

Question Consider generalizing Cohen-Sutherland clipping algorithm to a clipping window that is not an upright rectangle. Specifically, consider the scenarios where you have a clipping window which is (a) a convex polygon of n sides and (b) a concave polygon of n sides. Is that possible to generalize the outcode mechanism for trivial-accept and trivial-reject cases in the standard Cohen-Sutherland algorithm? If so, provide a concise description of how it works, if not, give an counter example.

Question We want to implement yet another 2D operation called tapering. Tapering is an operation that changes the width of an object perpendicular to an axis (the taper axis) passing through the centroid of the object. The change in the object's width is proportional to the distance away from the centroid along the taper axis, and the object becomes wider going in the positive sense of the axis and becomes narrower going in the negative sense of the axis. Given a taper axis direction of (a, b) , an object centroid (\bar{x}, \bar{y}) , and a taper factor t (t pixels change in width for every pixel movement away from the centroid along the taper axis), find the matrix in homogeneous coordinates that, when multiplied with a point with coordinate $[x, y, 1]^T$, generates the tapered version of that point. (**NOTE:** If the matrix is composed of several component transforms, you do not need to carry out the matrix multiplication to compose them. Also, you can leave trigonometric functions such as `sin` and `cos` as they are.)

Question Suppose in OpenGL the user chooses a perspective transformation and uses `glFrustum` to specify the view volume. The parameters to `glFrustum` are

left	5	view volume left edge
right	10	view volume right edge
top	-10	view volume top edge
bottom	-20	view volume bottom edge
near	4	view volume near clipping plane distance
far	10	view volume far clipping plane distance

Suppose that the viewer is at the origin and looks down along the $-z$ axis. It should be apparent that the view volume specified above is skewed to the right and downward from the $-z$ axis. Suppose we would like to center the view volume (and all the scene objects) around the $-z$ axis without changing the depth (z) of the scene objects. (Or this is the *shear* operation used in PHIGS.) Derive a transformation matrix in homogeneous coordinate which, when multiplied with an object point, will bring the point in the original view volume into a view volume which is centered around the $-z$ axis.