-------|
| Speed | 1ns | 10ns | 100ns | 1-10ms | 10sec |
| Size | KB | MB | GB | TB | PB |

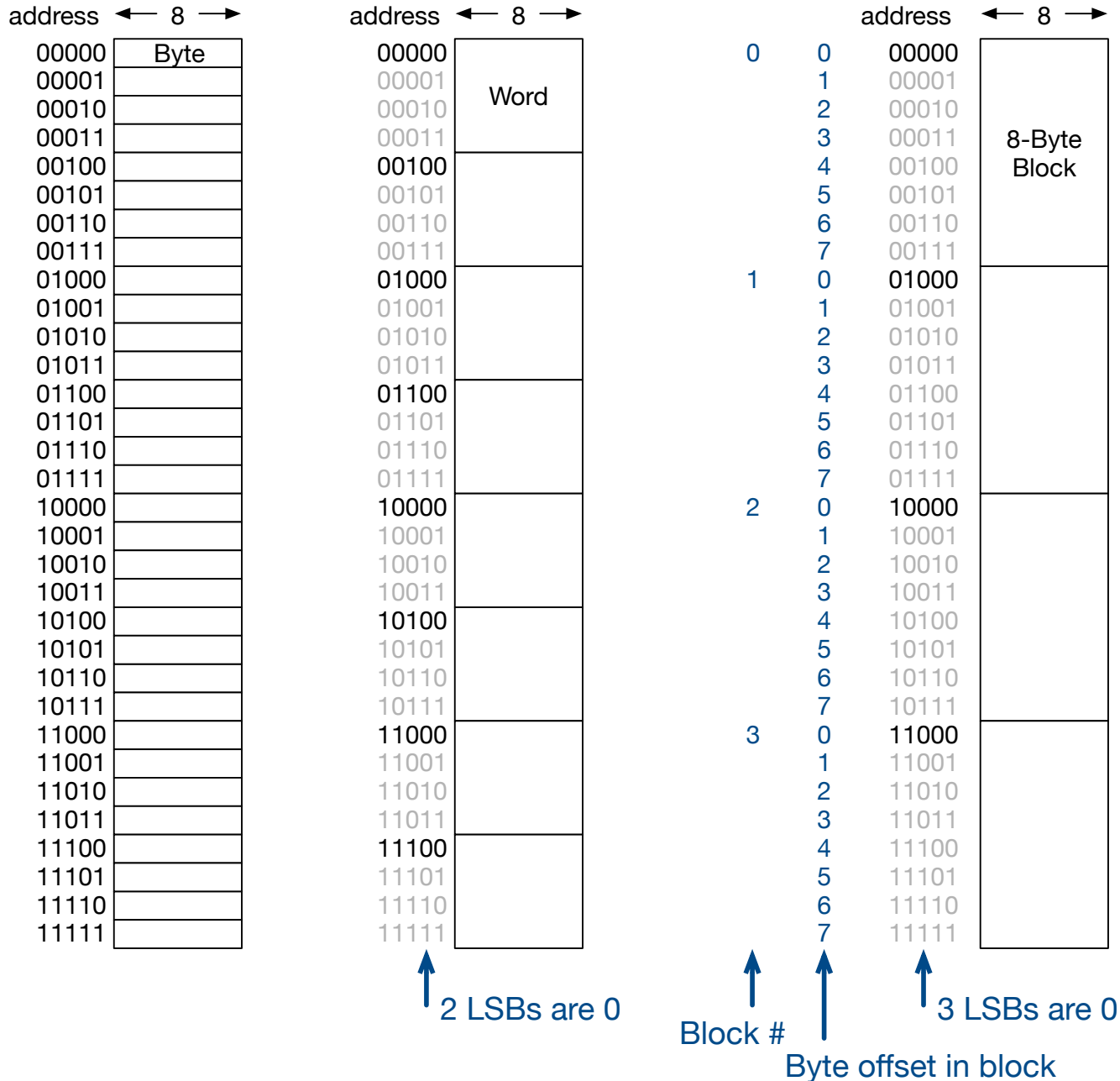
Review: Cache in Modern Computer Architecture



Cache Basics

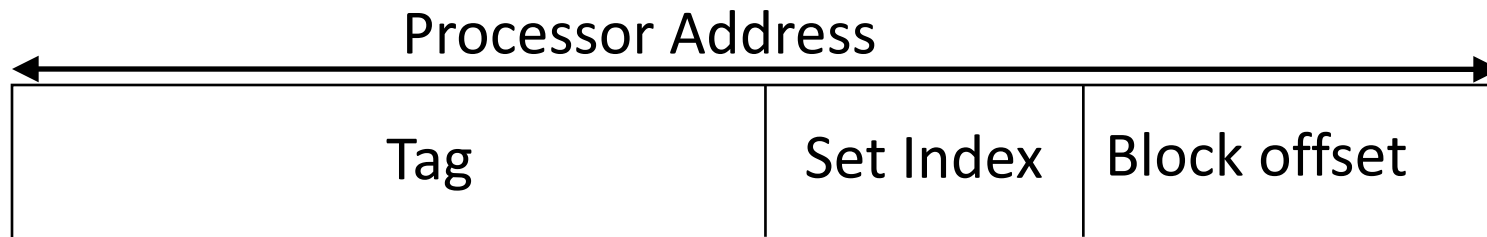
- **Cache is fast (expensive) memory which keeps copy of data in main memory; it is hidden from software**
 - Simplest example: data at memory address xxxxx1101 is stored at cache location 1101
- **Memory data is divided into blocks**
 - Cache access memory by a block (cache line)
 - Cache line length: # of bytes loaded together in one entry
- **Cache is divided by the number of sets**
 - A cache block can be hosted in one set.
- **Cache hit: in-cache memory access—cheap**
- **Cache miss: Need to access next, slower level of cache**

Memory Block-addressing example



Processor Address Fields used by Cache Controller

- **Block Offset:** Byte address within block
 - B is number of bytes per block
- **Set Index:** Selects which set. S is the number of sets
- **Tag:** Remaining portion of processor address



- Size of Tag = Address size – $\log(S)$ – $\log(B)$

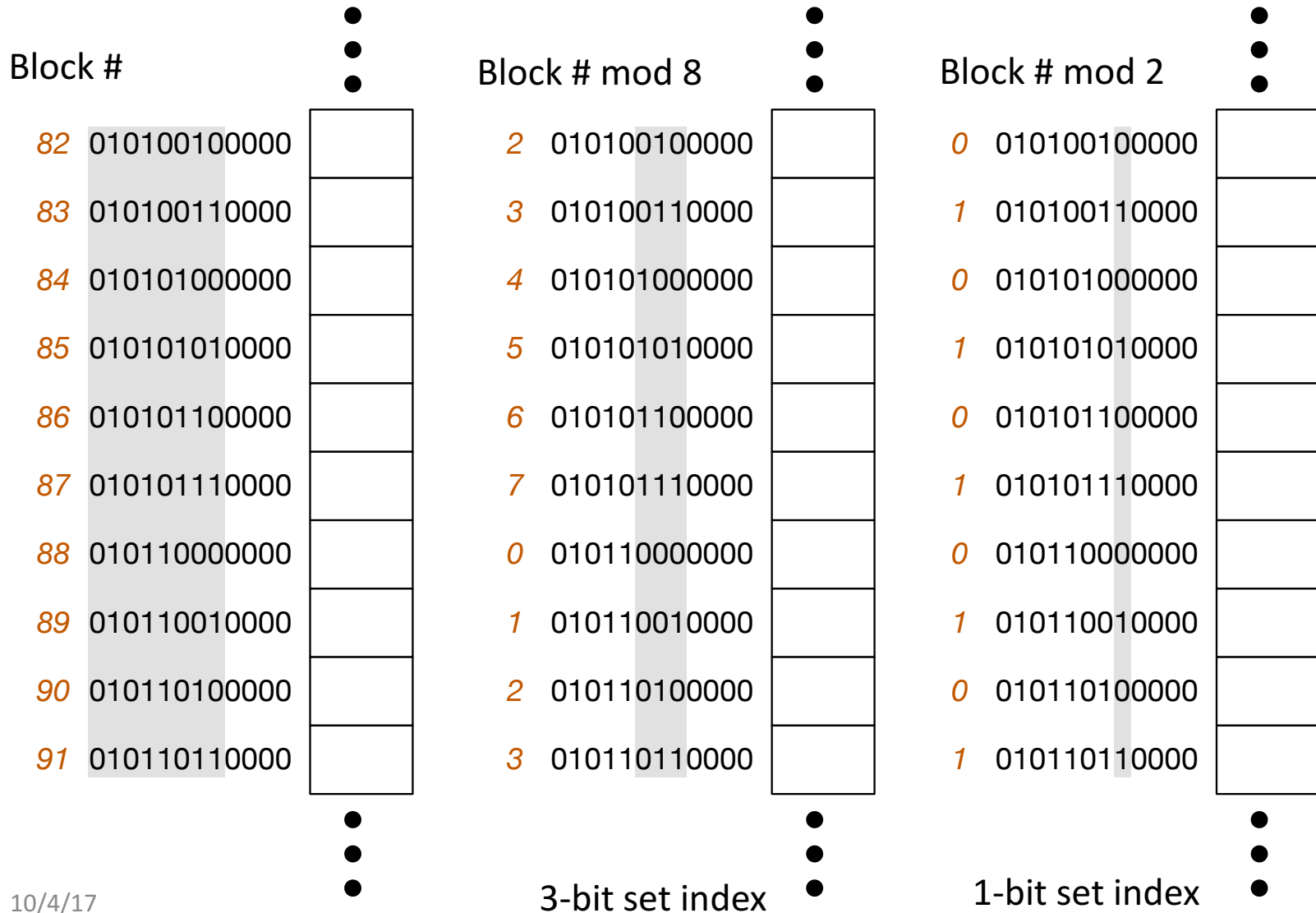
Cache Size C = Associativity N × # of Set S × Cache Block Size B

Example: Cache size 16K. 8 bytes as a block. → 2K blocks → If N=1, S=2K using 11 bits.

Associativity N represents # items that can be held per set

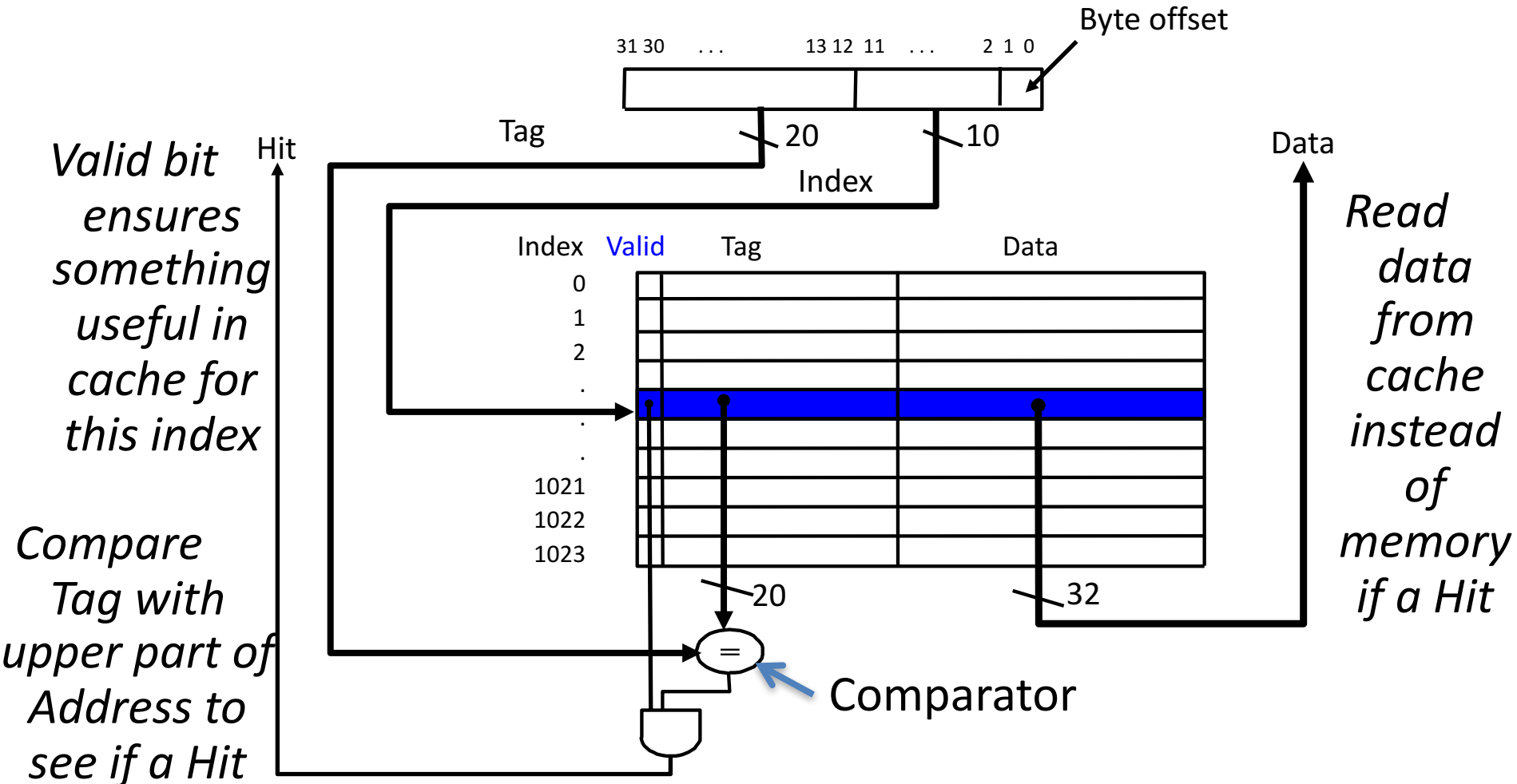
Block number aliasing example

12-bit memory addresses, 16 Byte blocks



Direct-Mapped Cache: $N=1$. $S=\text{Number of Blocks}=2^{10}$

- 4byte blocks, cache size = 1K words (or 4KB)

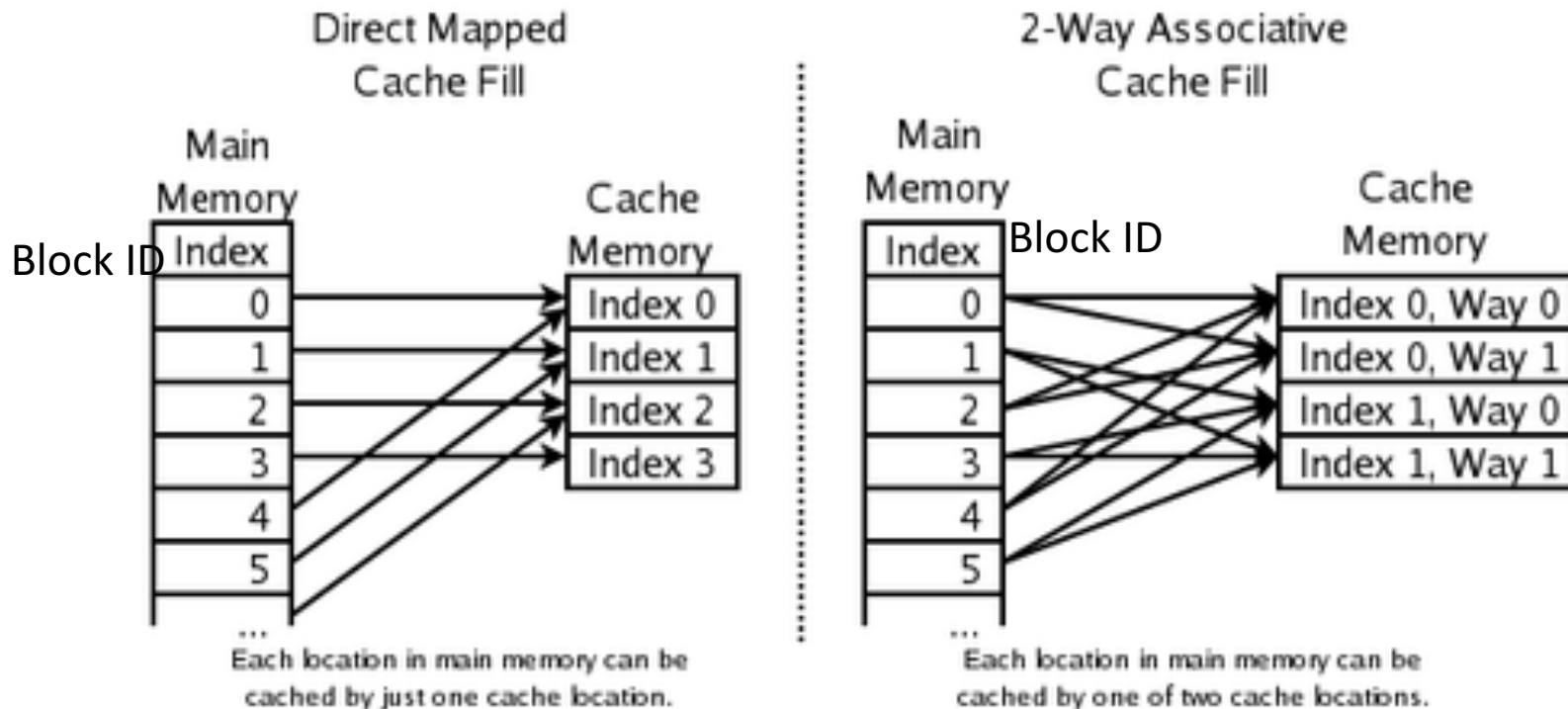


$$\text{Cache Size } C = \text{Associativity } N \times \text{\# of Set } S \times \text{Cache Block Size } B$$

Cache Organizations $Cache\ Size\ C = N \times \#\ of\ Set\ S \times Size\ B$

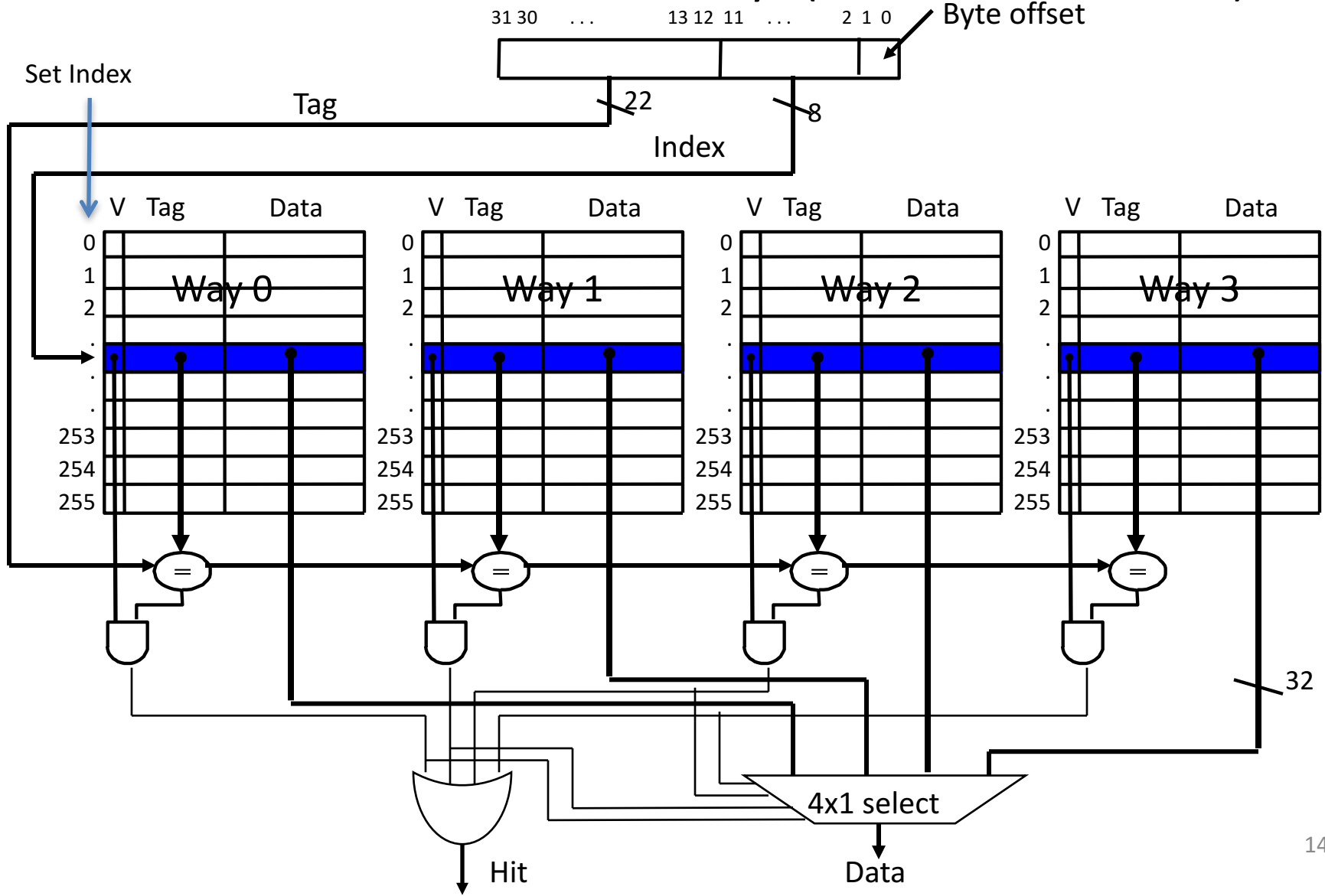
Associativity N represents # items that can be held per set

- “Fully Associative”: Block can go anywhere
 - $N =$ number of blocks. $S = 1$
- “Direct Mapped”: Block goes one place
 - $N = 1$. $S =$ cache capacity in terms of number of blocks
- “N-way Set Associative”: N places for a block



Four-Way Set-Associative Cache

- $2^8 = 256$ sets each with four ways (each with one block)



How to find if a data address in cache?

0b means binary number

- Assume block size 8 bytes → last 3 bits of address are offset.
- Set index 2 bits.
- Given address 0b1001011, where to find this item from cache?

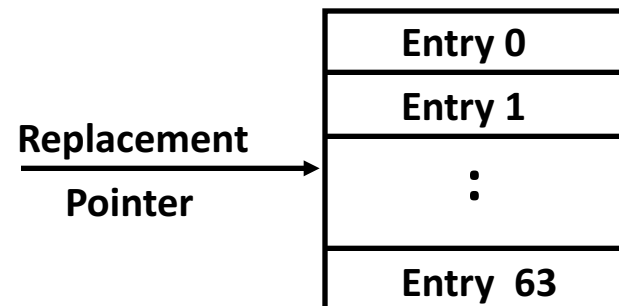
How to find if a data address in cache?

0b means binary number

- Assume block size 8 bytes → last 3 bits of address are offset.
- Set index 2 bits.
- 0b1001011 → Block number 0b1001.
- Set index 2 bits (mod 4)
 - Set number → 0b01.
- Tag = 0b10.
 - If directory based cache, only one block in set #1.
 - If 4 ways, there could be 4 blocks in set #1.
 - Use tag 0b10 to compare what is in the set.

Cache Replacement Policies

- **Random Replacement**
 - Hardware randomly selects a cache evict
- **Least-Recently Used**
 - Hardware keeps track of access history
 - Replace the entry that has not been used for the longest time
 - For 2-way set-associative cache, need one bit for LRU replacement
- **Example of a Simple “Pseudo” LRU Implementation**
 - Assume 64 Fully Associative entries
 - Hardware replacement pointer points to one cache entry
 - Whenever access is made to the entry the pointer points to:
 - Move the pointer to the next entry
 - Otherwise: do not move the pointer
 - (example of “not-most-recently used” replacement policy)

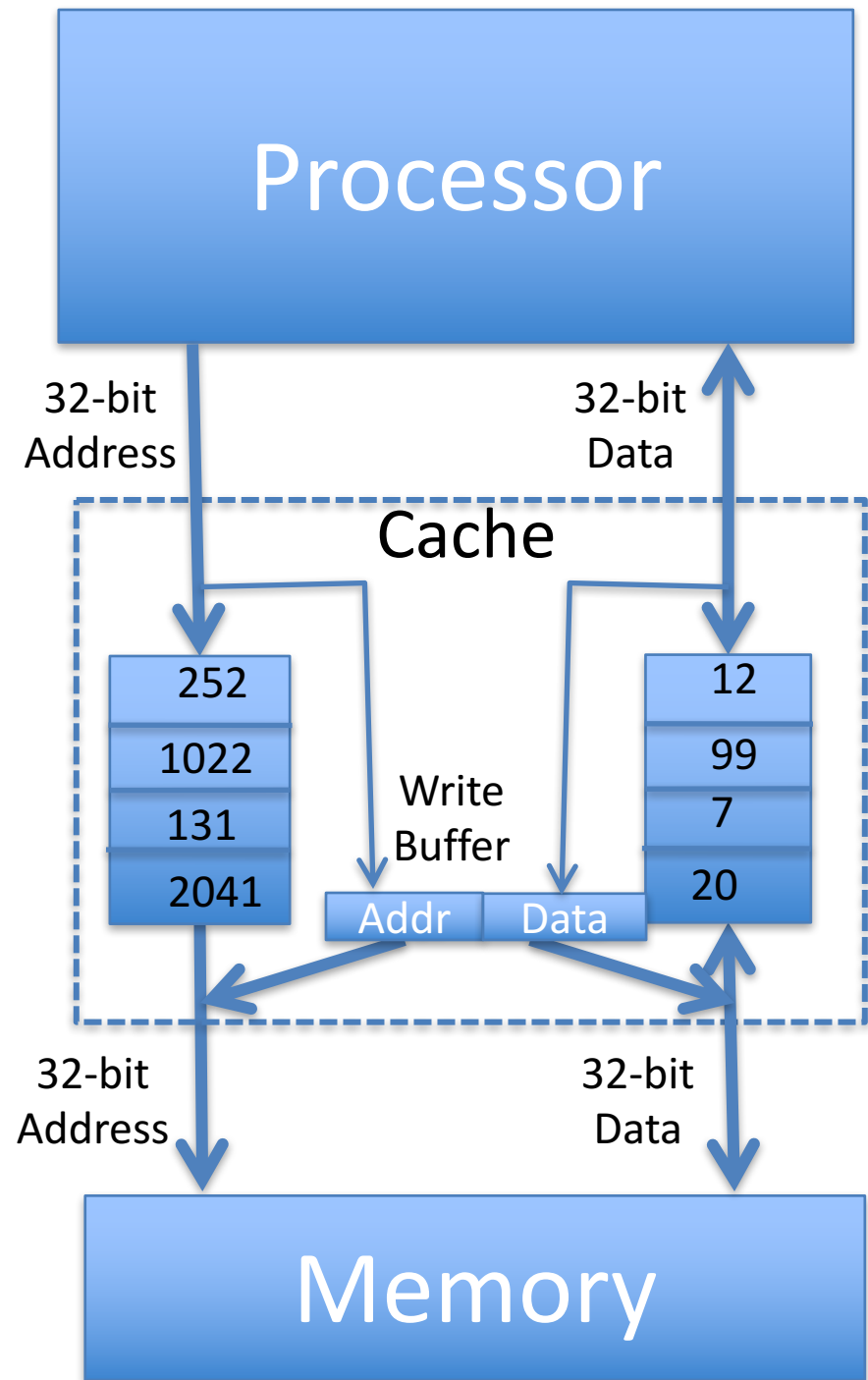


Handling Data Writing

- Store instructions write to memory, changing values
- Need to make sure cache and memory have same values on writes: 2 policies
 - 1) **Write-through policy**: write cache and write *through* the cache to memory
 - Every write eventually gets to memory
 - Too slow, so include Write Buffer to allow processor to continue once data in Buffer
 - Buffer updates memory in parallel to processor
 - 2) **Write-back policy**

Write-Through Cache

- Write both values in cache and in memory
- Write buffer stops CPU from stalling if memory cannot keep up
- Write buffer may have multiple entries to absorb bursts of writes
- What if store misses in cache?

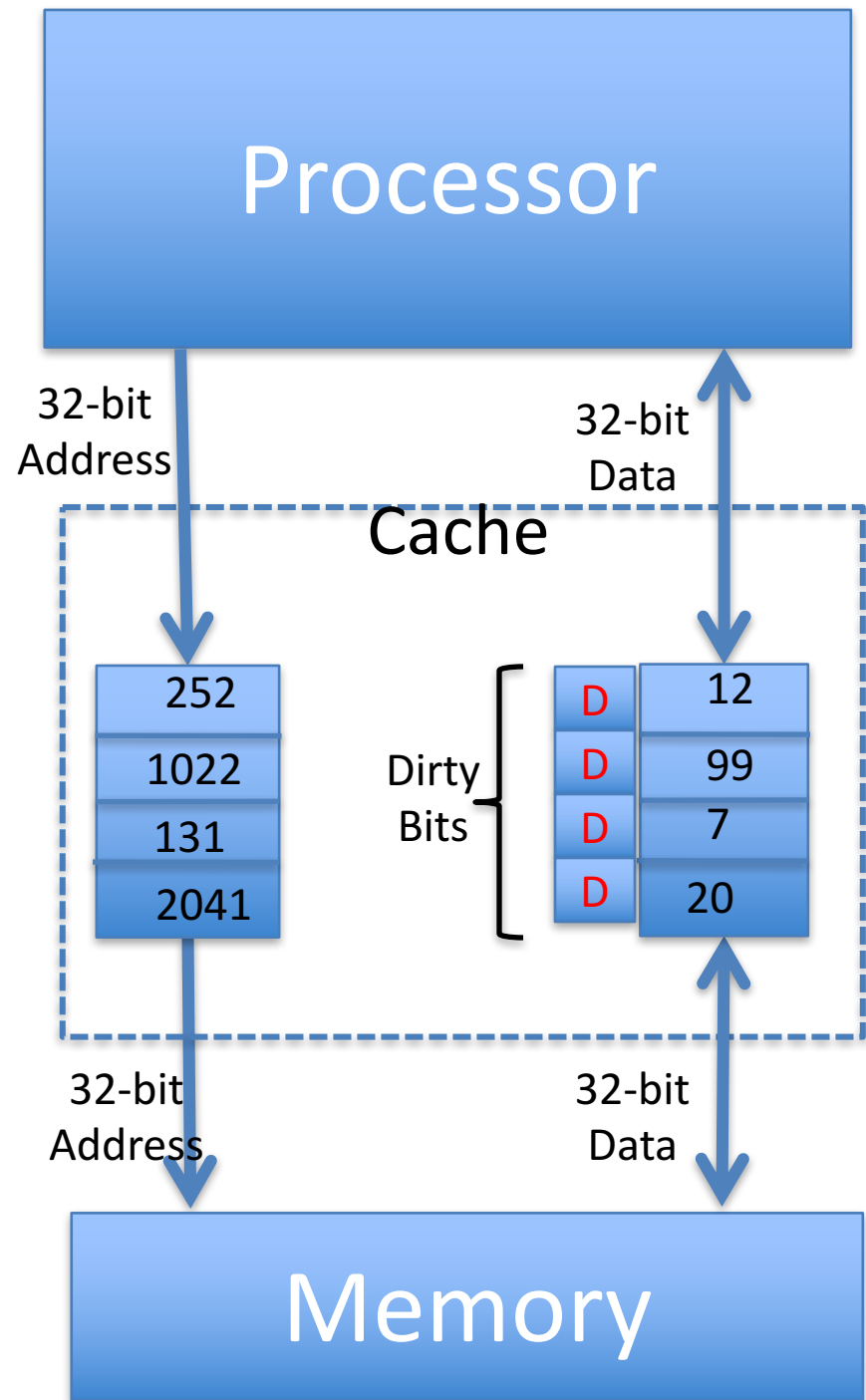


Handling Stores with Write-Back

- 2) **Write-Back Policy**: write only to cache and then write cache block *back* to memory when evict block from cache
- Writes collected in cache, only single write to memory per block
 - Include bit to see if wrote to block or not, and then only write back if bit is set
 - Called “**Dirty**” bit (writing makes it “dirty”)

Write-Back Cache

- Store/cache hit, write data in cache *only* & set dirty bit
 - Memory has stale value
- Store/cache miss, read data from memory, then update and set dirty bit
 - “Write-allocate” policy
- Load/cache hit, use value from cache
- On any miss, write back evicted block, only if dirty. Update cache with new block and clear dirty bit.



Write-Through vs. Write-Back

- Write-Through:
 - Simpler control logic
 - More predictable timing
simplifies processor control logic
 - Easier to make reliable, since memory always has copy of data (big idea: Redundancy!)
- Write-Back
 - More complex control logic
 - More variable timing (0,1,2 memory accesses per cache access)
 - Usually reduces write traffic
 - Harder to make reliable, sometimes cache has only copy of data

Cache (*Performance*) Terms

- **Hit rate**: fraction of accesses that hit in the cache
- **Miss rate**: $1 - \text{Hit rate}$
- **Miss penalty**: time to replace a block from lower level in memory hierarchy to cache
- **Hit time**: time to access cache memory (including tag comparison)

Average Memory Access Time (AMAT)

- Average Memory Access Time (AMAT) is the average time to access memory considering both hits and misses in the cache

$$\text{AMAT} = \text{Time for a hit} + \text{Miss rate} \times \text{Miss penalty}$$

Given a 0.2ns clock, a miss penalty of 50 clock cycles, a miss rate of 2% per instruction and a cache hit time of 1 clock cycle, what is AMAT?

$$\text{AMAT} = 1 \text{ cycle} + 0.02 * 50 = 2 \text{ cycles} = 0.4\text{ns.}$$